| Surname |
| :--- |
| First name(s) |


| Centre <br> Number | Candidate <br> Number |
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## GCSE

## шјес cbac

## 3300U60-1

## TUESDAY, 14 JUNE 2022 - MORNING

## MATHEMATICS <br> UNIT 2: CALCULATOR-ALLOWED <br> HIGHER TIER

1 hour 35 minutes

## ADDITIONAL MATERIALS

A calculator will be required for this examination.
A ruler, a protractor and a pair of compasses may be required.

## INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.
You may use a pencil for graphs and diagrams only.
Write your name, centre number and candidate number in the spaces at the top of this page.
Answer all the questions in the spaces provided.
If you run out of space, use the additional page at the back of the booklet. Question numbers must be given for all work written on the additional page.
Take $\pi$ as 3.14 or use the $\pi$ button on your calculator.

## INFORMATION FOR CANDIDATES

You should give details of your method of solution when appropriate.
Unless stated, diagrams are not drawn to scale.
Scale drawing solutions will not be acceptable where you are asked to calculate.
The number of marks is given in brackets at the end of each question or part-question.
In question 4, the assessment will take into account the

| For Examiner's use only |  |  |
| :---: | :---: | :---: |
| Question | Maximum <br> Mark | Mark <br> Awarded |
| 1. | 2 |  |
| 2. | 4 |  |
| 3. | 5 |  |
| 4. | 8 |  |
| 5. | 5 |  |
| 6. | 1 |  |
| 7. | 6 |  |
| 8. | 6 |  |
| 9. | 4 |  |
| 10. | 3 |  |
| 11. | 6 |  |
| 12. | 3 |  |
| 13. | 2 |  |
| 14. | 3 |  |
| 15. | 3 |  |
| 16. | 6 |  |
| 17. | 3 |  |
| Total | 70 |  |
|  |  |  |

communication and accuracy in writing.


## Formula List - Higher Tier

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


In any triangle $A B C$
Sine rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$
Area of triangle $=\frac{1}{2} a b \sin C$


## The Quadratic Equation

The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$ are given by $\quad x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

## Annual Equivalent Rate (AER)

AER, as a decimal, is calculated using the formula $\left(1+\frac{i}{n}\right)^{n}-1$, where $i$ is the nominal interest rate per annum as a decimal and $n$ is the number of compounding periods per annum.

1. Rotate the shape below through $90^{\circ}$ clockwise about the point $(-1,1)$.


(b) Expand and simplify $(y+5)(y-4)$.
2. The height of a cylinder is $24 \cdot 8 \mathrm{~cm}$.

The ratio of the diameter of the cylinder to the height of the cylinder is $3: 2$.
Find the volume of the cylinder.
Give your answer correct to 2 significant figures.
You must show all your working.
4. In this question, you will be assessed on the quality of your organisation, communication and accuracy in writing.


In the diagram above, the area of triangle $B C D$ is $60 \mathrm{~cm}^{2}$.
Calculate the length of $C D$.
You must show all your working.

Diagram not drawn to scale
5. (a) Factorise $8 x^{2}+6 x y$.
$\qquad$
$\qquad$
$\qquad$
(b) (i) Factorise $x^{2}+13 x+40$.
$\qquad$
$\qquad$
$\qquad$
(ii) Explain how you can check that your answer to part (i) is correct.
$\qquad$
$\qquad$
$\qquad$
6. Calculate $5.7 \times 10^{5} \times 6.4 \times 10^{-2}$.

Circle the correct answer.

$$
\begin{array}{lllll}
3.648 \times 10^{8} & 3.648 \times 10^{4} & -3.648 \times 10^{6} & 3.648 \times 10^{3} & 3.648 \times 10^{6}
\end{array}
$$

7. (a) The diagram below shows a right-angled triangle.


Diagram not drawn to scale

Calculate the value of $x$.
$\qquad$
(b) The diagram below shows a different right-angled triangle.


Diagram not drawn to scale

Calculate the value of $y$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
y=
$$

8. This cuboid has:

- length $=5 \mathrm{~cm}$
- width $=x \mathrm{~cm}$
- height $=\left(x^{2}+3\right) \mathrm{cm}$
- volume $=132 \mathrm{~cm}^{3}$.

Diagram not drawn to scale
(a) Show that $5 x^{3}+15 x=132$.
$\qquad$
(b) (i) A solution of the equation

$$
5 x^{3}+15 x=132
$$

lies between 2 and 3 .
Use the method of trial and improvement to find this solution correct to 1 decimal place.
You must show all your working.


## (a) Show that $5 x^{3}+15 x=132$

 ](ii) Hence, find the height of the cuboid.

Examiner

Height of the cuboid $=\ldots . . . .$.
9. Calculate the total surface area of a solid hemisphere with a radius of 34 cm .


Diagram not drawn to scale

Total surface area $=$
$\mathrm{cm}^{2}$
10. The value of $y$ is found using the formula $y=\frac{t}{w}$.

Examiner
$t=98$, correct to 2 significant figures.
$w=0 \cdot 5$, correct to 1 significant figure.
Calculate the least value of $y$.
Give your answer correct to 1 decimal place.
You must show all your working.

Least value of $y=$
11. The diagram shows a triangle $A B C$ and a circle with centre $A$. The points $B$ and $D$ lie on the circumference of the circle.

The length of the line $A C$ is 27 cm . The area of triangle $A B C$ is $112 \mathrm{~cm}^{2}$.


Diagram not drawn to scale

Calculate the area of the shaded region.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Area of shaded region $=$
$\mathrm{cm}^{2}$
12. Express the following as a single fraction in its simplest form.

$$
\frac{4}{3 x-7}+\frac{5}{2 x+9}
$$

13. Three fair spinners are shown in the diagram below.


The three spinners are spun.
Calculate the probability that all the spinners will land on an even number.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
14. The graph of $y=12+x-x^{2}$, for values of $x$ from $x=0$ to $x=4$, is drawn below.


Use the trapezium rule, with the ordinates $x=0, x=1, x=2, x=3$ and $x=4$, to estimate the area of the region bounded by the curve, the positive $x$-axis and the positive $y$-axis.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
15.


Calculate the size of $X \widehat{Y} Z$.
16. Shape $A$ is a square and Shape $B$ is a rectangle, as shown below.


$(5 x+1) \mathrm{cm}$

The area of square $A$ is equal to the area of rectangle $B$.
Form an equation in $x$ and hence calculate the value of $x$.
Give your answer correct to 1 decimal place.
You must show all your working.

## $x=$

17. Solid $A$ and Solid $B$ are similar.

Solid A has a volume of $8000 \mathrm{~cm}_{3}^{3}$ and a height of 30 cm . Solid B has a volume of $4913 \mathrm{~cm}^{3}$.

Calculate the height of Solid B.
$\qquad$

Height of Solid B = cm

## END OF PAPER



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