

Please write clearly in	block capitals.		
Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature			

# GCSE MATHEMATICS

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Higher Tier

Paper 3 Calculator

Tuesday 13 June 2017

Morning

Time allowed: 1 hour 30 minutes

## **Materials**

## For this paper you must have:

- a calculator
- · mathematical instruments.



### Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper.
   These must be tagged securely to this answer book.

## **Advice**

• In all calculations, show clearly how you work out your answer.

For Exam	iner's Use
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26	
TOTAL	

# Answer all questions in the spaces provided

1 
$$\mathbf{a} = \begin{pmatrix} -4 \\ -1 \end{pmatrix}$$
 and  $\mathbf{b} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$ 

Circle the vector 2a + b

[1 mark]

$$\begin{pmatrix} -5 \\ -3 \end{pmatrix}$$

$$\begin{pmatrix} -5 \\ -3 \end{pmatrix} \qquad \begin{pmatrix} -11 \\ -3 \end{pmatrix} \qquad \begin{pmatrix} -5 \\ -1 \end{pmatrix} \qquad \begin{pmatrix} -11 \\ -1 \end{pmatrix}$$

$$\begin{pmatrix} -5 \\ -1 \end{pmatrix}$$

$$\begin{pmatrix} -11 \\ -1 \end{pmatrix}$$

Which of these values of n makes  $2.7 \times 10^n$  a cube number? 2 Circle your answer.

[1 mark]

 $2x = \frac{y}{w}$  to make w the subject. Rearrange 3

Circle your answer.

[1 mark]

$$w = \frac{2y}{x} \qquad \qquad w = \frac{2x}{y} \qquad \qquad w = \frac{x}{2y}$$

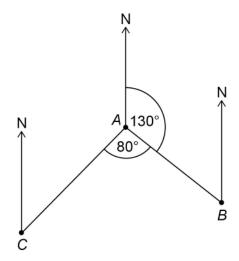
$$w = \frac{2x}{y}$$

$$w = \frac{y}{2x}$$

$$w = \frac{x}{2y}$$

3

4



Not drawn accurately

Work out the bearing of C from A.

Circle your answer.

[1 mark]

030°

130°

150°

210°

Turn over for the next question

4



Answer		nds on Tails 2		
Answer	The relative	ve frequency	of Tails is 0.4	
Answer	Work out	the number	of times the coin was thrown.	
Answer				I
Answer				·
Answer				
How are the whole number solutions to A and B different? A Solve $3 \le 3x < 18$ B Solve $3 < 3x \le 18$				
How are the whole number solutions to A and B different? A Solve $3 \le 3x < 18$ B Solve $3 < 3x \le 18$			Answer	
A Solve $3 \le 3x < 18$ B Solve $3 < 3x \le 18$				
A Solve $3 \le 3x < 18$ B Solve $3 < 3x \le 18$				
B Solve $3 < 3x \le 18$	How are t	he whole nu	mber solutions to A and B different?	
B Solve $3 < 3x \le 18$				
	Δ	Solve	3 / 3r / 18	
				I
				ļ



7 (a)	The length of a pipe is 6 metres to the nearest metre.	
	Complete the error interval for the length of the pipe.	[2 marks]
	Answer m ≼ length <	m
7 (b)	The length of a different pipe is 4 metres to the nearest metre.  Olly says,  "The total length of the two pipes is 11 metres to the nearest metre."  Give an example to show that he could be correct.	[2 marks]
	Turn over for the next question	

8



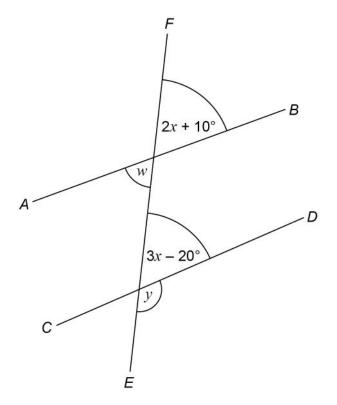
8	This shape is made from two triangles and four congruent parallelog	rams.
		Not drawn accurately
	For each statement, tick the correct box.	
8 (a)	The triangles are equilateral.	[1 mark]
	Must be true	
	Could be true	
	Must be false	
8 (b)	The triangles are congruent.	
		[1 mark]
	Must be true	
	Could be true	
	Must be false	



9	There are 720 boys and 700 girls in a school.	
	The probability that a boy chosen at random studies French is $\frac{2}{3}$	
	The probability that a girl chosen at random studies French is $\frac{3}{5}$	
9 (a)	Work out the number of students in the school who study French.  [3 marks]	
	Answer	
9 (b)	Work out the probability that a student chosen at random from the whole school does <b>not</b> study French.  [2 marks]	
	Answer	
	Turn over for the next question	



AB, CD and EF are straight lines.



Not drawn accurately

**10 (a)** Ava assumes that *AB* and *CD* are parallel.

What answer should she get for the size of angle y?

[4 marks]

Answer \_\_\_\_\_ degrees

What effect does this have on the size of angle <i>y</i> ?  Tick a box.	
y is bigger	
y is the same	
y is smaller	
Show working to support your answer.  [3 marks]	
Turn over for the next question	
	y is the same  y is smaller  Show working to support your answer.  [3 marks]



Purple paint is made by mixing red paint and blue paint in the ratio 5 : 2
Yan has 30 litres of red paint and 9 litres of blue paint.

What is the **maximum** amount of purple paint he can make?

[3 marks]

Answer litres

12  $\left(ar^b\right)^4 = 16r^{20}$  where a and b are positive integers.

Work out a and b

[2 marks]

a = \_\_\_\_\_ b = \_\_\_\_

13 In a class of 28 students

the mean height of the 12 boys is 1.58 metres

the mean height of all 28 students is 1.52 metres.

Work out the mean height of the girls.

[4 marks]

14 xy = c where c is a constant. Circle the correct statement.

[1 mark]

y is directly proportional to 
$$x$$
 y is directly proportional to  $\frac{1}{x}$ 

$$y$$
 is inversely proportional to  $\frac{1}{x}$   $x$  is directly proportional to  $y$ 

Turn over for the next question

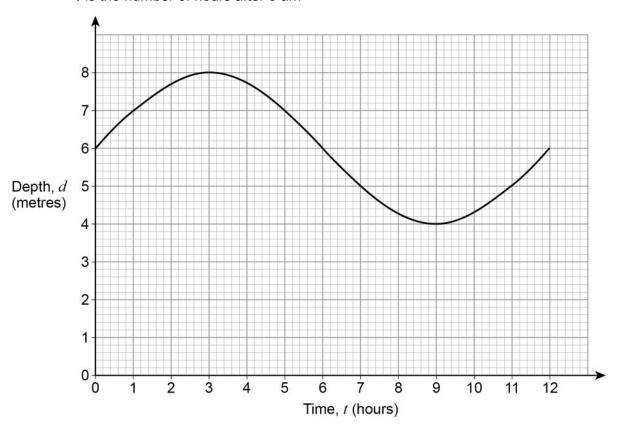
10



The graph shows the depth of water in a harbour for 12 hours.

d is the depth of water in a harbour in metres

t is the number of hours after 9 am



**15 (a)** For how many of the 12 hours is the depth more than 5 metres?

[1 mark]

Answer

**15 (b)** By how much does the depth change between 12 noon and 4 pm?

[1 mark]

Answer \_\_\_\_\_ metres



The value of a new car is £18 000	
The value of the car decreases by	
25% in the first year	
12% in each of the next 4 years.	
Work out the value of the car after 5 years.	
[3 marks]	]
	-
	-
	_
	-
	-
	_
	-
Answer £	

Turn over for the next question

5



17 Liam drives his car.

He drives the first 9 miles in 9 minutes.

He then drives at an average speed of 70 miles per hour for 1 hour 36 minutes.

He finds this information about his car.

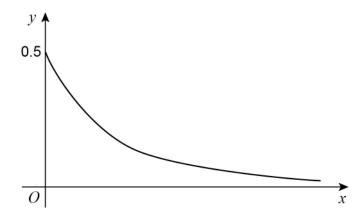
Average speed	Miles travelled per gallon
65 miles per hour or less	50
More than 65 miles per hour	40

Use the information to show that his car uses less than 3 gallons of petrol for the drive.

[5 marks]



Nick sketches the graph of  $y = 0.5^x$  for  $x \ge 0$ 



Make one criticism of his sketch.

[1 mark]

Turn over for the next question

6



A, B, C, D and E are points on a circle.  BFD and AFC are straight lines.  DC = DF  Not drawn accurately  Work out the size of angle x.  You must show your working which may be on the diagram.  [4 m.	BFD and AFC are straight lines. $DC = DF$ Not drawn accurately  Work out the size of angle $x$ .	BFD and AFC are straight lines.  DC = DF  Not drawn accurately  Work out the size of angle x.  You must show your working which may be on the diagram.	BFD and AFC are straight lines.  DC = DF  Not drawn accurately  Work out the size of angle x.  You must show your working which may be on the diagram.	A B C D and F are points on a circle	
Work out the size of angle $x$ .  You <b>must</b> show your working which may be on the diagram.	Work out the size of angle $x$ .  You <b>must</b> show your working which may be on the diagram.	Work out the size of angle $x$ .  You <b>must</b> show your working which may be on the diagram.	Work out the size of angle $x$ .  You <b>must</b> show your working which may be on the diagram.	BFD and AFC are straight lines.	
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				Work out the size of angle $x$ .	



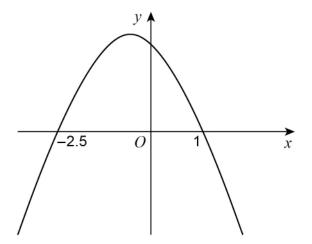
This sign shows when a lift is safe to use.
Total mass of people must be 450 kg or less
Ben and some other people are in the lift.
Their total mass is 525 kg to the nearest 5 kg
Ben gets out.
He has a mass of 78 kg to the nearest kg
Is the lift now safe to use?
You <b>must</b> show your working.
[4 marks]
<b>A</b>
Answer
Turn over for the next question

8



21 Here is a sketch of y = f(x) where f(x) is a quadratic function.

The graph intersects the *x*-axis where x = -2.5 and x = 1



Not drawn accurately

Circle the solution of f(x) > 0

[1 mark]

$$x < -2.5$$
 or  $x > 1$ 

$$x > -2.5$$
 or  $x > 1$ 

$$-2.5 < x < 1$$

$$x > -2.5$$
 or  $x < 1$ 

Work out ar	Work out an expression for the $n$ th term of the quadratic sequence					
	2	17	40	71		
Give your a	nswer in the	e form ar	$n^2 + bn + c$	where $\iota$	a,b and $c$ are constant	s. [3 marks
		Answer				

Turn over for the next question

4

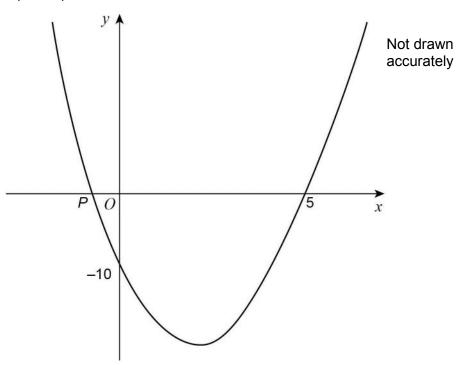


Here is a sketch of  $y = x^2 + bx + c$ 

The curve intersects

the x-axis at (5, 0) and point P

the y-axis at (0, -10)



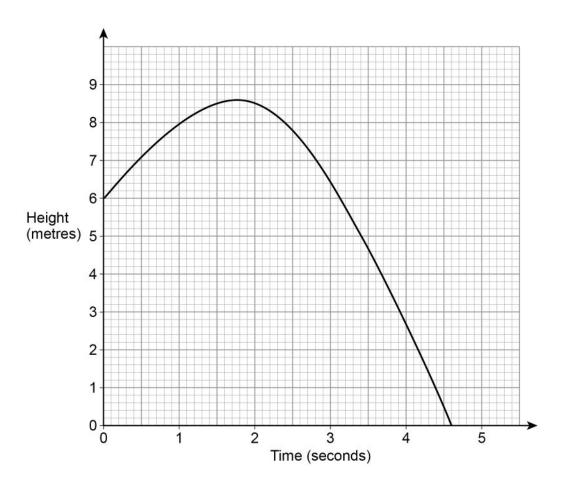
Work out the *x*-coordinate of the turning point of the graph.

[4 marks]

Answer \_\_\_\_

A ball is thrown from a point 6 metres above the ground.

The graph shows the height of the ball above the ground, in metres.



Estimate the speed of the ball, in m/s, after 1 second.

You **must** show your working.

[2 marks]

Answer m/s



**25** Rectangle *ABCD* is the horizontal base of a triangular prism *ABCDEF*.

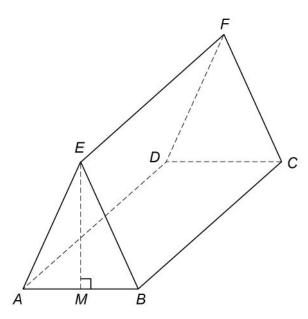
AE = BE

E is vertically above M, the midpoint of AB.

AB = 16 cm

$$AE = 17 \text{ cm}$$

BC = 30 cm



**25 (a)** Show that EM = 15 cm

[2 marks]

Ш		Ш	
Ш		Ш	Ш

Work out the size of angle <i>ECM</i> . <b>[4</b> I	marks]				
Answer degrees					
Turn over for the next question					
	Answer				

6



26 Here is an L-shape. All dimensions are in centimetres. -x-Not drawn accurately 9 3x + 1- 10 -



Work out the value of	on x.	[6 ma
		[6 ma
	Answer	

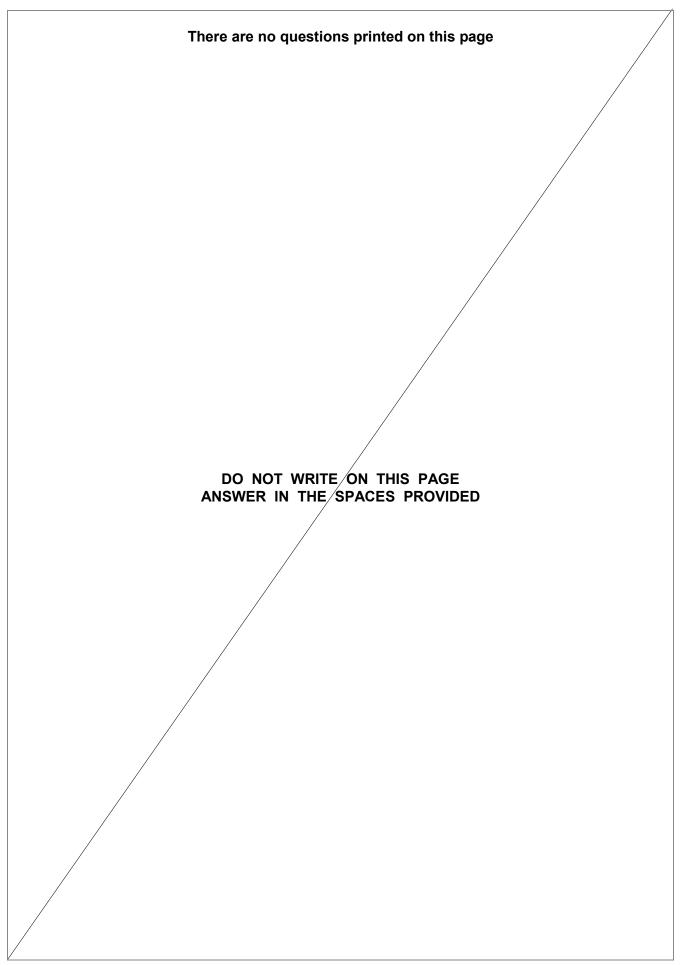


27	Prove that	$x^2 + x + 1$	is always positive.	[3 marks]

# **END OF QUESTIONS**

3







## There are no questions printed on this page

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