

# GCSE MATHEMATICS 8300/2H

Higher Tier Paper 2 Calculator

Mark scheme

November 2018

Version: 1.0. Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aga.org.uk

# **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

М	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≤ value < b
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

# **Diagrams**

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

# Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

### Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

# Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

# Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

# Work not replaced

Erased or crossed out work that is still legible should be marked.

# Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

# Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

# **Continental notation**

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Question	Answer	Mark	Comme	nts
	A and B	B1		
1	Add	litional G	uidance	
	(1, 5)	B1		
2		litional G	⊥ uidance	
	1 3 9 27 81	B1		
3	Additional Guidance			
	130°	B1		
4	Additional Guidance			
	Pi or π	B1	accept a value in range	e [3.14, 3.142]
	Additional Guidance			
5	Accept incorrect spelling if intention is clear eg accept pie			
	Answer $(C =) \pi d$			В0
	Answer $(C =) \pi d$ $(k =) \pi$			B1

Question	Answer	Mark	Comments		
	$2.5 \times 12$ or 30 and $7.5 \times 7$ or 52.5 and $12.5 \times 1$ or 95 $\frac{12.5 \times 1}{12 \times 1}$ their 30 + their 52.5 + their 12.5 $12 \times 1$ or $95 \div 20$	M1	allow one incorrect midpoint or [2, 3] × 12 and [7, 8] × 7 and [12, 13] (× 1) ignore $t \ge 15$ row $t \ge 15$ product must be 0 if seen condone bracket error seen eg 30 + 52.5 + 12.5 ÷ 20		
6(a)	4.75	A1	accept 4.8 or 5 if full working shown using <b>correct</b> midpoints		
	Additional Guidance				
	Two correct from 30, 52.5 and 12.5 implies the first mark and could be used to score up to M2			M1	
	Midpoints used in the ranges [2, 3], [7, 8] and [12, 13] must be seen eg $2.5\times12 \text{ and } 7\times7 \text{ and } 12\ (\times\ 1)$ or $3\times12$ and $7\times7$ and $13\ (\times\ 1)$ NB These could be used to score up to M2			M1	
	Correct products seen in the table but a different method shown in the working lines eg $20 \div 4 = 5$				
	Lower than part (a)	B1			
6(b)	Add	ditional G	uidance		

Question	Answer	Mark	Commer	nts
	Alternative method 1			
	35x + 6x = ax or $35 + 6 = a$ or $41x = ax$	M1		
	<i>a</i> = 41	A1		
_	40 + 3 <i>b</i> = 13	M1	oe	
	<i>b</i> = -9	A1	SC3 $a = 41$ , $b = -27$ or	$a = 41, b = \frac{5}{3}$
	Alternative method 2			
	35x + 40 + 6x + 3b or $41x + 40 + 3b$	M1		
	35x + 6x = ax or $35 + 6 = aand40 + 3b = 13$	M1dep	oe eg $41x = ax$ and $3b = ax$	–27
7	<i>a</i> = 41	A1	implies first M1 only	
7	<i>b</i> = -9	A1	SC3 $a = 41$ , $b = -27$ or $a = 41$ , $b = \frac{5}{3}$	
	Additional Guidance			
	a = 41 and $b = -9$			M1A1M1A1
	a = 41  or  b = -9			M1A1
_	35x, 40, $6x$ and $3b$ seen without addition signs shown or implied			M0
_	35x + 40 + 6x + b leading to an answer of $a = 41$ and $b = -27$			SC3
	$35x + 8 + 6x + 3b$ leading to an answer of $a = 41$ and $b = \frac{5}{3}$			SC3
	35x + 8 + 6x + b leading to an answer of $a = 41$ and $b = 5$			M1A1
	a = 41x			MO
	For $\frac{5}{3}$ accept 1.66 or 1.67			
	Condone multiplication signs eg 35 ×	<i>x</i> for 35 <i>x</i>		

Question	Answer	Mark	Comments		
	12 × 6 or 72	M1	oe area of rectangle		
	$\pi \times 6^2$ or $36\pi$ or [113, 113.112]	M1	oe may be implied $eg \ \pi \times 6^2 \div 4 \ or \ 9\pi \ or \ [28.2, 28.3]$		
	$\pi \times 6^2 \div 2$ or $18\pi$ or [56.4, 56.6]	M1dep	oe dep on 2nd M1		
	[15.4, 15.5] or 72 – 18π	A1			
8	Additional Guidance				
	$72 - 18\pi = 54\pi$			M1M1M1A0	
	$\pi \times 6^2 \div 2$ scores 2nd and 3rd M1				
	$12 \times 6 = 72$ $72 \div 2 = 36$ (unless identified as half of	(1st) M0			
	$\pi \times 6^2$ scores 2nd M1 even if subsequently used incorrectly				
	eg $\pi \times 6^2 = 36\pi$ $36\pi \times 2 = 72\pi$			(2nd) M1	
	Ignore units throughout			(=::3) ::::	

Comments

	Alternative method 1 comparing with	n 7.5 minut	tes	
	180 ÷ 135 or 180 ÷ 14 or 79.8 ÷ 14 or 79.8 ÷ 135	M1	oe or reciprocals	
	$\frac{14 \times 135}{180}$ or 10.5 or $\frac{79.8 \times 180}{135}$ or 106.4	M1dep	oe or reciprocals	
	$\frac{79.8 \times 180}{14 \times 135}$ or 7.6	M1dep	oe eg 79.8 ÷ 10.5 or 106.4 ÷ 14	
9	No and 7.6 (and 7.5)	A1	oe eg No and 7 minutes 36 seconds (and 7 minutes 30 seconds)	
	Alternative method 2 comparing with 79.8 litres			
	135 ÷ 180 or 14 ÷ 180 or 7.5 × 14 or 7.5 ÷ 180	M1	oe or reciprocals	
	$\frac{14 \times 135}{180}$ or 10.5 or $\frac{7.5 \times 135}{180}$ or 5.625	M1dep	oe or reciprocals	
	$\frac{7.5 \times 135 \times 14}{180}$ or 78.75	M1dep	oe eg 10.5 × 7.5 or 5.625 × 14	
	No and 78.75	A1		

Mark

Question

**Answer** 

Alternative methods and Additional Guidance continued on the next two pages

Question	Answer	Mark	Comments	
	Alternative method 3 comparing with 14 litres per minute			
	180 ÷ 135 or 180 ÷ 7.5 or 79.8 ÷ 135 or 79.8 ÷ 7.5	M1	oe or reciprocals	
	$\frac{7.5 \times 135}{180}$ or 5.625 or $\frac{79.8 \times 180}{135}$ or 106.4	M1dep	oe or reciprocals	
	$\frac{79.8 \times 180}{7.5 \times 135}$ or [14.18, 14.19]	M1dep	oe	
	No and [14.18, 14.19]	A1		
	Alternative method 4 comparing new rate of flow with rate required			
9	135 ÷ 180 or 14 ÷ 180	M1	oe or reciprocals	
cont	$\frac{14 \times 135}{180}$ or 10.5	M1dep	oe	
	79.8 ÷ 7.5 or 10.64	M1	oe	
	No and 10.5 and 10.64	A1		
	Alternative method 5 comparing with 135 degrees			
	180 ÷ 14 or 180 ÷ 7.5 or 79.8 ÷ 14 or 79.8 ÷ 7.5	M1	oe or reciprocals	
	180 ÷ 14 <b>and</b> 79.8 ÷ 7.5 or 180 ÷ 7.5 <b>and</b> 79.8 ÷ 14	M1dep	oe or matching reciprocals	
	$\frac{79.8 \times 180}{7.5 \times 14}$ or 136.8	M1dep	dep on M2	
	No and 136.8	A1		

# Additional Guidance continued on the next page

Question Answer	Mark	Comments
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	Additional Guidance				
	No may be implied eg It takes more				
	7.3(0) used for 7.5 may score up to M3				
9 cont	$7\frac{1}{2}$ minutes converted to 7.3(0) or 7 minutes 50 seconds	A0			
	Ignore incorrect conversion of 7.6 to minutes and seconds if 7.6 seen				
	Use the scheme that awards the most marks and ignore choice				

Question	Answer	Mark	Commen	ts
	4x + 5 = 6x - 10 or $4x + 5 = 10(x - 4)$ or $6x - 10 = 10(x - 4)$	M1	oe eg $4x + 5 + 6x - 10 = 2$ condone $10x - 4$ for $10(x)$	,
	4x - 6x = -10 - 5 or $-2x = -15$ or $4x - 10x = -40 - 5$ or $-6x = -45$ or $6x - 10x = -40 + 10$ or $-4x = -30$	M1dep	oe collection of terms eg $4x + 6x - 20x = -80 - 60$ or $-10x = -75$ condone $10x - 4$ for $10(x)$ eg $4x - 10x = -4 - 5$ or $6x - 10x = -4 + 10$	
	( <i>x</i> =) 7.5	A1	oe may be implied by (side I or (perimeter =) 105	ength =) 35
10	$(6 \times \text{their } 7.5 - 10) \times 3$ or $(4 \times \text{their } 7.5 + 5) \times 3$ or $10 \times (\text{their } 7.5 - 4) \times 3$ or $35 \times 3$ or $6 \times \text{their } 7.5 - 10 + 4 \times \text{their } 7.5 + 5$ $+ 10 \times (\text{their } 7.5 - 4)$ or $20 \times \text{their } 7.5 - 45$ or 105	M1dep	oe dep on M1M1 condone $10x - 4$ for $10(x - 4)$ must show working if M1M1A0	
	105 and Yes	A1	oe eg 1.05 and Yes	
	Ac	ditional G	Guidance	
	4x + 5 = 6x - 10 = 10(x - 4)			M1
	Condone $10x - 4$ for $10(x - 4)$ for up to M3			

Question	Answer	Mark	Comments	
	3.041 3.14 – 3.041 = 0.09	M1	condone 3.042	
11	or $3.041 + 0.1 = 3.141$ or $3.041$ and $3.14 - 0.1 = 3.04$	A1	condone 3.042 for 3.041	
	Additional Guidance			
-	Must see calculation for the A mark			
	Do not allow use of a more precise value of $\pi$ for the A mark			

Question	Answer	Mark	Commer	nts
	2.85 × 10 <sup>6</sup>	B2	B1 correct value not in s eg 2 850 000 or 28.5 × or 2.9 × 10 <sup>6</sup>	
	Ado	ditional G	uidance	
	Condone different spacing or comma	s eg 2850	0000 or 28,50,000	B1
	2.85.10 <sup>6</sup>			B1
	$2.85 \times 10^6$ in working with $2.9 \times 10^6$ on answer line			B2
12	$2.85 \times 10^6$ in working with $3 \times 10^6$ on answer line			B2
	$2.9 \times 10^6$ in working with $3 \times 10^6$ on answer line			B1
	3 × 10 <sup>6</sup> only			В0
	2.85 × 10 <sup>6</sup> in working with 2 850 000 on answer line			B1
	2 850 000 in working with 2 900 000 on answer line			B1
	2 900 000 only			В0
	2 850 000 in working with 2.8 × 10 <sup>6</sup> on answer line			B1
	$2.8 \times 10^6$ only			В0

Question	Answer	Mark	Comments	
	Evaluates method		eg1 his method does not 1.2 m does not divide exa	
			eg2 there are not a whol 50 cm in 1.2 m	e number of
		B1	eg3 50 cm will not fit in 0	).2 m
		ы	eg4 $1.2 \div 0.5 = 2.4$ which number	h is not a whole
			eg5 120 ÷ 50 = 2.4 and 6 boxes	cannot have 2.4
			eg6 can only fit 2 layers of boxes	
13	Evaluates claim	D4	eg1 he can only fit 40	
		B1	eg2 he will not fit (as many as) 48	
	Additional Guidance			
	Volume divided volume doesn't always work			(1st) B0
	He is wrong as he can put 42 boxes			(2nd) B0
	Only 2 layers will fit so he can't fit 48 boxes			B1B1
	Can't have 0.4 of a box so he can only fit 45 boxes			B1B0
	$5 \times 4 \times 2 = 40$			B0B1

Question	Answer	Mark	Comments	
	3 <i>n</i>	B1		
14		ditional G	uidance	
	- 1			

	Alternative method 1		
	45 ÷ (22 + 3) or 45 ÷ 25 or 1.8	M1	oe eg $\frac{45}{25}$
	22 × their 1.8 or 39.6 or 3 × their 1.8 or 5.4	M1dep	
	their 39.6 × 8.96 + their 5.4 × 7.31 or [354, 355] + [39, 40]	M1dep	
	394.29 or 394.3	A1	
15	Alternative method 2		
	45 ÷ (22 + 3) or 45 ÷ 25 or 1.8	M1	oe eg $\frac{45}{25}$
	their 1.8 × 8.96 or [16.1, 16.13] or their 1.8 × 7.31 or [13.1, 13.2]	M1dep	
	their [16.1, 16.13] × 22 + their [13.1, 13.2] × 3 or [354, 355] + [39, 40]	M1dep	
	394.29 or 394.3	A1	

Alternative method and Additional Guidance continued on the next page

Question	Answer	Mark	Comments	
	Alternative method 3			
	45 ÷ (22 + 3) or 45 ÷ 25 or 1.8	M1	oe eg $\frac{45}{25}$	
	22 × 8.96 or [197, 197.12] or 3 × 7.31 or [21.9, 22]	M1		
15 cont	their [197, 197.12] × their 1.8 + their [21.9, 22] × their 1.8 or [354, 355] + [39, 40]	M1dep	oe dep on M1M1	
	394.29 or 394.3	A1		
	Additional Guidance			
	Allow up to M2 even if not subseque	ntly used		
	Ignore units throughout			
	106	B1		
16(a)	Additional Guidance			

Question	Answer	Mark	Comments		
16(b)	50 - 42 or 8 or $\frac{42}{50}$ or $\frac{21}{25}$ or 0.84 or 84% $\frac{8}{50}$ or $\frac{4}{25}$ or 0.16 or 16% Add Ignore incorrect conversion if correct	M1 A1 ditional G		M1A0	
17	could be even or odd  Ade	B1	Guidance		

Question	Answer	Mark	Comments	
	$\frac{10}{10+7+3}$ or $\frac{10}{20}$ or $\frac{5}{10}$ or $\frac{1}{2}$ or 0.5	M1	oe eg 50%	
	$\frac{1}{8}$ or 0.125 or 12.5%	A1	oe eg $\frac{1000}{8000}$ or $\frac{125}{1000}$	
	Ad	ditional G	Guidance	
	Ignore incorrect conversion if correct	answer s	een	
18(a)	Answer $\frac{1}{2}$			M1
	10 out of 20			M0
	10 : 20			M0
	Answer 1 out of 8		M1A0	
	Answer 1:8 is A0 but M1 is possible			
	$\frac{10}{20}$ $\frac{7}{20}$ $\frac{3}{20}$			M1

Question	Answer	Mark	Comments		
	$\frac{10}{19}$ or $\frac{3}{19}$	M1	oe allow [0.52, 0.53] or [0.15, 0.16]		
	$\frac{10}{19} \times \frac{3}{18} (\times 2)$ or $\frac{3}{19} \times \frac{10}{18} (\times 2)$ or $\frac{5}{57} (\times 2)$ or $[0.087, 0.088] (\times 2)$	M1dep	oe eg $1 \times \frac{10}{19} \times \frac{3}{18}$ or $\frac{30}{342}$ allow $[0.52, 0.53] \times [0.16, 0.17]$ or $[0.15, 0.16] \times [0.55, 0.56]$		
	10/57 or 0.175 or 17.5%	A1	oe eg $\frac{60}{342}$ SC2 $\frac{7}{38}$ or 0.184 oe		
	Additional Guidance				
18(b)	$\frac{7}{20} \times \frac{10}{19} \times \frac{3}{18}$			M1M0A0	
	$\frac{7}{20} \times \frac{3}{19} \times \frac{10}{18}$			M1M0A0	
	If more than one product is seen, the for 2nd M1	correct on	e(s) must be selected		
	$\frac{10}{19} \times \frac{6}{18} + \frac{3}{19} \times \frac{10}{18}$			M1M0A0	
	Both correct products selected but multiplied together scores M1 only $\frac{10}{19} \times \frac{3}{18} \times \frac{3}{19} \times \frac{10}{18}$ M1M0A0 Ignore incorrect conversion if correct answer seen $5 \text{ out of } 57 \text{ cannot score } 2\text{nd M1 but implies } 1\text{st M1}$ $5:57 \text{ cannot score } 2\text{nd M1 but } 1\text{st M1 is possible}$				
	Answer 10 out of 57			M1M1A0	
	Answer 10 : 57 is A0 but M2 or M1M	0 is possib	le		

Question	Answer	Mark	Commer	nts
19	$4 \times 10 \text{ or } 40$ and $2 \times 3 \text{ or } 6$ or $\frac{2}{4} \text{ and } \frac{3}{10}$ or 0.5 and 0.3	M1	oe eg 50% and 30%	
	$\frac{2\times3}{4\times10}$ or $\frac{\text{their 6}}{\text{their 40}}$ or 0.15	M1dep	oe eg $\frac{3}{20}$ or $\frac{2}{4} \times \frac{3}{10}$	or 0.5 × 0.3
	15	A1		
	Ad	ditional G	uidance	
	2:4 and 3:10			MO

Question	Answer	Mark	Comments
20	$\frac{6n^2}{n} + 2n^3 \text{ or } 6n + 2n^3$ or $6n^3 - 6n$	M1	expands one bracket correctly allow $3 \times 2n$ for $\frac{6n^2}{n}$
	$\frac{6n^2}{n} + 2n^3 + 6n^3 - 6n$ or $6n + 2n^3 + 6n^3 - 6n$	M1dep	fully correct expansion allow $3 \times 2n$ for $\frac{6n^2}{n}$
	$8n^3$ and $(2n)^3$	A1	must have seen M1M1 oe eg $8n^3$ and $2n \times 2n \times 2n$ or $8n^3$ and $\sqrt[3]{8n^3} = 2n$ condone $8n^3$ and $2^3n^3$
	Additional Guidance		
	Do not allow $\frac{2n^2 \times 3}{n}$ for $\frac{6n^2}{n}$		

Question	Answer	Mark	Commen	ts	
	Alternative method 1				
	$y = \frac{k}{\sqrt{x}}$	M1	oe equation $ \text{implied by } 4 = \frac{k}{\sqrt{9}} \text{ oe } $		
	$(k =) 4 \times \sqrt{9}$ or $(k =) 12$	M1dep	oe		
	$y = \frac{12}{\sqrt{x}}$	A1	oe equation		
	Alternative method 2				
	$ky = \frac{1}{\sqrt{x}}$		oe equation		
	$\sqrt{x}$	M1	implied by $4k = \frac{1}{\sqrt{9}}$ oe		
21(a)	$(k =) \frac{1}{\sqrt{9}} \div 4 \text{ or } (k =) \frac{1}{12}$	M1dep	oe		
	$\frac{1}{12}y = \frac{1}{\sqrt{x}}$	A1	oe equation		
	Additional Guidance				
	Alt 1 $(k =)$ 12 or $(k \alpha)$ 12 with no incorrect working			M1M1	
	Condone use of α for up to M1M1A0				
	eg (Alt 1) $y \alpha \frac{k}{\sqrt{x}}$			M1	
	k α 12			M1dep	
	$y \propto \frac{12}{\sqrt{x}}$			A0	
	$y = \frac{12}{\sqrt{x}} \text{ oe}$			M1M1A1	

Question	Answer	Mark	Comments		
	$\frac{12}{\sqrt{25}}$ or $\frac{\text{their } k}{\sqrt{25}}$	M1	oe their k from (a)		
	2.4 or $\frac{12}{5}$ or $2\frac{2}{5}$	A1ft	ft $\frac{\text{their } k}{5}$		
	Ad	ditional G	iuidance		
2.4	y α 2.4			M1A0	
21(b)	$y = \frac{\frac{4}{3}}{\sqrt{x}} \text{ in (a)}$				
	$\frac{\frac{4}{3}}{\sqrt{25}}$			M1	
	$\frac{4}{15}$ (allow [0.266, 0.267])			A1ft	

Question	Answer	Mark	Comments	i
	$3(x-2)$ or $x^3(x^2-4)$ or $x^2(x^3-4x)$ or $x(x^4-4x^2)$ or $(x^4+2x^3)(x-2)$ or $x^3(x+2)(x-2)$ or $x^2(x^2+2x)(x-2)$ or $x(x^3+2x^2)(x-2)$	M1	numerator or denominator oe eg $x^2(x+2)(x^2-2x)$	factorised
	$3(x-2)$ and $x^3(x+2)(x-2)$ or $3(x-2)$ and $(x^4+2x^3)(x-2)$ or $3(x-2)$ and $x^2(x^2+2x)(x-2)$ or $3(x-2)$ and $x(x^3+2x^2)(x-2)$	A1	numerator and denominator each with factor (x – 2)  oe fully simplified expression	
22	$\frac{x^3(x+2)}{3}$ or $\frac{x^2(x^2+2x)}{3}$ or $\frac{x(x^3+2x^2)}{3}$ or $\frac{x^4+2x^3}{3}$	A1	eg $\frac{1}{3}x^3(x+2)$ or $\frac{x^4}{3} + \frac{2}{3}$	
	Additional Guidance			
	$\frac{x^3(x+2)}{3}$ followed by further incorrect work			M1A1A0
	$\frac{x^3 \times (x+2)}{3}$ or $\frac{1}{3} \times x^3 (x+2)$			M1A1A0
	$3 \times (x-2)$ and $x^3 \times (x+2) \times (x-2)$			M1A1
	$3 \times (x-2)$ or $x^3 \times (x^2-4)$			M1
	1(3x-6) or $-1(6-3x)$			M0
	-3(2-x)			M1
	$-3(2-x)$ and $-x^3(x+2)(2-x)$			M1A1

Question	Answer	Mark	Commer	nts	
	$-\frac{1}{3}a$	B1			
23	23 Additional Guidance				
24	Plots at least three of (0, 6) (-1, -1) (-2, -2) (-3, -3) (-4, -10)	M1	points may be implied by through the points tolerance ±2 mm	y a curve passing	
	Plots (0, 6) (-1, -1) (-2, -2) (-3, -3) (-4, -10) and joins with a smooth curve	A1	points may be implied by a curve passing through the points tolerance ±2 mm		
	Additional Guidance				
	Draws $y = f(x - 2)$ or $y = f(x) + 2$ or $y = f(x) - 2$			M0A0	

Question	Answer	Mark	Commer	nts
	$\tan 49 = \frac{AC}{16}$	M1	oe eg tan $(90 - 49) = \frac{16}{AC}$ or $AC^2 + 16^2 = \left(\frac{16}{\cos 49}\right)$	)2
	tan 49 × 16 or [18.4, 18.41]	M1dep	oe eg $\frac{16}{\tan{(90-49)}}$ or $\sqrt{\left(\frac{16}{\cos{49}}\right)^2 - 16^2}$	
25	$\frac{\sin x}{\text{their} [18.4, 18.41]} = \frac{\sin 35}{20}$ or $\frac{\text{their} [18.4, 18.41]}{\sin x} = \frac{20}{\sin 35}$	M1dep	oe eg $\frac{\sin x}{16 \tan 49} = \frac{\sin 3}{20}$ dep on 1st M1	3 <u>5</u>
	$\sin x = \frac{\sin 35}{20} \times \text{their} [18.4, 18.41]$	M1dep	oe eg sin $x = \frac{16 \tan 49}{20}$ or $\sin^{-1} \left( \frac{\sin 35}{20} \times \text{their } [1 \text{ or } \sin^{-1} [0.527, 0.528] \right)$ dep on 1st and 3rd M1	
	[31.8, 31.9]	A1	allow 32 with full method	l seen
	Additional Guidance			
	Answer [31.8, 31.9] possibly from scale drawing			5 marks
	Answer 32 possibly from scale drawing			Zero

Question	Answer	Mark	Comments
	$\frac{x^2-2}{x^2-2+2}$ or $\frac{x^2-2}{x^2}$	M1	
	$\frac{x^2}{x^2} - \frac{2}{x^2}$ or $1 - \frac{2}{x^2}$	A1	implied by correct final answer must be two terms oe eg $x^2x^{-2} - 2x^{-2}$
26	$1 - 2x^{-2}$ or	A1	
	a=1 and $b=-2$ and $n=-2$	ditional C	Guidance
	$\frac{1}{64} = k^3$ or $\sqrt[3]{\frac{1}{64}}$	M1	oe equation in $k$
	$(k =) \frac{1}{4}$ or $(k =) 0.25$		must see working for M1

	Additional Guidance		
	Additional Guidance		
	$\left(\frac{1}{4}\right)^{\frac{1}{2}} = \frac{1}{2} \text{ or } 0.25^{\frac{1}{2}} = 0.5$	A1	must see working for M1A1 allow $\sqrt{\frac{1}{4}} = \frac{1}{2}$ or $\sqrt{0.25} = 0.5$
27			implied by $y = \left(\frac{1}{4}\right)^x$ $\left(\frac{1}{4}\right)^3 = \frac{1}{64} \text{ is M1A1}$
	7	A1	implied by $y = \left(\frac{1}{4}\right)^x$
	$(k =) \frac{1}{4}$ or $(k =) 0.25$		must see working for M1
	$\frac{1}{64} = k^3$ or $\sqrt[3]{\frac{1}{64}}$	M1	oe equation in $k$

Question	Answer	Mark	Commer	nts
	0.25 or $\frac{1}{4}$ or $\frac{2}{8}$	B1		
28(a)	$m/s^2$ or $ms^{-2}$ or $m/s/s$ or $\frac{m}{s^2}$	B1	oe eg metres per secon SC2 acceleration and u eg 25 cm/s <sup>2</sup> or 3240 km	nit not in m/s <sup>2</sup>
	Ado	ditional G	uidance	
	$\frac{2}{14-6}$ with no further simplification			(1st) B0

	Alternative method 1		
	$\frac{1}{2} \times 6 \times (v-2)$ or $\frac{1}{2} \times (14-6) \times (v+v-2)$ or $(14-6) \times (v-2)$ or $\frac{1}{2} \times (14-6) \times 2$ or 8	M1	oe partial area any letter
28(b)	$\frac{1}{2} \times 6 \times (v-2)$ + $\frac{1}{2} \times (14-6) \times (v+v-2)$ or $3(v-2) + 8(v-2) + 8$ or $11v - 14$	M1dep	oe full area in one variable  eg $14 \times v - \frac{1}{2} \times 6 \times (v - 2)$ $-\frac{1}{2} \times 2 \times (6 + 14)$ implies M2
	$\frac{1}{2} \times 6 \times (v-2)$ + $\frac{1}{2} \times (14-6) \times (v+v-2) = 80$ or $94 \div 11$	A1	oe full area in one variable equated to 80
	8.5(4) or 8.55 or $\frac{94}{11}$ or $8\frac{6}{11}$	A1	

Alternative method and Additional Guidance continued on the next page

Alternative method 2 $ \frac{1}{2} \times 6 \times x $ or $\frac{1}{2} \times (14 - 6) \times (x + x + 2)$ or $(14 - 6) \times x$ or $\frac{1}{2} \times (14 - 6) \times 2$ or 8 $ \frac{1}{2} \times 6 \times x $ or $\frac{1}{2} \times (14 - 6) \times 2$ or 8 $ \frac{1}{2} \times 6 \times x $ or $3x + 8x + 8$ or $11x + 8$ or $11x + 8$ or $12 \times 6 \times x$ $ \frac{1}{2} \times 6 \times x $ $ \frac{1}{2} \times 6 \times x $ or $3x + 8x + 8$ or $11x + 8$ or $11x + 8$ or $11x + 8$ or $15x + 8$ or $15x$	Question	Answer	Mark	Comments
$ \frac{2}{2} \times 6 \times x $ or $\frac{1}{2} \times (14 - 6) \times (x + x + 2)$ or $(14 - 6) \times x$ or $\frac{1}{2} \times (14 - 6) \times 2$ or 8 $ \frac{1}{2} \times 6 \times x $ or $\frac{1}{2} \times (14 - 6) \times (x + x + 2)$ or $3x + 8x + 8$ or $11x + 8$ $ \frac{1}{2} \times 6 \times x $ $ + \frac{1}{2} \times (14 - 6) \times (x + x + 2) $ or $3x + 8x + 8$ or $11x + 8$ or $11x + 8$ $ \frac{1}{2} \times 6 \times x $ $ + \frac{1}{2} \times (14 - 6) \times (x + x + 2) = 80 $ or $72 \div 11$ or $6.5(4)$ or $6.55$ or $\frac{72}{11}$ or $6\frac{6}{11}$ 8.5(4) or $8.55$ or $\frac{94}{11}$ or $8\frac{6}{11}$ A1		Alternative method 2		
28(b) cont $ \begin{array}{cccccccccccccccccccccccccccccccccc$		or $\frac{1}{2} \times (14-6) \times (x+x+2)$ or $(14-6) \times x$	M1	x is the speed at 6 seconds
$\frac{1}{2} \times 6 \times x$ $+ \frac{1}{2} \times (14 - 6) \times (x + x + 2) = 80$ or $72 \div 11$ or $6.5(4)$ or $6.55$ or $\frac{72}{11}$ or $6\frac{6}{11}$ 8.5(4) or 8.55 or $\frac{94}{11}$ or $8\frac{6}{11}$ A1		$+ \frac{1}{2} \times (14 - 6) \times (x + x + 2)$ or $3x + 8x + 8$	M1dep	full area in one variable  eg $14 \times (x+2) - \frac{1}{2} \times 6 \times x$ $-\frac{1}{2} \times 2 \times (6+14)$
	Com	$+ \frac{1}{2} \times (14 - 6) \times (x + x + 2) = 80$ or $72 \div 11$ or $6.5(4)$ or $6.55$	A1	
Additional Guidance		8.5(4) or 8.55 or $\frac{94}{11}$ or $8\frac{6}{11}$	A1	
		Additional		Guidance
First M1 Do not allow 8 from 14 – 6		First M1 Do not allow 8 from 14 – 6		
Ignore units throughout		Ignore units throughout		