

GCSE Mathematics

8300/2 – Paper 2 Higher Tier Mark scheme

June 2018

Version/Stage: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

Copyright © 2018 AQA and its licensors. All rights reserved.

AQA retains the copyright on all its publications. However, registered schools/colleges for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to schools/colleges to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

Μ	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
М dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≤ value < b
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

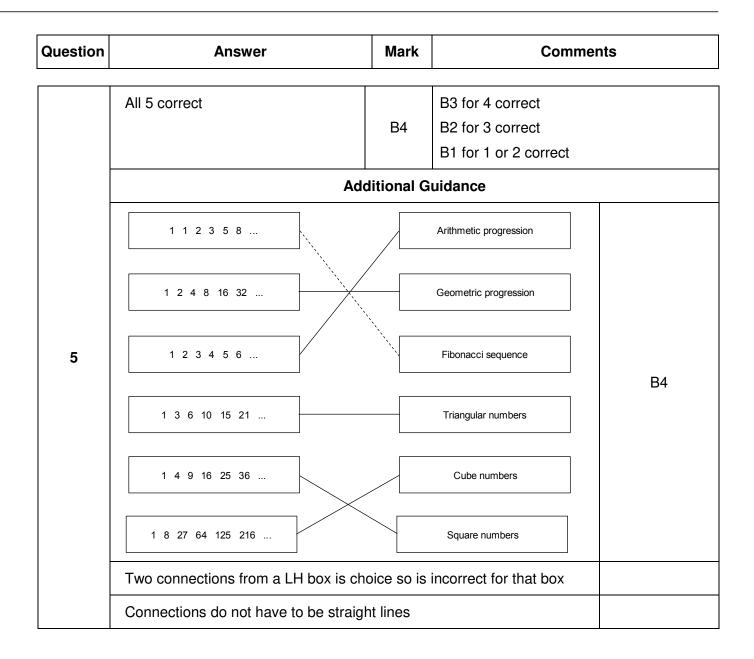
Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Question	Answer	Mark	Comments	
	segment	B1		
1	Add	itional G	uidance	

	6×10^{7}	B1					
2	2 Additional Guidance						

	3:2	B1			
3					

	400%	B1			
4	Addi	tional Gu	Jidance		



Question	Answer	Mark	Comments		
	Alternative method 1				
6	Any one of 60 000 ÷ 420 000 or 0.14 or 14.()% or $\frac{1}{7}$ or 480 000 ÷ 420 000 or 1.14 or 114.()% or $\frac{8}{7}$ or 420 000 ÷ 60 000 or 7 or 420 000 ÷ 60 000 or 0.875 or 87.5% or $\frac{7}{8}$ or 60 000 ÷ 540 000 or 0.11 or 11.()% or $\frac{1}{9}$ or 540 000 ÷ 60 000 or 9	M1	oe eg 60 000 : 420 000 or 1 : 7		
	Any one of $60\ 000 \div 480\ 000\ \text{or}\ 0.125$ or $12.5\%\ \text{or}\ \frac{1}{8}$ or $540\ 000 \div 480\ 000\ \text{or}\ 1.125$ or $112.5\%\ \text{or}\ \frac{9}{8}$ or $480\ 000 \div 60\ 000\ \text{or}\ 8$ or $480\ 000 \div 540\ 000\ \text{or}\ 0.88$ or $0.89\ \text{or}\ 88.()\%\ \text{or}\ 89\%\ \text{or}\ \frac{8}{9}$	M1	must be a matching pair (could be different forms) to award M2 (see A1 for list of matching pairs) oe eg 60 000 : 480 000 or 1 : 8 or 540 000 : 480 000 or 9 : 8		

Question	Answer	Mark	Comments		
	Alternative method 2				
	No and any one of		ое		
	$\frac{60\ 000}{420\ 000}$ × 480 000 and		B2 any one of the calculations		
	[67200, 68640]		B1 any one of the fractions oe		
	or		for on indept frontions, desired and		
	$\frac{60\ 000}{480\ 000}$ × 540 000 and 67 500		for equivalent fractions, decimals and percentages see Alternative method 1		
	or				
	$\frac{60\ 000}{480\ 000}$ × 420 000 and 52 500	ВЗ			
	or				
	$\frac{60\ 000}{540\ 000}$ × 480 000 and				
6 cont	[52 800, 53 334]				
	or	80			
	$\frac{420\ 000}{480\ 000}$ × 540 000 and 472 500				
	or				
	$\frac{480\ 000}{420\ 000}$ × 480 000 and				
	[547 200, 548 640]				
	or				
	$\frac{480\ 000}{540\ 000}$ × 480 000 and				
	[422 400, 427 200]				
	or				
	$\frac{540\ 000}{480\ 000}$ × 420 000 and 472 500				

Question	Answer	Mark	Commen	ts
	Add	litional G	uidance	
	In Alt 1, for M2 the matching pair do n eg 14.3% and $\frac{1}{8}$ and No	ot have to	be in comparable form	M1M1A0
6 cont	For comparable fractions, they must be same numerators or the same denomination of the same den	inators fo		M1M1A1
	For comparable ratios, they must be in same LH sides or the same RH sides eg Alt 1 60 000 : 420 000 and 60 000	for the A		M1M1A1
	If working with percentages, condone absence of % symbol eg Alt 1 14 and 12.5 and No			M1M1A1
	Both are increases of 60 000 and it is cannot be the same percentage	then over	different amounts so	M0M0A0

Question	Answer	Mark	Comments
7(a)	Two different probabilities from $\frac{15}{20}$ or 0.75 or 75% or $\frac{22}{30}$ or 0.73 or 73.()% or $\frac{17}{40}$ or 0.425 or 0.43 or 42.5% or 43% or $\frac{54}{90}$ or 0.6 or 60% or $\frac{37}{50}$ or 0.74 or 74% or $\frac{32}{60}$ or 0.53 or 53.()% or $\frac{39}{70}$ or 0.557 or 0.56 or 55.7% or 56%	B2	oe B1 for one correct probability

Question	Answer	Mark	Commer	nts	
	Additional Guidance				
	Accept $\frac{108}{180}$ as one of the probabilities	3			
	Mark the answer line if it has two answ probabilities in the working lines	vers ignor	ing any incorrect		
	Ignore any incorrect cancelling or char percentage)	nge of for	m (fraction, decimal or		
	If the answer line only has one answer, check the working lines for a second answer for B2. Ignore any extra probabilities, unless incorrect, in which case award B1 max				
7(a) cont	eg Working lines $\frac{15}{20}$ Answer line $\frac{54}{90}$			B2	
	eg Working lines $\frac{15}{20}$, $\frac{5}{15}$ Answer line	<u>54</u> 90		B1	
	If the answer line is blank, check the w B2. Ignore any extra probabilities, unle B1 max	•			
	eg Working lines $\frac{15}{20}$, $\frac{22}{30}$, $\frac{54}{90}$ Answer line blank			B2	
	eg Working lines $\frac{15}{20}$, $\frac{5}{15}$, $\frac{54}{90}$ Answer line blank			B1	
	Probabilities must not be given as ratio	DS			
	Do not accept the average of the giver	n probabi	ities as answer		

Question	Answer	Mark	Commer	nts	
	Alternative method 1 (ft their part (a))				
	Their probability with the greater number of trials	B1ft	ft their two different probabilities from part (a)		
	and valid reason eg More throws		both probabilities must h denominator based on th		
	Alternative method 2 (independent	of part (a))		
	54 90 and valid reason eg Total throws	B1	oe		
-	Additional Guidance				
-	Accept any unambiguous indication of their probability eg the day				
7(b)	Using ratios			B0	
	Ignore any non-contradictory statements				
	60% and It's for all three days			B1	
	$\frac{54}{90}$ and It takes into account more throws			B1	
	$\frac{17}{40}$ (with $\frac{22}{30}$ also in (a)) and Because he threw it more on Wednesday			B1ft	
	$\frac{54}{90}$ and Shows the overall probability			B1	
	$\frac{54}{90}$ and Probability over total throws			B1	
	$\frac{54}{90}$ (with Wednesday probability in (a)) and It's the average total days, not just Wednesdays			B1ft	

Question	Answer	Mark	Comments	
	Correct ft probability or $\frac{54}{90}$ and It's me	ore reliab	e	B0
	$\frac{54}{90}$ and There's a lot of data			B0
7(b) cont	Correct ft probability or $\frac{54}{90}$ and He may get better with more throws			B0
	$\frac{54}{90}$ and He throws 90 times	$\frac{54}{30}$ and He throws 90 times		
	Correct ft probability or $\frac{54}{90}$ and More	probability or $\frac{54}{90}$ and More hits		

	Alternative method 1		
	22.5(0) and 4		
	or		
	27 and 8		
	or		
	31.5(0) and 12		
	or		
	36 and 16		
	or	M1	
8	40.5(0) and 20		
	or		
	45 and 24		
	or		
	30 : 16		
	or		
	45 : 24		
	45 and 24 chosen	A1	eg 45 : 24 is the final ratio seen
	6	A1	

Mark scheme and additional guidance continues on the next page

Question	Answer	Mark	Commer	ıts	
	Alternative method 2				
	18 + 4.5x and 4x seen or $\frac{18 + 4.5x}{15} = \frac{4x}{8}$	M1	any letter oe sets up correct equation		
	8(18 + 4.5x) = 60x or $144 + 36x = 60x$ or $24x = 144$	M1dep	eliminates denominators oe	;	
8 cont	6	A1			
	Additional Guidance				
	Answer 6 that is not from incorrect method			M1A1A1	
	45 and 24 followed by eg 49.5(0) and 28 (answer not 6)			M1A0A0	
	Equivalent ratio to 15 : 8 that is not 30 : 16 or 45 : 24 eg 60 : 32 (answer not 6)			M0A0A0	
	Final calculation $\frac{15}{8} \times 24 = 45$ (answ	er not 6)		M1A1A0	

Question	Answer	Mark	Comments	
9(a)	8.35 and 8.45 in the correct order	B2	B1 8.35 on the left or 8.45 on the right or 8.45 and 8.35 in the wrong order accept 8.449 for 8.45	
	Ade	ditional G	uidance	
	Do not accept 8.449 for 8.449			

	41.75 and 42.25	B1ft	correct or ft their two diffe from (a) their 8.35 must be in the their 8.45 must be in the correct order or ft order accept 42.249 for 42.25	range (8.3, 8.4]
9(b)	Additional Guidance			
	(8.3, 8.4] does not include 8.3 but does include 8.4 (8.4, 8.5] does not include 8.4 but does include 8.5			
	Answer of 8.35 and 8.44 in part (a) leading to 41.75 and 42.2			B1ft
	Answer of 8 and 9 in part (a) leading to 40 and 45			B0ft

Question	Answer	Mark	Comments
	Alternative method 1		
	$\frac{4}{3}\pi \times 30^{3} \text{ or } 36\ 000\pi$ or [112 757, 113 112] or $\frac{1}{2} \times \frac{4}{3}\pi \times 30^{3} \text{ or } 18\ 000\pi$ or [55 954, 56 839]	M1	oe allow 1.33 for $\frac{4}{3}$ allow 0.66 or 0.67 for $\frac{2}{3}$
10	their [112 757, 113 112] ÷ 4000 or 9π or 28.() or their [55 954, 56 839] ÷ 4000 or $\frac{9\pi}{2}$ or [13.9, 14.21] or their [112 757, 113 112] ÷ (4000 × 60) or $\frac{3\pi}{20}$ or [0.46, 0.4713] or their [55 954, 56 839] ÷ (4000 × 60) or $\frac{3\pi}{40}$ or 0.23 or 0.24	M1dep	
	[13.9, 14.21] and Yes or 0.23 or 0.24 and Yes	A1	

Mark scheme and additional guidance continues on the next page

Question	Answer	Mark	Comments		
	Alternative method 2				
	$\frac{4}{3}\pi \times 30^{3} \text{ or } 36\ 000\pi$ or [112 757, 113 112] or $\frac{1}{2} \times \frac{4}{3}\pi \times 30^{3} \text{ or } 18\ 000\pi$ or [55 954, 56 839]	M1	oe allow 1.33 for $\frac{4}{3}$ allow 0.66 or 0.67 for $\frac{2}{3}$		
	4000 × 15 or 60 000	M1			
	[55 954, 56 839] and 60 000 and Yes	A1			
	Alternative method 3				
10 cont	$\frac{4}{3}\pi \times 30^{3} \text{ or } 36\ 000\pi$ or [112 757, 113 112] or $\frac{1}{2} \times \frac{4}{3}\pi \times 30^{3} \text{ or } 18\ 000\pi$ or [55 954, 56 839]	M1	oe allow 1.33 for $\frac{4}{3}$ allow 0.66 or 0.67 for $\frac{2}{3}$		
	their [112 757, 113 112] \div 15 or 2400 π or [7517, 7541] or their [55 954, 56 839] \div 15 or 1200 π or [3730, 3790]	M1dep			
	[3730, 3790] and Yes	A1			
	Additional guidance				
	Do not award A1 if incorrect conversion	on of $\frac{1}{4}$ ho	ur seen		

Answer	Mark	Commer	nts
$\frac{1}{3} \text{ or } \frac{2}{6} \text{ or } 0.33 \text{ or } 33.()\% \text{ on}$ each top branch and $\frac{2}{3} \text{ or } \frac{4}{6} \text{ or } 0.66 \text{ or } 0.67 \text{ or}$ 66.()% or 67% on each bottom branch	B1	accept any equivalent fra or percentage	action, decimal
Ado	ditional G	uidance	
Decimals must have at least 2 decimal places so do not accept 0.3 or 0.6 or 0.7			
Only accept the percentages shown, do not accept 30% or 60%			
Ignore working around the edge of the diagram			
$\frac{\frac{1}{3}}{\frac{\frac{2}{3}}{\frac{2}{3}}}$ Less than 3 $\frac{2}{3}$ 3 or more	$\begin{array}{c c} 1\\3\\2\\3\\1\\3\\2\\3\\2\\3\\3\end{array}$	Less than 3 3 or more Less than 3	B1
	$\frac{1}{3} \text{ or } \frac{2}{6} \text{ or } 0.33 \text{ or } 33.()\% \text{ on each top branch and } \frac{2}{3} \text{ or } \frac{4}{6} \text{ or } 0.66 \text{ or } 0.67 \text{ or } 66.()\% \text{ or } 67\% \text{ on each bottom branch } Add Decimals must have at least 2 decima or } 0.7 Only accept the percentages shown, of Ignore working around the edge of the \frac{1}{3} Less than 3$	$\frac{\frac{1}{3} \text{ or } \frac{2}{6} \text{ or } 0.33 \text{ or } 33.()\% \text{ on each top branch and B1}$ $\frac{\frac{2}{3} \text{ or } \frac{4}{6} \text{ or } 0.66 \text{ or } 0.67 \text{ or } 66.()\% \text{ or } 67\% \text{ on each bottom branch}$ Decimals must have at least 2 decimal places score or 0.7 Only accept the percentages shown, do not acceled lignore working around the edge of the diagram $\frac{\frac{1}{3}}{\frac{2}{3}}$ Less than 3 $\frac{\frac{1}{3}}{\frac{2}{3}}$ $\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{3}$	$\frac{1}{3}$ or $\frac{2}{6}$ or 0.33 or 33.()% on each top branch andaccept any equivalent fra or percentage $\frac{2}{3}$ or $\frac{4}{6}$ or 0.66 or 0.67 or 66.()% or 67% on each bottom branchB1Additional GuidanceDecimals must have at least 2 decimal places so do not accept 0.3 or 0.6 or 0.7Only accept the percentages shown, do not accept 30% or 60%Ignore working around the edge of the diagram $\frac{1}{3}$ Less than 3 $\frac{2}{3}$ 3 or more $\frac{1}{3}$ Less than 3

Question	Answer	Mark	Comments	
	1/9 or 0.11 or 11.()%	B1		
	Additional Guidance			
11(b)	Ignore probability words such as 'unlikely' or 'evens'			
	Accept equivalent answers eg $\frac{2}{18}$, $\frac{3}{27}$, 0.1			
	Do not accept 0.1 or 10%			

	Alternative method 1 Probabilities on branches in (a) all correct				
	$\frac{1}{3} \times \frac{2}{3} \text{ or } \frac{2}{3} \times \frac{1}{3} \text{ or } \frac{2}{9}$	M1	oe accept 0.33 for $\frac{1}{3}$ accept 0.66 or 0.67 for $\frac{2}{3}$		
11(0)	4/9 or 0.44 or 44.()%	A1			
11(c)	Alternative method 2 Probabilities	on branc	ches in (a) all correct		
	$1 - (\frac{1}{3} \times \frac{1}{3}) - (\frac{2}{3} \times \frac{2}{3})$	M1	oe accept 0.33 for $\frac{1}{3}$ accept 0.66 or 0.67 for $\frac{2}{3}$		
	4/9 or 0.44 or 44.()%	A1			

Question	Answer	Mark	Comments	
	Alternative method 3 Probabilities on branches in (a) not all correct			
11(c)	$\frac{1}{3} \times \text{their } \frac{2}{3}$ where their $\frac{2}{3}$ must be for 2nd dice 3 or more or their $\frac{2}{3} \times \text{their } \frac{1}{3}$ where their $\frac{2}{3}$ must be for 1st dice 3 or more and their $\frac{1}{3}$ must be for 2nd dice less than 3	M1	oe accept 0.33 for $\frac{1}{3}$ accept 0.66 or 0.67 for $\frac{2}{3}$ their fractions must be between 0 and 1	
cont	⁴ / ₉ or 0.44 or 44.()%	A1ft	ft their fractions	
	Alternative method 4 Probabilities on branches in (a) not all correct			
	$1 - (\frac{1}{3} \times \frac{1}{3}) - (\text{their } \frac{2}{3} \times \text{their } \frac{2}{3})$ where their $\frac{2}{3}$ must be for 1st dice 3 or more and their $\frac{2}{3}$ must be for 2nd dice 3 or more	M1	accept 0.33 for $\frac{1}{3}$ accept 0.66 or 0.67 for $\frac{2}{3}$ their fractions must be between 0 and 1	
	4/9 or 0.44 or 44.()%	A1ft	ft their fractions	

Question	Answer	Mark	Commer	nts
	Ad	ditional G	uidance	
	If probabilities on branches in (a) are all $\frac{1}{3}$			M0A0
	Decimals must have at least 2 decimal places so do not accept 0.3 or 0.6 or 0.7			
11(c) cont	Ignore any incorrect cancelling or chapercentage)	ange of for	m (fraction, decimal or	
	$\frac{1}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{1}{3}$			M0A0
	$\frac{1}{3} \times \frac{2}{3}$ and $\frac{1}{3} \times \frac{1}{3}$ without selecting $\frac{1}{3} \times \frac{2}{3}$ is choice			MO

	$\frac{1}{2}$ or 0.5	B1	oe eg $\frac{4}{8}$ or $\frac{2}{4}$
	Ade	ditional C	Guidance
	1 : 2 or 50%		B0
12(a)	$\frac{1}{2}x$	В0	
	y = 0.5x + 2		B0
	<u>0.5</u> 1		В0
	Ignore units		

Question	Answer	Mark	Comments
12(b)	 The answer to part (a) is too big The answer to part (a) stays the same The answer to part (a) is too small 	B1	
	Ad	ditional G	luidance

Question	Answer	Mark	Comments
	Alternative method 1		
13	Any correct factorisation of the numerator or the denominator	M1	eg $8(x^2 - 1)$ or $4(x + 1)$ or $2(4x^2 - 4)$ or $2(2x + 2)$ or $4(2x^2 - 2)$ or $(4x + 4)(2x - 2)$ or $(4x - 4)(2x + 2)$ or $(8x + 8)(x - 1)$ or $(8x - 8)(x + 1)$ or $-2(-4x^2 + 4)$ does not need to be seen in a fraction may be implied eg $\frac{2x^2 - 2}{x + 1}$ or $\frac{4x^2 - 4}{2x + 2}$
	Correct fraction with a common algebraic factor in the numerator and the denominator	A1	eg $\frac{8(x+1)(x-1)}{4(x+1)}$ or $\frac{2(2x+2)(2x-2)}{2(2x+2)}$ or $\frac{2(x+1)(x-1)}{(x+1)}$ or $\frac{4(x+1)(2x-2)}{4(x+1)}$ or $\frac{(4x+4)(2x-2)}{4x+4}$
	2x - 2 or $a = 2$ and $b = -2$ with M1A1 scored	A1	

Mark scheme and additional guidance continues on the next page

Question	Answer	Mark	Comme	nts	
	Alternative method 2				
	$4ax^2 + 4ax + 4bx + 4b$	M1	oe expands $(ax + b)(4x + 4)$ least 3 terms correct	to 4 terms with at	
	Any 2 of 4a = 8 $4b = -8$ $4a + 4b = 0$	A1			
13	a = 2 and $b = -2andshows that third equation issatisfiedwith M1A1 scored$	A1			
cont	Additional Guidance				
	M1 is implied by the first A1 eg $\frac{8(x+1)(x-1)}{4(x+1)}$			M1A1	
	$1(8x^2 - 8)$ or $-1(8 - 8x^2)$ etc			MO	
	2x - 2 without M1A1 scored			M0A0A0	
	M1A1 scored and $2x - 2$ followed by attempt to solve $2x - 2 = 0$			M1A1A1	
	M1A1 scored and $2x - 2$ followed by $2(x - 1)$			M1A1A1	
	M1A1 scored followed by $2(x - 1)$ but $2x - 2$ not seen			M1A1A0	

Question	Answer	Mark	Comme	nts	
	Arc radius [3.8, 4.2] cm centre <i>P</i> or arc radius [4.8, 5.2] cm centre <i>Q</i>	M1	only need arcs within tole correct region ignore other lines M1 arc radius [3.8, 4.2] c and arc radius [4.8, 5.2] cm cd and correct ft region identified	m centre <i>Q</i> entre <i>P</i>	
	Arc radius [3.8, 4.2] cm centre <i>P</i> and arc radius [4.8, 5.2] cm centre <i>Q</i> and region identified	A1	only need arcs within tole correct region ignore other lines	erance for the	
	Additional Guidance				
	Arcs may go outside the rectangle				
14	Allow any unambiguous indication of eg labelled R or appropriate shading				
	Do not accept highlighting the perimeter of the region for identification of the region				
			Q	M1A1	

Question	Answer	Mark	Comments	
	Men had more consistent scores than women	B1		
15	Ac	Iditional G	uidance	

	2400×3.8 or $\frac{m}{3.8} = 2400$ or $\frac{m}{2400} = 3.8$	M1	oe equation allow mass for <i>m</i> allow any letter apart fron	1 <i>v</i> or <i>d</i>
16(a)	9120	A1		
	Additional Guidance			

16(b)	$\pi r^2 h = 3.8$ or $\pi \times 0.5^2 \times h$ or $0.25\pi h$ or $[0.78, 0.79]h$ or $3.8 \div (\pi \times 0.5^2)$ or $3.8 \div 0.25\pi$ or $3.8 \div [0.78, 0.79]$	M1	oe eg $\pi r^2 = \frac{3.8}{h}$	
	[4.8, 4.841]	A1		
	Ad	ditional G	Guidance	
	$\pi 0.5^2 h$			M1

Question	Answer	Mark	Comments
	[2.9, 3]	B1	
17(a)		Additional G	auidance

	[1.4, 1.6]	B1			
17(b)	17(b) Additional Guidance				

17(c)	$\frac{[4.55, 4.65] - 0}{3.5 - [1.5, 1.6]} \text{ or } \frac{[4.55, 4.65]}{[1.9, 2]}$ or $\frac{[4.55, 4.65] - 0}{[1.5, 1.6] - 3.5} \text{ or } \frac{[4.55, 4.65]}{[-2, -1.9]}$ or $[-2.45, -2.275]$	M1	oe
	[2.275, 2.45]	A1	
	Ade	ditional G	auidance

	5 and 6 with no incorrect evaluation seen for 3^5 or 3^6 or 5 and 6 with no incorrect evaluation seen for $\sqrt[5]{300}$ or $\sqrt[6]{300}$	B1	5 and 6 in either order allow any evaluations truncated or B1 rounded to 2 sf or 1 sf		
	Ade				
	5 and 6 with either 3 ⁵ or 3 ⁶ evaluated	B0			
18	3 ⁵ or 3 ⁶	B0			
	243 and 729	B0			
	$3^{5} = 243$ Allow 240 or 200 (with no incorrect value seen) $3^{6} = 729$ Allow 720 or 730 or 700 (with no incorrect value seen)				
	⁵ √300 = 3.1(2) or 3.13				
	$\sqrt[6]{300} = 2.5(8)$ or 2.59 or 2.6				

Question	Answer	Mark	Comments
	Alternative method 1 Using one	half of the	isosceles triangle
	(base angle =) 35 or (top angle =) 55	B1	may be on diagram
	$\cos (\text{their 35}) = \frac{6}{x}$		oe eg $\frac{\sin 90}{x} = \frac{\sin (\text{their 55})}{6}$ any letter
	sin (their 55) = $\frac{6}{x}$	M1	their 35 must be acute their 55 must be acute
19	or 6 ² + (6 tan (their 35)) ²		
	6 cos (their 35) or		oe
	6 sin (their 55)	M1dep	
	or $\sqrt{6^2 + (6 \tan (\text{their } 35))^2}$		
	or 7.3(2) [50.6, 50.65]	A1ft	ft B0M2 with evaluation of 36 + 2 × their 7.3(2)

Mark scheme and additional guidance continues on the next page

Question	Answer	Mark	Comments	5
	Alternative method 2 Using the is	osceles	triangle	
	(base angle =) 35 or (top angle =) 110	B1	may be on diagram	
	$\frac{x}{\sin (\text{their } 35)} = \frac{12}{\sin (\text{their } 110)}$ or $12^2 = x^2 + x^2 - 2 \times x \times x \times \cos (\text{their } 110)$ or $x^2 = x^2 + 12^2 - 2 \times x \times 12 \times \cos (\text{their } 35)$	M1	oe any letter their 35 must be acute their 110 cannot be 125	
19 cont	$\frac{12}{\sin (\text{their 110})} \times \sin (\text{their 35})$ or $\sqrt{\frac{12^2}{2-2\cos (\text{their 110})}}$ or $\frac{12^2}{2 \times 12 \times \cos (\text{their 35})}$ or 7.3(2)	M1dep	00	
	[50.6, 50.65]	A1ft	ft B0M2 with evaluation of 36 + 2 × their 7.3(2)	
	Ad	ditional	Guidance	
	Allow B1 even if the angle is not subs	sequently	used	
	Alt 2 Top angle 90			M0M0A0
	Answer [50.6, 50.65] (possibly from s	cale draw	<i>r</i> ing)	B1M1M1A1

Question	Answer	Mark	Comme	nts
	$0.25\pi^2(30 - 20)^2(30 + 20)$ or $0.25\pi^2 \times 10^2 \times 50$	M1	oe allow use of π as [3.14, 3	.142]
	[12 320, 12 340.21]	A1	may be implied	
	12 300 or 1.23 × 10 ⁴ with no value outside [12 320, 12 340.21] seen	A1		
	Ade	Guidance		
20	$0.25\pi^2(30-20)^2(30+20)$ 12 300			M1 A1(implied)A1
	12 300 with no incorrect working			M1A1A1
	12 300.0 is not to 3 significant figures			
	M1 gained followed by answer 12 300	M1A0A0		
	Do not allow misreads eg $0.25\pi^2(30)$	M0A0A0		
	Brackets expanded correctly and value	ies substi	tuted	M1

Question	Answer	Mark	Commen	ts
	Alternative method 1			
	$80^2 + 60^2 - 2 \times 80 \times 60 \times \cos 75$ or $6400 + 3600 - 9600 \cos 75$ or $7515.()$	M1	oe	
	$\sqrt{\text{their 7515.()}}$ or [86.6, 86.7] or 87	M1dep		
	[86.6, 86.7] and Liz or 87 and Liz	A1	accept 86 and Liz or 90 ar with full method seen	nd Liz
	Alternative method 2			
	$80^{2} + 60^{2} - 2 \times 80 \times 60 \times \cos 75$ or 6400 + 3600 - 9600 cos 75 or 7515.()	M1	oe	
	(80 ² =) 6400 and 7515.() and Liz	A2		
21(a)	Additional Guidance			
	$80^{2} + 60^{2} - 2 \times 80 \times 60 \times \cos 75 \text{ see}$ score up to M2 eg 80 ² + 60 ² - 2 × 80 × 60 × cos 75 = 6400 + 3600 - 9600 cos 75 = 400 cos 75 = 103.5	M1		
	√103.5			M1depA0
You may need to check on your calculator whether to a after first M1 with a processing error seen		ether to award M1dep		
	eg $80^2 + 60^2 - 2 \times 80 \times 60 \times \cos 75$	= 3654 (processing error)	M1
	60.4 (square root of 3654 is implied)	M1depA0		
	Ignore any reasons given			
	Alt 2 not possible to score M1A1			
	Answer [86.6, 86.7] and Liz (possibly	y from sca	ale drawing)	M1M1A1
	[86.6, 86.7] (possibly from scale drav	ving)		M1M1

Question	Answer	Mark	Commei	nts	
	Alternative method 1 (answer Liz	in (a))			
	No change	B1	oe eg Liz will still arrive first	·· (1)	
	Alternative method 2 (answer Tia	in (a))	or Liz will be there even e	earlier (than Tia)	
	Not possible to tell		oe eg Liz might arrive before	Tia	
		B1ft	or it depends on how muc walks	ch faster Liz	
	Alternative method 3 (answer they arrive at same time in (a))				
21(b)	Liz will arrive first	B1ft	oe eg Liz wins		
	Alternative method 4 (neither Liz or Tia in (a))				
	If Liz had arrived first there would be no change		oe		
	and if Tia had arrived first it would not be possible to tell	B1ft			
	Additional Guidance				
	If correct decision is made, ignore no	on-contrad	lictory further work		
	Alt 1 Liz will arrive earlier			B1	
	Alt 1 No			B0	
	Alt 2 Yes			В0	

	$x^2 + y^2 = 25$	B1		
22	Additional Guidance			

Question	Answer	Mark	Commer	its
	$\sqrt[3]{64}$ and $\sqrt[3]{343}$ or 4 and 7 or $\sqrt[3]{[5.3, 5.4]}$ or [1.74, 1.754411] or $\sqrt[3]{[0.18, 0.19]}$ or [0.56, 0.575]	M1	oe eg 4:7 or 7:4 or $\sqrt[3]{\frac{343}{64}}$ or $\frac{7}{4}$ or $\sqrt[3]{\frac{64}{343}}$ or $\frac{4}{7}$	
	their 4 ² and their 7 ² or 16 and 49 or their [1.74, 1.754411] ² or [3.02, 3.08] or their [0.56, 0.575] ² or [0.31, 0.331]	M1dep	oe eg 16: 49 or 49: 16 or $\left(\text{their } \frac{7}{4} \right)^2$ or $\frac{49}{16}$ or $\left(\text{their } \frac{4}{7} \right)^2$ or $\frac{16}{49}$	
23	539	A1		
	Ad	àuidance	N/1	
	$64^{\frac{2}{3}}$ and $343^{\frac{2}{3}}$			M1 M1M1
	$\left(\frac{343}{64}\right)^{\frac{2}{3}}$ or $\left(\frac{64}{343}\right)^{\frac{2}{3}}$			M1M1
	Answer 539 with evidence of roundin eg1 $176 \times 3.06 = 538.56$ Answer 5 eg2 $176 \times 3.06 = 539$ (may have ke	39		M1M1A0 M1M1A1
	$\left(\sqrt{176} \times \frac{7}{4}\right)^2$			M1M1
	$176 \div 16 = 11$ and 11×49			M1M1
	4 and 7 (and/or 4 ² and 7 ²) but uses c and 7	lifferent m	ethod not involving 4	M1M0A0

Question	Answer	Mark	Comments
	Alternative method 1		
	Any product of three valid dimensions that would give a volume < 34 000 or any product of three valid dimensions that would give a volume > 34 000	M1	eg 49.5 × 34.5 × 19.5 or 50.5 × 35.5 × 20.5 or 50 × 35 × 20 ignore any evaluations of products
24	Any product of three valid dimensions that would give a volume < 34 000 and any product of three valid dimensions that would give a volume > 34 000	M1dep	eg 49.5 × 34.5 × 19.5 and 50.5 × 35.5 × 20.5 ignore any evaluations of products
	34 × 1000 or 34 000	M1	converts to cm ³
	their volume < 34 000 and their volume > 34 000 and 34 000 and ticks Cannot tell	A1	both volumes in cm ³ must see working for M3 answers for their volumes must be seen and be correct or rounded or truncated to at least 2 sf (unless 34 000 to 2 sf when must be to at least 3 sf)

Question	Answer	Mark	Comments
	Alternative method 2		
	Any product of three valid dimensions that would give a volume < 34 000 or any product of three valid dimensions that would give a volume > 34 000	M1	eg 49.5 × 34.5 × 19.5 or 50.5 × 35.5 × 20.5 or 50 × 35 × 20 ignore any evaluations of products
24 cont	Any product of three valid dimensions that would give a volume < 34 000 and any product of three valid dimensions that would give a volume > 34 000	M1dep	eg 49.5 × 34.5 × 19.5 and 50.5 × 35.5 × 20.5 ignore any evaluations of products
	one of their volumes ÷ 1000	M1dep	dep on first M1 converts to litres
	their volume < 34 and their volume > 34 and ticks Cannot tell	A1	both volumes in litres must see working for M3 answers for their volumes must be seen and be correct or rounded or truncated to at least 2 sf (unless 34 000 to 2 sf when must be to at least 3 sf)

Question	Answer	Mark	Commer	nts		
	Additional Guidance					
	There are an infinite number of sets of three valid dimensions Valid dimensions for 50 are [49.5, 50.5] for 35 are [34.5, 35.5] for 20 are [19.5, 20.5]					
	49.5 × 34.5 × 19.5 = 33 301.() or 33 49.6 × 34.6 × 19.6 = [33 636, 33 637] or 33 640 49.7 × 34.7 × 19.7 = 33 974.() or 33 49.8 × 34.8 × 19.8 = 34 314.() or 34	or 33 000 000 or 33	or 33 600 or 33 630 8 900 or 33 970			
24 cont	49.9 × 34.9 × 19.9 = 34 656.() or 34 600 or 34 700 or 34 650 or 34 660 50 × 35 × 20 = 35 000 50.1 × 35.1 × 20.1 = 35 346.() or 35 000 or 35 300 or 35 340 or 35 350					
	Three valid dimensions do not have to eg 49.6 × 35 × 20.4 (= 35 414.() or	•		M1		
	49.5 34.5 19.5 and 33 301 (answer im	plies mult	iplication signs)	M1		
	49.5 34.5 19.5 (no answer so multipli	cation sigr	ns not implied)	M0		
	33 301 but 49.5 34.5 19.5 not seen			M0		
	Units do not have to be seen					

Question	Answer	Mark	Commer	nts
	$\frac{x}{x+35} = \frac{5}{12}$ or $\frac{35}{x+35} = \frac{7}{12}$ or $\frac{x}{35} = \frac{5}{7}$ or x: 35 = 5:7 or links $\frac{7}{12}$ to 35	M1	oe eg $x + 35 = 60$ or links $\frac{1}{12}$ to 5	
25	12x - 5x = 175 or $7x = 175$ or $420 - 245 = 7x$ or $(x =) 25$ or $\frac{25}{60}$	M1dep	oe collects terms 25 may be seen in section Venn diagram	n labelled <i>x</i> on
	(y =) 150 – 47 – 35 – their 25 or 43	M1dep	dep on M2 43 may be seen in section Venn diagram	n labelled y on
	$\frac{43}{150}$ or 0.286 or 0.287 or 0.29 or 28.6% or 28.7% or 29%	A1		
	Ad	ditional G	Guidance	
	Accept $\frac{7}{12} = 35$			M1
	Ignore any incorrect cancelling or char percentage)	nge of forr	m (fraction, decimal or	

Question	Answer	Mark	Comments
	Alternative method 1		
	$4x^2 + 5x + 3 = x + 2$	M1	
	$4x^2 + 5x - x + 3 - 2 (= 0)$		oe collection of terms
	or $4x^2 + 4x + 1 (= 0)$	M1dep	eg $4x^2 + 5x - x = 2 - 3$
			or $4x^2 + 4x = -1$
	(2x + 1)(2x + 1) (= 0)		0e
	or $4\left(x+\frac{1}{2}\right)^2 (=0)$		$\operatorname{eg}\left(x+\frac{1}{2}\right)^{2}(=0)$
	or $\frac{-4\pm\sqrt{4^2-4\times4\times1}}{2\times4}$	A1	
	or $b^2 - 4ac = 4^2 - 4 \times 4 \times 1$		allow $b^2 - 4ac = 16 - 16$
26	or D(iscriminant) = $4^2 - 4 \times 4 \times 1$		or D(iscriminant) = 16 – 16
	$(x =) -\frac{1}{2}$ with no other solutions with M2A1 seen or		oe
	states that as brackets are the same there is only one solution with M2A1 seen		
	or $b^2 - 4ac = 4^2 - 4 \times 4 \times 1 = 0$ and states there is only one solution with M2A1 seen	A1	allow $b^2 - 4ac = 16 - 16 = 0$ and states there is only one solution with M2A1seen
	or		
	D(iscriminant) = $4^2 - 4 \times 4 \times 1 = 0$ and states there is only one solution with M2A1 seen		allow $D(iscriminant) = 16 - 16 = 0$ and states there is only one solution with M2A1seen

Question	Answer	Mark	Comments	
	Alternative method 2			
	$y = 4(y-2)^2 + 5(y-2) + 3$	M1	ое	
	$4y^2 - 16y + 16 + 5y - 10 + 3 - y$ (= 0) or $4y^2 - 12y + 9$ (= 0)	M1dep	oe expansion and collection of terms eg $4y^2 - 16y + 5y - y = 10 - 16 - 3$ or $4y^2 - 12y = -9$	
	(2y-3)(2y-3) (= 0) or $4\left(y-\frac{3}{2}\right)^2 (= 0)$		oe eg $\left(y-\frac{3}{2}\right)^2$ (= 0)	
	or $\frac{12 \pm \sqrt{(-12)^2 - 4 \times 4 \times 9}}{2 \times 4}$ or $b^2 - 4ac = (-12)^2 - 4 \times 4 \times 9$	A1	allow $b^2 - 4ac = 144 - 144$	
	or		or	
26 cont	$D(\text{iscriminant}) = (-12)^2 - 4 \times 4 \times 9$		allow D(iscriminant) = 144 – 144	
	$(y =) \frac{3}{2}$ with no other solutions with M2A1 seen or states that as brackets are the same there is only one solution with		0e	
	M2A1 seen or $b^2 - 4ac = (-12)^2 - 4 \times 4 \times 9 = 0$ and states there is only one solution with M2A1 seen	A1	allow $b^2 - 4ac = 144 - 144 = 0$ and states there is only one solution with M2A1seen	
	or			
	D(iscriminant) = $(-12)^2 - 4 \times 4 \times 9$ = 0 and states there is only one solution with M2A1 seen		allow D(iscriminant) = 144 – 144 = 0 and states there is only one solution with M2A1seen	

Question	Answer	Mark	Commer	nts	
	Additional Guidance				
	Alt 1 $(x =) -\frac{1}{2}$ with no working or A	Alt 2 $(y =)$	$\frac{3}{2}$ with no working	M0M0A0A0	
	Alt 1 Ignore any <i>y</i> -coordinate whether correct $\left(=\frac{3}{2}\right)$ or incorrect				
	Alt 2 Ignore any <i>x</i> -coordinate whethe	r correct ($=-\frac{1}{2}$ or incorrect		
	T & I leading to $x = -\frac{1}{2}$			M0M0A0A0	
26 cont	To award M1dep you must see a correct expression with terms collected or a correct equation with terms collected				
	$4x^2 + 5x + 3 = x + 2$			M1	
	$4x^2 + 1 = -4x$ (all x terms not collected on one side)			M0dep	
	$4x^2 + 5x + 3 = x + 2$	M1			
	$4x^2 + 4x + 3 = 2$ (all constant terms no	M0dep			
	If using the discriminant to award A marks, you must see either $b^2 - 4ac$ or D(iscriminant)				
	$b^2 - 4ac = 4^2 - 4 \times 4 \times 1$ can be implied				
	eg $b + \sqrt{b^2 - 4ac}$ and $4 + \sqrt{4^2 - 4 \times 4 \times 1}$ scores first A1				
	For final A1 must see $b^2 - 4ac = 4^2 - 4 \times 4 \times 1 = 0$ and				
	statement that there is only one solution with M2A1 seen				

Question	Answer	Mark	Comments	
	Alternative method 1 Working with 2.75			
27	10 <i>x</i> = 27.5 or 100 <i>x</i> = 275.5	M1	oe multiplication by a power of 10 eg $1000x = 2755.5$ any letter	
	10x - x = 27.5 2.75 or $9x = 24.8$ with $10x = 27.5$ seen or 100x - 10x = 275.5 27.5 or $90x = 248$ with $100x = 275.5$ and $10x = 27.5$ seen or 100x - x = 275.5 2.75 or $99x = 272.8$ with 100x = 275.5 seen	M1dep	oe subtraction to eliminate recurring digits eg $1000x - 10x = 2755.5 27.5$ or $990x = 2728$ with $1000x = 2755.5$ and $10x = 27.5$ seen numbers must all be correct	
	x = 2.75 stated and M2 scored and 9x = 24.8 and $x = \frac{24.8}{9} = \frac{124}{45}$ or x = 2.75 stated and M2 scored and 90x = 248 and $x = \frac{248}{90} = \frac{124}{45}$ or x = 2.75 stated and M2 scored and 99x = 272.8 and $x = \frac{272.8}{99} = \frac{124}{45}$	A1	oe eg x = 2.75 stated and M2 scored and 990x = 2728 and $x = \frac{2728}{990} = \frac{124}{45}$	

Question	Answer	Mark	Comments				
	Alternative method 2 Working with 0.75						
	10 <i>x</i> = 7.5 or 100 <i>x</i> = 75.5	M1	oe multiplication by a power of 10 eg 1000 <i>x</i> = 755.5 any letter				
	10x - x = 7.5 0.75 or $9x = 6.8$ with $10x = 7.5$ seen or 100x - 10x = 75.5 7.5 or $90x = 68$ with $100x = 75.5$ and $10x = 7.5$ seen or 100x - x = 75.5 0.75 or $99x = 74.8$ with $100x = 75.5$ seen	M1dep	oe subtraction to eliminate recurring digits eg $1000x - 10x = 755.5 7.5$ or $990x = 748$ with $1000x = 755.5$ and $10x = 7.5$ seen numbers must all be correct				
27 cont	x = 0.75 stated and M2 scored and $9x = 6.8$ and $x = \frac{6.8}{9}$ and $2\frac{6.8}{9} = \frac{124}{45}$ or x = 0.75 stated and M2 scored and $90x = 68$ and $x = \frac{68}{90}$ and $2\frac{68}{90} = \frac{124}{45}$ or x = 0.75 stated and M2 scored and $99x = 74.8$ and $x = \frac{74.8}{99}$ and $2\frac{74.8}{99} = \frac{124}{45}$	A1	oe eg x = 0.75 stated and M2 scored and 990x = 748 and $x = \frac{748}{990}$ and $2\frac{748}{990} = \frac{124}{45}$				

Question	Answer	Mark	Comments		
	Alternative method 3 Working with 0.05				
27 cont	10 <i>x</i> = 0.5 or 100 <i>x</i> = 5.5	M1	oe multiplication by a power of 10 eg $1000x = 55.55$ any letter		
	10x - x = 0.5 0.05 or $9x = 0.5$ with $10x = 0.5$ seen or 100x - 10x = 5.5 0.5 or $90x = 5$ with $100x = 5.5$ and $10x = 0.5$ seen or 100x - x = 5.5 0.05 or $99x = 5.5$ with 100x = 5.5 seen	M1dep	oe subtraction to eliminate recurring digits eg $1000x - 10x = 55.5 0.5$ or $990x = 55$ with $1000x = 55.5$ and $10x = 0.5$ seen numbers must all be correct		
	x = 0.05 stated and M2 scored and $9x = 0.5$ and $x = \frac{0.5}{9}$ and $2.7 + \frac{0.5}{9} = \frac{124}{45}$ or x = 0.05 stated and M2 scored and $90x = 5$ and $x = \frac{5}{90}$ and $2.7 + \frac{5}{90} = \frac{124}{45}$ or x = 0.05 stated and M2 scored and $99x = 5.5$ and $x = \frac{5.5}{99}$ and $2.7 + \frac{5.5}{99} = \frac{124}{45}$	A1	oe eg $x = 0.05$ stated and M2 scored and 990 $x = 55$ and $x = \frac{55}{990}$ and 2.7 + $\frac{55}{990} = \frac{124}{45}$		

Question	Answer	Mark	Comments		
	Additional Guidance				
	124 ÷ 45 = 2.75	M0M0A0			
	Alt 1 M1dep oe subtraction to eliminate recurring decimals includes 100x - 10x = 248 with $100x = 275.5$ and $10x = 27.5$ seen or $90x = 275.5 27.5$ with $100x = 275.5$ and $10x = 27.5$ seen (apply same principle in Alts 2 and 3)				
27 cont	Alt 2 equivalents for final part of A1 eg For $2\frac{68}{90} = \frac{124}{45}$ allow 2 + $\frac{68}{90} = \frac{124}{45}$				
	Alt 3 equivalents for final part of A1 eg For 2.7 + $\frac{5}{90} = \frac{124}{45}$ allow 2 + $\frac{7}{10} + \frac{5}{90} = \frac{124}{45}$				

28(a)	5 - 2x	B1	may be implied	
	3(x-1) + 7 or $3x + 4$	M1	oe ignore incorrect expansion if $3(x - 1) + 7$ seen	
	9 + <i>x</i>	A1		
	Additional Guidance			
	Working out 2f(x)			B0
	Working out $g(x + 1)$			M0

Question	Answer	Mark	Commer	nts	
	Alternative method 1				
	x - 7 = 3y or $y - 7 = 3x$	M1	allow $x - 7 = 3g$ or $g - 7$	7 = 3x	
	$\frac{x-7}{3} \text{ or } \frac{y-7}{3}$	A1	oe allow $\frac{g-7}{3}$		
	$-1.4 \text{ or } -\frac{7}{5}$	A1	oe		
	Alternative method 2				
28(b)	3(2x) + 7	M1	oe		
	x = 3(2x) + 7 or $x = 6x + 7$	A1	oe equation		
	-1.4 or $-\frac{7}{5}$	A1	ое		
	Additional Guidance				
	Beware -3x - 7 = 2x leading to -1.4			M0A0A0	