## GCE

## Mathematics A

## H240/02: Pure Mathematics and Statistics

Advanced GCE

Mark Scheme for Autumn 2021

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

## Text Instructions

## 1. Annotations and abbreviations

| Annotation in RM assessor | Meaning |
| :--- | :--- |
| $\checkmark$ and $\boldsymbol{x}$ |  |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| $\wedge$ | Omission sign |
| MR | Blank Page |
| BP |  |
| Seen |  |
| Highlighting | Meaning |
|  | Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark |
| Other <br> mark scheme | Correct answer only |
| dep* | Or equivalent |
| cao | Rounded or truncated |
| oe | Seen or implied |
| rot | Without wrong working |
| soi | Answer given |
| www | Anything which rounds to |
| AG | By Calculator |
| awrt | This question included the instruction: In this question you must show detailed reasoning. |
| BC |  |
| DR |  |

## 2. Subject-specific Marking Instructions for $\mathbf{A}$ Level Mathematics $A$

Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ${ }^{\wedge}$ ) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.
Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).
If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.
b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader

The following types of marks are available.
M
A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an $M$ mark may be specified.
A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.
Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold "In this question you must show detailed reasoning", or the command words "Show" or "Determine". Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

If in any case the scheme operates with considerable unfairness consult your Team Leader.


| Question |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 4 | (a) | 6000 | $\begin{aligned} & \hline \text { B1 } \\ & {[1]} \\ & \hline \end{aligned}$ |  |
| 4 | (b) | 2000 | $\begin{aligned} & \text { B1f } \\ & {[1]} \end{aligned}$ | $\mathrm{ft} \mathrm{their} \mathrm{(a)} \mathrm{-} 4000$ |
| 4 | (c) | Oscillates or Goes up and down. oe Fluctuates. Moves in a cycle | B1 <br> [1] | Ignore all else <br> NOT "Increases for $1^{\text {st }} 6$ months then decreases" |
| 4 | (d) | $\begin{aligned} & 30 t=360 \\ & \text { Time to return to initial size }=12 \text { months } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & {[2]} \end{aligned}$ | May be implied by answer Allow $t=12$, or $t=12$ months, or just 12 |
| 4 | (e) | $\begin{aligned} & 4500=5000-1000 \cos (30 t)^{-0} \\ & \cos (30 t)^{\circ}=0.5 \\ & 30 t=60 \text { or } 300(\text { both }) \end{aligned}$ <br> 2nd time $P=4500$ is when $t=10$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \end{gathered}$ | Substitute $P=4500$ May be implied by next line <br> Correct rearrangement <br> Attempt $30 t=\cos ^{-1}($ their 0.5$)$, giving $\alpha$ and $360-\alpha$. <br> Condone $30 \mathrm{t}=\frac{\pi}{3}, \frac{5 \pi}{3}$ <br> or after 10 months. Allow $t=10$ months, or just 10 SC. (If not gained $1^{\text {st }} \mathrm{M} 1 \mathrm{~A} 1$ )Correct answer with no or inadequate working and/or T\&I: $t=10$ stated: B2; $t=10$ embedded: B1B0 |
|  |  | Alternative methods for 2nd M1A1 $30 t=60$ or -60 (both) $\quad(\mathrm{t}=2$ or -2 ) 2 nd time $P=4500$ is when $t=-2+12=10$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | $30 t=60(t=2)$ <br> (end of $1^{\text {st }}$ cycle at $t=12$ ) $2^{\text {nd }}$ time $P=4500$ is when $t=12-2=10$ |
|  |  | $\begin{aligned} & 30 t=60 \quad(t=2) \\ & 6-2=4 ; t=6+4=10 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ |  |
|  |  |  | [4] |  |
| 4 | (f) | $\begin{aligned} \mathrm{eg} P & =5000-1000 \mathrm{e}^{-t} \cos (30 t)^{\mathrm{o}} \\ P & =5000-1000 \mathrm{e}^{-k t} \cos (30 t)^{\circ}(k>0) \end{aligned}$ <br> Answers in words must be equivalent to one of these | B1 | or other good answers $\begin{aligned} \operatorname{eg} P & =5000-\left(1000 \cos (30 t)^{\circ}\right)^{1 / t} \\ \quad P & =5000-\frac{1000}{t} \cos (30 t)^{\circ} .(t>0) \end{aligned}$ |


| Question |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 5 | (a) | Midpoint $A B$ is $(3.5,5.5)$; Gradient $A B=-\frac{1}{7}$ <br> Gradient of perpendicular bisector $-1 /\left(-\frac{1}{7}\right)$ $y-5.5=7(x-3.5) \quad$ oe $\quad$ ISW | B1 <br> M1 <br> A1 | Both. Allow midpoint $=\left(\frac{0+7}{2}, \frac{6+5}{2}\right)$ ISW $(=7)$ <br> cao. Correct answer, no working or inadequate working: SC B2 |
|  |  | Midpt $A B$ is $(3.5,5.5)$; Gradient $A B=-\frac{1}{7}$ $\begin{aligned} & (y=7 x+c) \quad 5.5=7 \times 3.5+c \\ & y=7 x-19 \end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { M1 } \\ \text { A1 } \end{gathered}$ | Both <br> ft their midpt and gradient, NOT $-\frac{1}{7}$ cao. Any correct form |
|  |  | $\begin{aligned} & x^{2}+(y-6)^{2}=(x-7)^{2}+(y-5)^{2} \\ & -12 y+36=-14 x-10 y+49+25 \text { ISW } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | Attempt expansion cao. Any correct form eg $y=7 x-19$ |
|  |  |  | [3] |  |
| 5 | (b) | Perpendicular bisector of $B C$ is $x+7 y-17=0$ OR of $C A$ is $4 y=3 x-1$ <br> Example method, perp bisectors of $A B \& B C$ : $x+7(7 x-19)-17=0 \quad(\Rightarrow x=3)$ | B1 <br> M1 | Any correct form for another perp bisector <br> Attempt solve simultaneously equations of two perpendicular bisectors. Can be implied |
|  |  | Alternative method for $1^{\text {st }}$ two marks $\mathrm{Grad} B C$ is 7 so $B C \& A B$ perpendicular Hence $A C$ is a diameter | M1 <br> B1 |  |
|  |  | Centre is $(3,2)$ eg Radius ${ }^{2}=3^{2}+(6-2)^{2}=25$ <br> Equn of circle is $(x-3)^{2}+(y-2)^{2}=25$ or $x^{2}-6 x+y^{2}-4 y=12 \quad$ oe | B1 <br> M1 <br> A1ft <br> [5] | cao. $\quad \mathrm{NB}$, if centre $=(3,2)$ without clear working, B0M0B1 Correct method for $r^{2}$ or $r$ using their centre $\& A$ or $B$ or $C$ <br> ISW. ft their centre \& radius, dep both M1 marks |

\begin{tabular}{|c|c|c|c|c|}
\hline \multicolumn{2}{|r|}{Question} \& Answer \& Mark \& Guidance \\
\hline 6 \& (a) \& \[
\begin{aligned}
\& 0.1\left(1+1.1^{2}+1.2^{2}+1.3^{2}+1.4^{2}\right) \\
\& 0.1\left(1.1^{2}+1.2^{2}+1.3^{2}+1.4^{2}+1.5^{2}\right)
\end{aligned}
\] \& \[
\begin{aligned}
\& \text { B1 } \\
\& {[1]}
\end{aligned}
\] \& NB. Check working Both seen oe \\
\hline 6 \& (b) \& \begin{tabular}{l}
0.79 \\
About half way between the last two bounds or \((0.784+0.799) \div 2=0.79\) Ignore all else
\end{tabular} \& \begin{tabular}{l}
B1 \\
B1 \\
[2]
\end{tabular} \& \begin{tabular}{l}
Not 0.7915 condone "The mean of the last two bounds" or other sensible Allow UB and LB are converging towards 0.79 oe \\
The two B1 marks are independent
\end{tabular} \\
\hline 6 \& (c) \& \[
\lim _{\delta x \rightarrow 0} \sum_{x=1}^{1.5} y \delta x
\] \& \[
\begin{aligned}
\& \text { B1 } \\
\& \text { B1 }
\end{aligned}
\] \& \begin{tabular}{l}
for \(\lim _{\delta x \rightarrow 0} \sum y \delta x . \quad\) Allow \(x^{2}\) instead of \(y\) \\
for limits, dep using \(\Sigma\) not integral. \(\lim _{\delta x \rightarrow 0} \sum_{1}^{1.5} y \delta x\) B1B0
\end{tabular} \\
\hline 7 \& \& \[
\begin{aligned}
\& \cos (x+\delta x)-\cos x \\
\& =\cos x \cos \delta x-\sin x \sin \delta x-\cos x \\
\& \lim _{\delta x \rightarrow 0} \frac{\cos x \cos \delta x-\sin x \sin \delta x-\cos x}{\delta x} \\
\& \text { as } \delta x \rightarrow 0: \cos \delta x \rightarrow 1 \\
\& \quad \text { and } \frac{\sin \delta x}{\delta x} \rightarrow 1 \\
\& \begin{array}{l}
\left(\lim _{\delta x \rightarrow 0} \frac{\cos x-\sin x \delta x-\cos x}{\delta x}\right) \\
=-\sin x
\end{array} \quad \text { or } 1-\frac{(\delta x)^{2}}{2} \\
\&
\end{aligned}
\] \& B1
M1

M1

A1 \& | Allow $h$ or other letter for $\delta x$ throughout |
| :--- |
| or $\lim _{\delta x \rightarrow 0} \frac{\cos (x+\delta x)-\cos x}{\delta x}$ or may be seen later. Must include $\lim _{\delta x \rightarrow 0}$ |
| Allow $\cos \delta x=1$ for small $\delta x \quad$ (or $1-\frac{(\delta x)^{2}}{2}$ ) |
| Allow $\sin \delta x=\delta x$ for small $\delta x$ |
| Both must be explicitly stated for M1 |
| If not stated but implied, M0, but can still possibly gain final A1 |
| Dep on at least B1M1 gained, and approximations either seen explicitly or seen substituted. |
| and nothing incorrect seen |
| NB. $\cos x-\sin x-\cos x=-\sin x$ is incorrect and scores A0 | <br>

\hline
\end{tabular}




| Question |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | [4] |  |
| 9 | (b) | $\overrightarrow{O F}=\mathbf{a}+\mathbf{b}+\mathbf{c}$ <br> Hence $X$ lies on $O F$, so $A M$ and $O F$ intersect | $\begin{gathered} \text { B1* } \\ \text { B1dep } \\ {[2]} \end{gathered}$ | Both statements needed. NB dep on B1 |
| 10 | (a) | Very likely weight will increase with time oe or He is only looking for positive correlation | B1 $[1]$ | Or eg "Expect weight to increase with time" oe <br> "Foetuses grow" oe Ignore all else |
| 10 | (b) | $\mathrm{H}_{0}: \rho=0 \quad$ Allow other letters $\mathrm{H}_{1}: \rho>0$ where $\rho$ is the correlation coefficient for the population or where $\rho$ is the correlation coefficient between time and weight <br> Comp 0.722 with 0.6851 <br> Reject $\mathrm{H}_{0}$. Condone Accept $\mathrm{H}_{1}$ <br> There is evidence of (positive linear) correlation between time from conception to birth and weight of new-born babies <br> Or eg It appears that birth weight increases with time (from conception to birth) | B1 <br> B1 <br> M1 <br> M1 <br> A1 <br> [5] | B1B0 for 1 error, eg undefined $\rho$ or 2-tail <br> For hypotheses in words, not using parameter: <br> $\mathrm{H}_{0}$ : There is no correlation between time and weight <br> $\mathrm{H}_{1}$ : There is positive correlation between time and weight B1B0 But omission of "positive": B0B0 <br> May be implied by conclusion <br> Allow without "positive" and without "linear" <br> In context, not definite |
| 11 | (a) | Population large oe | B1 | or, eg Would take too long to contact all students. |


| Question |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | [1] | NOT "Easier" |
| 11 | (b) | eg: Includes students from all years (or ages) Numbers in years in correct proportions Different years might like different music | B1 | or: Different years may have different numbers of students <br> NOT "It's more representative" or "Takes all students into account" <br> "You get a range of people" "It avoids bias" |
| 11 | (c) | $\begin{aligned} & 21+2 \times 4.2=29.4 \\ & 22.9+1.5(22.9-18.0)=30.25 \end{aligned}$ <br> Unclear whether 30 is an outlier | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \hline[3] \end{aligned}$ | Allow " 30 is more than 2 sds away from the mean" Allow " 30 is less than $1.5 \times \mathrm{IQR}$ from UQ" or eg "It depends which definition you use." <br> Any comment implying uncertainty <br> Ignore comments about mean $\pm 3$ sds or mean $\pm 1 \mathrm{sd}$ |
| 11 | (d) | $\mathrm{H}_{0}: \mu=20$ <br> $\mathrm{H}_{1}: \mu>20$ where $\mu=$ pop mean time spent oe $\bar{X} \sim \mathrm{~N}\left(20, \frac{4.2^{2}}{60}\right) \text { and } \bar{X}=21$ $\mathrm{P}(\bar{X}>21)=0.0326$ <br> Compare 0.05 | B1 <br> B1 <br> M1 <br> A1 <br> A1 | NB Allow 2 sf throughout <br> Allow other letters, not $X$ unless defined. Not $\bar{X}$ <br> B1B0 for 1 error eg 2-tail or: <br> Correct distribution and value of $\bar{X}$. <br> stated or implied eg by 0.0326 or 0.967 or 20.9 or 1.84 or 0.000335 <br> even if within incorrect statement eg $\mathrm{P}(X=21)=0.0326$ <br> Condone $\frac{4.2^{2}}{\sqrt{60}}$ or $\frac{4.2^{2}}{60^{2}}$ or $\frac{4.2}{60}$ <br> BC Allow 2 sf, ie 0.033 <br> Dep 0.0326 or 1.84 or 0.9674 or $\mathrm{P}(X>21)$ or $\mathrm{P}(X \geq 21)$ soi <br> Must compare like with like, |


| Question |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | eg NOT prob cf $z$-value or large prob cf small prob or CV cf wrong end of acceptance region |
| 11 | (d) <br> ctd | $\begin{aligned} & \text { Alternative methods for M1A1A1 } \\ & \text { or } \frac{a-20}{4.2 \div \sqrt{60}}=1.645 \quad(a=20.9) \\ & \mathrm{CV}=20.9 \\ & 21>20.9 \quad \text { or } 21 \text { not in acceptance region } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | Condone $\frac{4.2^{2}}{\sqrt{60}}$ or $\frac{4.2^{2}}{60^{2}}$ or $\frac{4.2}{60}$ |
|  |  | $\begin{aligned} & \text { or } \frac{21-20}{4.2 \div \sqrt{60}} \\ & z_{\text {calc }}=1.84 \\ & \text { Compare } 1.645 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | Condone $\frac{4.2^{2}}{\sqrt{60}}$ or $\frac{4.2^{2}}{60^{2}}$ or $\frac{4.2}{60}$ |
|  |  | $\bar{X} \sim \mathrm{~N}\left(20, \frac{4.2^{2}}{60}\right)$ and $\bar{X}=\frac{1260}{60}$ or 21 $\mathrm{P}(\bar{X}<21)=0.9674$ <br> Compare 0.95 | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | Condone $\frac{4.2^{2}}{\sqrt{60}}$ or $\frac{4.2^{2}}{60^{2}}$ or $\frac{4.2}{60}$ BC |
|  |  | Reject $\mathrm{H}_{0} \quad$ Condon Accept $\mathrm{H}_{1}$ | M1 | Dependent on clearly valid comparison of like with like. <br> Dep 0.0485 or 0.951 or 20.9 or 1.84 or $\mathrm{P}(X>21)$ or $\mathrm{P}(X \geq 21)$ soi May be implied by conclusion, eg "There is evidence that mean time is $>20$ hours" M1A1 |
|  |  | There is evidence that (mean) time spent is $>20$ hours or eg there is evidence to support Zac's belief | A1f | In context, not definite; <br> eg "Mean time is $>20$ hours": A0 <br> But "There is evidence to reject $\mathrm{H}_{0}$ and that mean time is $>20 \mathrm{~h}$ " |




| Question |  |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | (c) | (ii) <br> ctd | say they were using private transport. | B1 | independent Ignore all else |
|  |  |  | People will still have to travel by car, so the results won't be very different | B2 |  |
|  |  |  | Alternatives, assuming (incorrectly) users of P\&R will report both methods or just public: |  |  |
|  |  |  | Public transport increase or private decrease | $\begin{aligned} & \text { B1 } \\ & \text { B0 } \end{aligned}$ | "Agree" may be implied Ignore all else |
|  |  |  | P\&R will result in more people using private transport, so this will show an increase | $\begin{aligned} & \text { B1 } \\ & \text { B0 } \end{aligned}$ | Not just "Increase in private" without justification |
|  |  |  | Users of P\&R will use both public and private, so not clear | $\begin{aligned} & \text { B1 } \\ & \text { B0 } \end{aligned}$ |  |
|  |  |  | No, because other changes might have been made that affect the proportions. | B2 |  |
|  |  |  | If P\&R users report both, or just public, then yes, public will show increase | B2 |  |
|  |  |  | Recognition of issue as to whether P\&R users should report private or public Hence unclear whether change will show | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | Other sensible answers may be seen not covered in this MS |
|  |  |  |  | [2] |  |
| 14 | (a) |  | $\begin{aligned} & k\left(1+\frac{1}{2}+\frac{1}{3}+\frac{1}{4}\right)=1 \\ & k \times \frac{25}{12}=1 \quad \text { or eg } \frac{25}{3} k=4 \quad \text { or } 25 k=12 . \\ & \text { hence } k=\frac{12}{25} \quad \text { AG } \end{aligned}$ | M1 <br> A1 | Correct equation involving multiple of $k$ <br> Must see previous line and answer |


| Question |  | Answer | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: |
|  |  | or verification: $\frac{12}{25}+\frac{6}{25}+\frac{4}{25}+\frac{3}{25}=1$ | $\begin{aligned} & \hline \text { M1 } \\ & \text { A1 } \\ & \hline[2] \end{aligned}$ |  |
| 14 | (b) | $\begin{array}{cccc} 1 & 2 & 3 & 4 \\ \frac{12}{25} & \frac{6}{25} & \frac{4}{25} & \frac{3}{25} \end{array}$ | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | or equivalent exact values |
| 14 | (c) | $\begin{aligned} & (3,1,1)(4,1,1)(4,2,1)(4,1,2) \\ & \begin{aligned} & \frac{4}{25} \times\left(\frac{12}{25}\right)^{2}+\frac{3}{25} \times\left(\frac{12}{25}\right)^{2}+\frac{3}{25} \times \frac{6}{25} \times \frac{12}{25} \\ &+\frac{3}{25} \times \frac{12}{25} \times \frac{6}{25} \text { oe } \end{aligned} \\ & =\frac{288}{3125} \text { or } 0.09216 \end{aligned}$ | M1 <br> M1 <br> A1 <br> [3] | At least three of these seen or implied. No extras or repeats. <br> At least two correct terms, no incorrect coefficients; ft their table. Allow in terms of $k$ <br> Allow 0.0922 ( 3 sf ) |
| 14 | (d) | $(1,1,1,1,3)$ <br> (1, 1, 1, 2, 2) <br> $\left(\frac{12}{25}\right)^{4} \times \frac{4}{25} \times 5+\left(\frac{12}{25}\right)^{3} \times\left(\frac{6}{25}\right)^{2} \times{ }^{5} \mathrm{C}_{2} \quad$ oe | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | B1B1 for both sets in any order, without extras. Both soi. B1 for both sets in any order, with extras. <br> $\left(\frac{12}{25}\right)^{4} \times \frac{4}{25}$ or $\left(\frac{12}{25}\right)^{3} \times\left(\frac{6}{25}\right)^{2}$ oe seen. Ignore coeffs. ft their table <br> For either $\left(\frac{12}{25}\right)^{4} \times \frac{4}{25} \times 5$ or $\left(\frac{12}{25}\right)^{3} \times\left(\frac{6}{25}\right)^{2} \times{ }^{5} \mathrm{C}_{2}$ oe ft their table |
|  |  | Alternative method for M1A1 or $\left(\frac{12}{25}\right)^{4} \times \frac{4}{25} \times(4+1)+\left(\frac{12}{25}\right)^{3} \times\left(\frac{6}{25}\right)^{2} \times\left({ }^{4} \mathrm{C}_{2}+4\right)$ | M1 A1 | oe <br> For either $\left(\frac{12}{25}\right)^{4} \times \frac{4}{25} \times(4+1)$ or $\left(\frac{12}{25}\right)^{3} \times\left(\frac{6}{25}\right)^{2} \times\left({ }^{4} \mathrm{C}_{2}+4\right)$ oe |
|  |  | $=\frac{41472}{390625} \text { or } 0.10616832$ | $\begin{array}{r} \text { A1 } \\ {[5]} \\ \hline \end{array}$ | Allow 0.106 (3 sf) |

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