

Centre number				Candidate numbe	er .	
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Forename(s)						

AS **MATHEMATICS**

Paper 2

Wednesday 20 May 2020

Morning

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- · Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer each question in the space provided for that question.
 If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

Question	Mark
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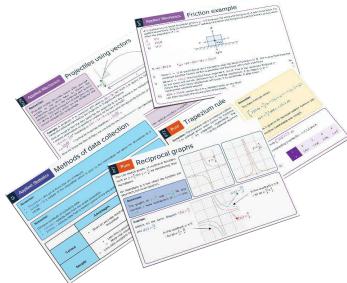


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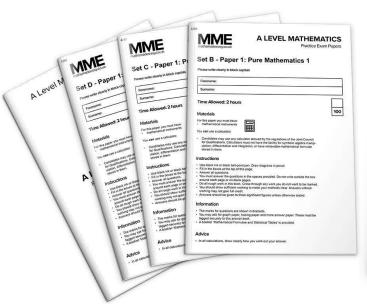
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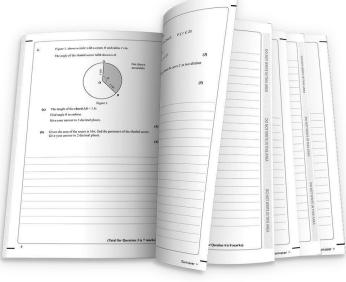
Revision Cards





Predicted Papers





Available to buy separately or as a bundle

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Section A

Answer all questions in the spaces provided.

1 Identify the expression below that is equivalent to c^{2/5}

Circle your answer.



2 It is given that $y = \frac{1}{x}$ and x < -1

Determine which statement below fully describes the possible values of y.

Tick (✓) one box.

 $-\infty < y < -1$ y > -1



[1 mark]

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3 It is given that

$$y = 3x^4 + \frac{2}{x} - \frac{x}{4} + 1$$

Find an expression for $\frac{d^2y}{dx^2}$

$$\frac{dy}{dx} = 12x^3 - \frac{2}{2x} - \frac{1}{4}$$

[3 marks]

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Turn over for the next question



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4	Find all the solutions of	
	$9\sin^2 x - 6\sin x + \cos^2 x = 0$	
	where $0^{\circ} \le x \le 180^{\circ}$	
	Give your solutions to the nearest degree.	
	Fully justify your answer.	[4 marks
	$9 \sin^2 x - b \sin x + \cos^2 x = 0$	Į4 marks
	=7 $9\sin^2 x - 6\sin x + (1 - \sin^2 x) = 0$	
	$=7 8 \sin^2 x - 6 \sin x + 1 = 0$	
	$= 7 (4 \sin x - 1)(2 \sin x - 1) = 0$	
	Sinx= 1/4 or Sinx= 1/2	
	x = 14°, 30°, 150°, 166°.	

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	Ov	59		

He states that the coefficient of the fourth term is 15120 Joseph's teacher comments that his answer is almost correct. Using a suitable calculation, explain the teacher's comment. Coefficient of the X³ term = *C3 x 24 x (-3) *x³ = -15120 x³ Toseph has the correct number but the urong sign, way due to making a mistake when cubing a negative number.	Joseph is exp	panding $(2-3x)^7$ in ascending powers of x.
Using a suitable calculation, explain the teacher's comment. $Coefficient of the x^{3} term =^{+}C_{3} \times 2^{4} \times (-3)^{3} x^{3} = -15120 x^{3} To steph has the correct number but the urong sign, when due to making a mistake$	He states that	it the coefficient of the fourth term is 15120
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= -15120 x = -15120 x = Toseph has the correct number but the wrong sign, well due to making a mistake	Using a suita	ble calculation, explain the teacher's comment.
wrong sign, when due to making a mistake	Coetto	
	Josep	h has the correct number but the
when cubing a negative number.	wrong	Sign, whey due to making a mistake
	when	cubing a negative number.

Turn over for the next question



5

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6 A circle has equation

$$x^2 + y^2 + 10x - 4y - 71 = 0$$

6 (a) Find the centre of the circle.

[2 marks]

$$x^{2} + y^{2} + 10x - 4y - 71 = 0$$

$$= 7 (x+5)^{2} - 25 + (y-2)^{2} - 4 - 71 = 0$$

$$= 7 (x+5)^{2} + (y-2)^{2} = 100$$

centre = (-5, 2)

6 (b) Hence, find the equation of the tangent to the circle at the point (1, 10), giving your answer in the form ax + by + c = 0 where a, b and c are integers.

[4 marks]

$$= \frac{10-2}{1+5} = 8 = \frac{14}{3}$$

: gradient of tangent = -3/4

Equation of tangent: y-10 = -3/4 (x-1)

$$=7$$
 $y = \frac{-3}{4} \times + \frac{3}{4} + 10$

$$=7$$
 $3x + 4y - 43 = 0$

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The population of	f a countr	y was 3	.6 m	illion i	n 1989.	
It grew exponent	ially to re	ach 6 m	illion	in 20	19.	
Estimate the popunchanged.	ulation of	the cou	intry	in 204	19 if the exponer	ntial growth continues
	6 ×	3.6	=	10	million	[2 marks]
			_			

Turn over for the next question



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8 (a) Using
$$y = 2^{2x}$$
 as a substitution, show that

$$16^x - 2^{(2x+3)} - 9 = 0$$

can be written as

$$y^2 - 8y - 9 = 0$$

$$2^{2\times +3} = 2^{2\times} \times 2^{2} = 89$$

[2 marks]

$$y_{1} + y_{1} + y_{2} + y_{3} + y_{4} + y_{5$$

can be wroten as y2-8y-9=0



8 (b) Hence, show that the equation

outside the box

$$16^x - 2^{(2x+3)} - 9 = 0$$

has $x = \log_2 3$ as its only solution.

Fully justify your answer.

[4 marks]

Thus 22x = 9 is the only real Solution.

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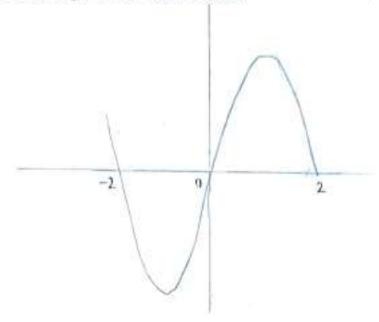
	$\int (4x - x^3) dx$
	$\int (4x-x^3) dx = 2x^4 - 1/4x^4 + c$ [2 marks]
9	
8	
5	
-	
- 1	
8	
(ii)	Evaluate
(ii)	
(ii)	$\int_{-2}^{2} (4x - x^{3}) dx$ $\left[2 \times^{2} - \frac{1}{4} \times^{4}\right]_{-2}^{2} = \left(2(2)^{2} - \frac{1}{4}(2)^{4}\right) - \left(2(-2)^{2} - \frac{1}{4}(-2)^{4}\right)$
(ii)	$\int_{-2}^{2} (4x - x^3) dx$
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Using a sketch, explain why the integral in part (a)(ii) does not give the area enclosed between the curve $y = 4x - x^3$ and the x-axis. 9 (b)

[2 marks]



$$=7 y = x(4-x^2)$$

The integral of the area below the x-axis

is negative, thus were carried with the area above the x-axis.

9 (c)

Find the area enclosed between the curve
$$y = 4x - x^3$$
 and the x-axis.
A rea = $2 \int_{a}^{2} 4x - x^3 dx$

$$= 2 \left[2x^{2} - \frac{1}{4}(2)^{2}\right]_{0}^{2} = 2\left[2(2)^{2} - \frac{1}{4}(2)^{2}\right]_{0}^{2}$$



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$$\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 - 12x + c$$

The curve has a turning point at (-1, 1)

10 (a) Find the coordinates of the other turning point of the curve.

Fully justify your answer.

her dy/dx = \$0

[6 marks]

$$3x^2 - 12x - 15 = 0$$

$$=7(3x-15)(x+1)=0$$

$$y = \int \frac{dy}{dx} dx = x^3 - 6x^2 - 15x + K$$

using known point (-1,1):

So the other turning point is (5,-107).



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(b)	Find the set of values of x for which y is increasing. [2 marks] $ \chi < -1 \text{and} x > 5 $	
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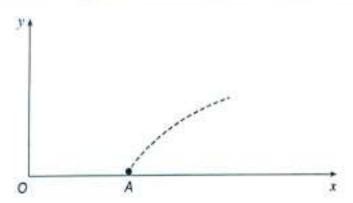


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11 A fire crew is tackling a grass fire on horizontal ground.

The crew directs a single jet of water which flows continuously from point A.



The path of the jet can be modelled by the equation

$$y = -0.0125x^2 + 0.5x - 2.55$$

where x metres is the horizontal distance of the jet from the fire truck at O and y metres is the height of the jet above the ground.

The coordinates of point A are (a, 0)

11 (a) (i) Find the value of a.

[3 marks]

$$=7 x^2 - 40x + 204 = 0$$

$$=7(x-6)(x-34)=0$$

11 (a) (ii) Find the horizontal distance from A to the point where the jet hits the ground.

[1 mark]

$$34 - 6 = 28$$
 mutres

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Calculate the maximum vertical height reached by the jet. [4 marks
$dx = -0.025 \times + 0.5$
let de/dx = 0
8 025 x = 0.5
=> x = 20
Max hught = -0.0125 (20) + 0 5(20) - 2.55
= 2.45 m
A vertical wall is located 11 metres horizontally from A in the direction of the jet. The height of the wall is 2.3 metres.
height of the wall is 2.3 metres.
height of the wall is 2.3 metres. Using the model, determine whether the jet passes over the wall, stating any necessary modelling assumption.
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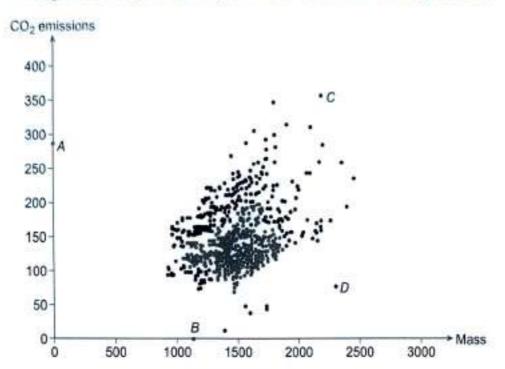


Section B

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Answer all questions in the spaces provided.

12 A student plots the scatter diagram below showing the mass in kilograms against the CO₂ emissions in grams per kilogram for a sample of cars in the Large Data Set.



Their teacher tells them to remove an error to clean the data.

Identify the data point which should be removed.

Circle your answer below.

[1 mark]



В

C

D



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13 The random variable X is such that $X \sim B\left(n, \frac{1}{3}\right)$

The standard deviation of X is 4

Find the value of n.

Circle your answer.

[1 mark]

9

12

18

72

Turn over for the next question



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14	A retail company has 5200 employees in 100 stores throughout the United Kingdo	m.
.7	The company recently introduced a new reward scheme for its staff.	
	The management team wanted to sample the staff to find out their opinions of the new scheme.	
	Three possible sampling methods were suggested:	
	Method A Choose 100 people who work at the largest store	
	Method B Choose one person at random from each of the 100 st	ores
	Method C List all employees in alphabetical order and assign each number from 1 to 5200	'nа
	Choose a random number between 1 and 52	
	Choose this person and every 52nd person on the list thereafter.	
14 (a)		nark)
	People from the same store are tiking to	
	have similar opiaions, so the sample would	
	be brazed.	
	-	
		_
		-
		_
14 (b)	Give one advantage of using Method B compared with using Method C.	nark]
	Each store is granenteed to be represented.	
		_
		_
		_
		-



c) (i)	Identify the method of sampling used in Method C. [1 mark]
	Systematic sampling -
) (ii)	Give a reason why Method C does not provide a random sample. [1 mark] Not all subsets of size 100
	are possible, so each sample of size 100 is
	not equally likely to be selected, so not rundern.
	Turn over for the next question

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	sample of t	en CO ₂ emiss	ions was	selected	from tr	e Large	Data Se
The emissi	ons in gran	ns per kilogran	n were:				
	13	45 45 0	49	77 49	49	49 78	
Find the st	andard dev	iation of the sa	ample.				
		22	q				
		alculated the a		CO ₂ emis	sions f	or cars in	the La
And the second second		and in 2016.					
The averag	ges are liste	d below.					
	Ye	ear of registra	ition	2002	2	2016	
	A	verage CO ₂ e	mission	171.	2	120.4	
Determine	whether th	is claim is con	rect.				
		122					
Fully justify	your answ						
Fully justify		ver. . 120:4)	- 2	= 145	8		
Fully justify	+1 -2 +					16 15	
Fully justify	+1·2 +	120-4)	ple .	size (ile iš l	arge
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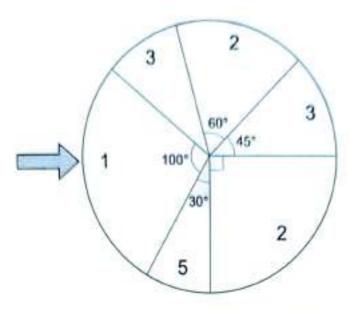
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16	A mathematical puzzle is published every day in a newspaper.
	Over a long period of time Paula is able to solve the puzzle correctly 60% of the time.
16 (a)	For a randomly chosen 14-day period find the probability that:
16 (a) (i)	Paula correctly solves exactly 8 puzzles [1 mark] P(X = 8) = 0.2.07
16 (a) (ii)	Paula correctly solves at least 7 but not more than 11 puzzles. $P\left(\ \times \leqslant I\left(\right) \ -\ P\left(\ \times \leqslant 6\right) \right]$
	= 0.96020841 - 0.1501401
	= 0.810
16 (b)	State one assumption that is necessary for the distribution used in part (a) to be valid. [1 mark]
	The ability to solve one puzzle is independent
	from any other day.
	Turn over for the next question



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A game consists of spinning a circular wheel divided into numbered sectors as shown below.



On each spin the score, X, is the value shown in the sector that the arrow points to when the spinner stops.

The probability of the arrow pointing at a sector is proportional to the angle subtended at the centre by that sector.

17 (a) Show that $P(X = 1) = \frac{5}{18}$

[1 mark]

$$P(X=1) = \frac{100}{360} = \frac{5}{18}$$

17 (b) Complete the probability distribution for X in the table below.

x	1	2_	3	5
D/V = -1	5	5,	2,	Age
P(X = x)	18	12	-9	12

[2 marks]

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box

$$P(X=1) = \frac{90+60}{360} = \frac{5}{12}$$

$$P(X=3) = \frac{45+35}{360}$$

$$P(X=5) = \frac{30}{360} = \frac{1}{12}$$

Turn over for the next question

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Find the probability that exactly one of the discs is blue. $P(sne below) = \frac{+}{12} \times \frac{5}{11} + \frac{5}{12} \times \frac{+}{11}$ $= \frac{35}{66}$	$P(\text{one belue}) = \frac{+}{12} \times \frac{5}{11} + \frac{5}{12} \times \frac{+}{11}$ $= \frac{35}{66}$				vn at rar						900	emen	t.	
P(one belue) = 12 x 11 + 12 x 11	$P(\text{one betwe}) = \frac{12}{12} \times \frac{1}{11} + \frac{1}{12} \times \frac{1}{11}$ $= \frac{35}{66}$	Find												12 -
= 35			P	(one	betwe				5	+	17	x #		[2]
		-		-		=	35							
		-												
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		_						_	_					
		05-0									-			
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														_
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[3 marks]

18 (b) Bag A contain	s 7 blue discs,	4 red discs and	1 yellow disc.
----------------------	-----------------	-----------------	----------------

Bag B contains 3 blue discs and 6 red discs.

A disc is drawn at random from Bag A and placed in Bag B.

A disc is then drawn at random from Bag B.

Find the probability that the disc drawn from Bag B is red.

$$\frac{28}{120} + \frac{48}{120} = \frac{14}{30}$$



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19 It is known from historical data that 15% of the residents of a town buy the local weekly newspaper, 'Local News'.

A new free weekly paper is introduced into the town.

The owners of 'Local News' are interested to know whether the introduction of the free newspaper has changed the proportion of residents who buy their paper.

In a random sample of 50 residents of the town taken after the free newspaper was introduced, it was found that 3 of them purchased 'Local News' regularly.

Investigate, at the 5% significance level, whether this sample provides evidence that the proportion of local residents who buy 'Local News' has changed.

[6 marks] "Number of residents who buy Local News" 0.15 Ho P = HI: P # 0.15 For Ho: X ~ B(50,0.15) P(X & 3) = 0.04604657 0.046> 0.025 Therefore, we accept the as there is insuffuent endence to suggest that the trabatran at residents buying "Local News has changed.

END OF QUESTIONS

