



Oxford Cambridge and RSA

**GCE**

**Further Mathematics A**

**Y542/01: Statistics**

Advanced GCE

**Mark Scheme for November 2020**

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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## Text Instructions

## Annotations and abbreviations

Annotation in RM assessor	Meaning
✓ and ✖	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank Page
Seen	
Highlighting	
Other abbreviations in mark scheme	Meaning
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
a wrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.

**Subject-specific Marking Instructions for A Level Mathematics A**

- a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words “Determine” or “Show that”, or some other indication that the method must be given explicitly.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

d When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation ‘dep\*’ is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

- When a value **is given** in the paper only accept an answer correct to at least as many significant figures as the given value.

- When a value **is not given** in the paper accept any answer that agrees with the correct value to **3 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.

NB for Specification B (MEI) the rubric is not specific about the level of accuracy required, so this statement reads “2 s.f”.

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for  $g$  should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

g Rules for replaced work and multiple attempts:

- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
- If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
- If a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate’s data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. Note that a miscopy of the candidate’s own working is not a misread but an accuracy error.

i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold “In this question you must show detailed reasoning”, or the command words “Show” or “Determine”. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question		Answer	Marks	AO	Guidance		
1		$53.1 \pm 1.96 \sqrt{\frac{30}{8}}$ (49.30, 56.90)	<b>M1</b> <b>A1</b> <b>A1</b> <b>A1</b> <b>[4]</b>	3.3 1.1 1.1 3.4	Correct structure with 8 Square root correct Awrt 1.96 used, can be implied Both, only these numbers (4 sf needed at least once)	Allow e.g. (49.30, 56.9)	
2	(a)	(i)	The points do not lie very close to a straight line	<b>B1</b> <b>[1]</b>	1.1	Or equivalent. Must refer to diagram, not just to “correlation”	Ignore extras unless wrong
		(ii)	$H_0: \rho = 0, H_1: \rho > 0$ , where $\rho$ is the population pmcc between prices in 1972 and prices in 2018  $0.381 < 0.4973$ Do not reject $H_0$ .  There is insufficient evidence of (positive) correlation between prices in the two years.	<b>B2</b>  <b>M1</b> <b>M1ft</b> <b>A1ft</b> <b>[5]</b>	1.1 2.5  1.1 1.1 2.2b	One error, e.g. $\rho$ not defined, B1 (but allow “population” not stated) $H_0: r = 0, H_1: r > 0$ : same scheme, but B2 needs “population” pmcc Compare with 0.497(3) Correct first conclusion, needs like-with-like In context, not too definite	$H_0$ : no correlation, $H_1$ : positive correlation: B1  FT on CV 0.5760 only
		<b>Exx</b>	$\alpha$ : Insufficient evidence to reject $H_0$ . No correlation between ... $\beta$ : Wrong first conclusion, correct interpretation: M0A0 $\gamma$ : Hypotheses wrong way round: maximum M1M1			M1A1 (bod)	
	(b)		0.650	<b>B2</b> <b>[2]</b>	3.1a 1.1	Full marks for correct answer by any method	SC: if B0 allow B1 for any 3 of 8.85, 46.35, 8.8725, 241.7331, 43.153

Question	Answer	Marks	AO	Guidance	
3 (a)	$H_0: m_A = m_B$ , $H_1: m_A < m_B$ where $m_A$ and $m_B$ are the median journey times for $A$ and $B$ $W \sim N(180, 510)$	<b>B1</b>	1.1	<i>OR</i> : Median journey times equal, oe. Allow if <i>ms</i> used but not defined	Allow “mean” or “average” only if “population” stated
		<b>B1</b>	1.1	Both, can be implied, needs $m = 12$	Allow $\sqrt{510}$ or $510^2$
	Consider correct tail, either 219 or 141 ( $R_m = 219$ , $m(m + n + 1) - R_m = 141$ )	<b>M1</b>	1.1	Find <i>either</i> $P(\geq 219)$ (218.5) <i>or</i> $P(\leq 141)$ (141.5)	Use of 0.9559 is M0 here. For CV method see below
	$p = \Phi\left(\frac{141.5 - 180}{\sqrt{510}}\right) = 0.0441\dots$ <b>BC</b>  $0.0441 < 0.1$	<b>M1</b> <b>A1</b> <b>A1ft</b>	1.1 1.1 1.1	Needs <i>some</i> evidence. E.g.: 0.0421, 0.0401, 0.470 (no/wrong cc, $\sqrt{\phantom{x}}$ ): M1	0.9559 > 0.9: A1A1 (M1A1) 0.9559 > 0.1: A1A0 M0A0
	<b>OR:</b> CV $180 - z \times \sqrt{510}$ 141 (141.5) used $z = 1.282$ (CV = 151.05, 151.058..) <b>A1</b> $141.5 < 151.05(85)$ or $218.5 > 208.95$ <b>A1</b>	<b>M1</b> <b>M1</b> <b>A1</b> <b>A1</b>		Allow $\sqrt{\phantom{x}}$ errors  Stated or implied CV and cc correct e.g. $141 < 150.55$	180 + 1.282 $\sqrt{510}$ etc is M0 <i>unless</i> 219 (218.5) used, in which case give M2(A1A1) E.g. $219 > 209.45$
Reject $H_0$ . Significant evidence that route B takes longer	<b>M1ft</b> <b>A1ft</b> <b>[8]</b>	1.1 2.2b	Correct first conclusion Contextualised, not too definite	Needs like-with-like, e.g. 0.9559 with 0.9	
	SC Sum of A's ranks = $435 - 219 = 216$ used: B1B0 M0M1A0A1 M1A1 max 5/8				
	<b>Exx</b> $\alpha$ : $H_0$ : Journey times are the same, $H_1$ : journey times for $B$ are higher: <b>B0</b> $\beta$ : $H_0$ : No evidence that median journey times are different, etc: <b>B0</b>				
(b)	Must be a random sample (of all journeys) <i>Or</i> distributions must be same shape (necessary assumption for Wilcoxon rank-sum test!)	<b>B1</b> <b>[1]</b>	3.5b	Or equivalent. Allow “(journeys) independent”	<i>Not</i> “representative”.



Question		Answer	Marks	AO	Guidance
4		$3E(X) = 30$ or $E(X) = 10$ $9 \times \text{Var}(X) = 36$ or $\text{Var}(X) = 4$ $\frac{1}{12}(n^2 - 1) = 4$ $\Rightarrow n = 7$ $E(X - m) = \frac{1}{2}(n + 1)$	<b>B1</b> <b>B1</b> <b>M1</b> <b>A1</b> <b>M1</b>	2.2a 2.2a 1.1 2.2a 3.1b	Used, stated or implied One of these, used, stated or implied Use variance of uniform $n = 7$ only, no need for “reject –7” Use expectation of uniform, e.g. $2m + n + 1 = 20$ .
	<b>OR:</b>	$\text{Var}(Y + m) = \frac{1}{12}(n^2 - 1)$ $\Rightarrow n = 7$ $E(Y + m) = \frac{1}{2}(n + 1) + m$	<b>M1</b> <b>A1</b> <b>M1</b>	1.1 2.2a 3.1b	$n = 7$ only, no need for “reject –7” Use expectation of uniform, e.g. $2m + n + 1 = 20$ .
		$10 - m = 4$ $m = 6$	<b>M1</b> <b>A1</b> <b>[7]</b>	2.1 2.2a	Validly derive single equation for $m$ $m = 6$ only NB: $\text{Var} = (n - 1)^2/12$ is from <i>continuous</i> uniform!

Question		Answer	Marks	AO	Guidance	
5	(a)	${}^5C_3 \times {}^{21}C_2 + {}^5C_4 \times {}^{21}C_1 + 1$ [= 2100 + 105 + 1] $\div {}^{26}C_5$ [= 65780] $\frac{1103}{32890}$ or 0.0335...	<b>M1dep</b> <b>A1</b>  <b>*depM1</b> <b>A1</b> <b>[4]</b>	3.1b 1.1  1.1 3.2a	Any correct pair of ${}^nC_r$ s multiplied All terms correct  Awrt 0.0335 or any exact fraction  Or $1 - P(0, 1, 2) = 1 - .9665$ e.g. $\frac{2206}{65780}$ or $\frac{264720}{7893600}$	
		<b>OR:</b> $Or: \frac{5}{26} \times \frac{4}{25} \times \frac{3}{24} \times \frac{2}{23} \times \frac{1}{22}$ $\frac{5}{26} \times \frac{4}{25} \times \frac{3}{24} \times \frac{2}{23} \times \frac{21}{22} \times 5$ $\frac{5}{26} \times \frac{4}{25} \times \frac{3}{24} \times \frac{21}{23} \times \frac{20}{22} \times 10$ Total $\frac{1103}{32890}$ or 0.0335...	<b>B1</b> <b>B1</b> <b>B1</b> <b>B1</b> <b>[4]</b>	Must have 5 oe, e.g. ${}^5C_1$ Must have 10 oe, e.g. ${}^5C_3$		
	(b)	(i)	$\frac{22! \times 5!}{26!}$ ( $= \frac{1 \times 2 \times 3 \times 4 \times 5}{23 \times 24 \times 25 \times 26} = \frac{120}{358800}$ ) $= \frac{1}{2990}$ <b>AG</b>	<b>M1</b> <b>A1</b> <b>A1</b> <b>[3]</b>	1.1 2.1 2.2a	Oe. Allow M1 for 21! instead of 22! Fully correct Correctly obtain AG using exact method  $\frac{1 \times 2 \times 3 \times 4 \times 5}{22 \times 23 \times 24 \times 25 \times 26}$ : M1 Allow even if no working after $22! \times 5! \div 26!$
		(ii)	22 fences: 22 for [VVV] $\times$ 21 for [VV] Consonants arranged in 21! ways Vowels arranged in 5! ways ( $= {}^5P_3 \times {}^2P_2$ ) Product $\div 26! = \frac{21}{2990}$ ( $= 2.832 \times 10^{24} \div 4.0329 \times 10^{26}$ )	<b>M1</b> <b>M1</b> <b>A1</b> <b>A1</b> <b>[4]</b>	3.1b 1.1 2.1 3.2a	Correct strategy, allow ${}^{22}C_2$ for ${}^{22}P_2$ At least one of these, no subtraction Both correct Allow from calculator but must be exact fraction  21! $\times$ 3! $\times$ 2! $\times$ 22 $\times$ 21: M2A0 21! $\times$ 3! $\times$ 2! $\div$ 26! M0M1 ${}^5C_3 \times 3! \times 2! = 5!$
		<b>OR:</b>	Treat 21 consonants, [VVV] and [VV] as 23 23! $\times$ 5! / 26! ( $= 1/130$ ) Subtract $2 \times 1/2990$ Answer is $\frac{21}{2990}$	<b>M1</b> <b>A1</b> <b>M1</b> <b>A1</b> <b>[4]</b>	3.1b 2.1 3.2a 1.1	Correct strategy, allow 23! $\times$ 2! $\times$ 3! Correct ( $5! = {}^5P_3 \times {}^2P_2 = {}^5C_3 \times 2! \times 3!$ ) M1 also for subtracting $1 \times 1/2990$ Final answer, exact fraction (11/1495 is M1A1M1A0)

Question		Answer	Marks	AO	Guidance
6	(a)	Any reason for independence (or not) ... and for constant average rate (or not), in each case without misunderstanding of what they mean	<b>B1</b> <b>B1</b> [2]	3.5b 3.5b	“Events occur independently and at constant average rate”: B0 SC: Mere assertion of both, properly contextualised: B1 SC: Variance = 4.67 which is closer to 5: B1 SC: Considers only the assumptions given in the question: B0
	(b)	(i)	0.146(223) <b>BC</b>	<b>M1</b> <b>A1</b> [2]	3.4 1.1 Correct method stated or implied Correct answer only, awrt 0.146
		(ii)	0.133(372) <b>BC</b>	<b>M1</b> <b>A1</b> [2]	1.1 1.1 0.068: M1A0 (treat 0.1337 as a slip, i.e. give A1 BOD)
	(c)	Po(12.2) P( $\leq 15$ ) – P( $\leq 9$ )                      [= 0.8296 – 0.2253]  = 0.604(224) <b>BC</b>	<b>M1</b> <b>M1</b>  <b>A1</b> [3]	3.3 1.1  3.4	Stated or implied Allow P( $\leq 16$ ) or P( $\leq 10$ ), e.g. 0.503 or 0.662 (M1M1A0) Allow this M1 also from $\lambda = 7.2$ (0.187, 0.110, 0.189) Correct answer only, awrt 0.604
	(d)	Sales of CD players and integrated systems need to be independent	<b>B1</b> [1]	1.1	Need “independent” or “not related” clearly referred to the two types of machine. <i>Not just</i> “purchases independent” or “distributions independent”
	(e)	If a customer buys a CD player they probably won’t (or will) buy an integrated system as well	<b>B1</b> [1]	3.5b	Any reason for non-independence of sales of CD players and integrated sound systems Can get B0B1 provided they are focussing on independence
		<b>Exx</b>	$\alpha$ : May buy both so not independent: B0 $\beta$ : Often bought together: B1 $\gamma$ : Misunderstanding of context, e.g. CDs/CD players, or assuming that integrated systems don’t include CD players: can get B1		

Question		Answer	Marks	AO	Guidance	
7	(a)	Geometric Mean = $400 \div 100 (= 4)$ and $p = 1/\text{mean}$	M1 M1	1.1 2.4	Stated explicitly Use mean (or P(1) etc) to deduce $p$ (“Determine”, so justification is needed for 0.25)	Needs to deduce $p$ in part (a), not defer it to (b)  SC Geo(0.2) using $P(1) = 0.2$ : M1M1A0
		Therefore $p = 0.25$	A1 [3]	1.1	Allow even if second M1 not gained	
		Probability is $0.75^6 (= 0.1779785\dots)$	M1	3.3		
	(b)	OR: Or: 0.177978 or 0.177979 or better seen, or $1 - [P(1) + \dots + P(6)]$ with evidence, e.g. formula	M1		Allow $\pm 1$ term	
		Expected frequency = probability $\times 100 = 17.798$	A1 [2]	2.1	17.798 correctly obtained, with sufficient evidence, www	$100 - \Sigma(\text{other frequencies})$ : SC B1
	(c)	$H_0$ : data consistent with (geometric) distribution $H_1$ : not consistent $\Sigma X^2 = 9.005$ $9.005 < 11.07$ ( $\nu = 5$ ) Do not reject $H_0$ .  Insufficient evidence that a geometric distribution is not a good fit.	B1 B1 B1 M1ft  A1ft [5]	1.1 1.1 1.1 1.1  2.2b	Both, allow equivalents, but not “evidence that ...”. 9.005 or 9.01 Compare their $\Sigma X^2$ with 11.07 Correct first conclusion, ft on their 9.005 or on 12.59, needs like-with-like Contextualised, not too definite (needs double negative) Don’t penalise “Geo(0.25)”	E.g. $H_0: X \sim \text{Geo}(p)$ Allow Geo(0.25)  Allow from comparison with 12.59 but nothing else  Allow addition slip in $\Sigma X^2$ SC Geo(0.2): can get full marks if given data used, $\Sigma X^2 = 4.54$ used gets B1B1B0M1A1
	Exx	$\alpha$ : Reject $H_0$ . Data is consistent with geometric: $\beta$ : Insufficient evidence to reject $H_0$ . Data is consistent with geometric:		M1A0 M1A1 (BOD)		

Question		Answer	Marks	AO	Guidance
8	(a)	$\int_1^{\infty} kx^{-n} dx = \left[ \frac{k}{(1-n)x^{n-1}} \right]_1^{\infty}$ $= \frac{k}{n-1} = 1 \text{ so } k = n - 1$	<b>M1</b> <b>B1</b> <b>A1</b> <b>[3]</b>	1.1 1.1 1.1	Integral attempted, correct limits Correct indefinite integral Correctly obtain $k = n - 1$ , www Don't need full details of $\lim(a \rightarrow \infty)$
	(b) (i)	$\int 3x^{-4} dx = -\frac{1}{x^3} + c$ $x = 1, F(x) = 0 \text{ so } c = 1. \text{ Hence } 1 - x^{-3}.$ $F(x) = \begin{cases} 0 & x < 1, \\ 1 - \frac{1}{x^3} & x \geq 1 \end{cases}$	<b>M1</b> <b>A1</b> <b>B1</b> <b>[3]</b>	1.1 1.1 1.1	Needs + $c$ or definite integral between 1 and $x$ , oe Fully correct active part of CDF "0 for $x < 1$ " stated and no wrong ranges (doesn't need M1 or A1) Allow $\leq$ for $<$ , and/or $>$ for $\geq$ Wrong $k$ : can get M1A0B1 Ignore ranges here Or "0 otherwise" if " $x \geq 1$ " stated in active part
	(ii)	$\frac{P[(X > 7) \cap (X > 5)]}{P(X > 5)} = \frac{P(X > 7)}{P(X > 5)}$ $= \frac{1 - F(7)}{1 - F(5)}$ $= \frac{125}{343} \text{ or } 0.364(431\dots)$	<b>M1*</b> <b>A1</b> <b>*depM1</b> <b>A1ft</b> <b>[4]</b>	3.1a 3.1a 3.3 1.1	Use conditional probability method $P[(X > 7) \cap (X > 5)] = P(X > 7)$ Convert probabilities into $F(X)$ , <i>not</i> using $P(X > 7) \times P(X > 5)$ Any exact fraction or awrt 0.364, ft on $1 - a/x^3, a \neq 0, 1$ $\frac{[1 - F(7)][1 - F(5)]}{1 - F(5)}$ M1A0M0A0 Allow from $F(x) = 1 - a/x^3$ , otherwise www
	(c)	$E(X^2) = \int_1^{\infty} kx^{2-n} dx = \left[ \frac{kx^{3-n}}{(3-n)} \right]_1^{\infty} \quad (n \neq 3)$ <p>If <math>n = 3, E(X^2) = \lim_{x \rightarrow \infty} [2 \ln(x)]</math>, not defined</p> <p>Infinite integral does not converge if <math>3 - n \geq 0</math></p> <p>If <math>n \geq 4</math> then <math>E(X) = \left[ \frac{kx^{2-n}}{(2-n)} \right]_1^{\infty}</math> converges</p> <p>Therefore <math>\text{Var}(X)</math> is not defined if and only if <math>n = 2</math> or <math>3</math>.</p>	<b>M1*</b> <b>B1</b>  <b>*depM1</b>  <b>B1</b> <b>A1</b> <b>[5]</b>	2.1 1.1  2.2a  2.3 2.2a	Correct limits needed somewhere Correct indefinite integral or $\frac{n-1}{n-3}$ No marks just for this unless last 3 marks all zero, then if this (or for $n = 2$ ) is shown, award SC B1 Make deduction based on convergence, ft Consider convergence of $E(X)$ Shown not defined for $n = 2$ or $3$ and <i>only</i> for those SC: $E(X^2) = \frac{n-1}{n-3}$ , M1B1 $E(X) = \frac{n-1}{n-2} \Rightarrow n \neq 2$ or $3$ : (not valid, must consider $\ln$ if $n = 2$ or $3$ ): B0 No limits used: M0B1M0B0 SC: $\text{Var}(X) < 0$ when $n < 3$ : M1B1M1 (B0) A0 But no need to state "if and only if"

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