Write your name here Surname Other names Candidate Number Centre Number Pearson Edexcel Level 1/Level 2 GCSE (9 - 1) **Mathematics** Paper 1 (Non-Calculator) **Higher Tier** Paper Reference Specimen Papers Set 2 Time: 1 hour 30 minutes 1MA1/1H You must have: Ruler graduated in centimetres and millimetres, Total Marks protractor, pair of compasses, pen, HB pencil, eraser.

#### Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided

   there may be more space than you need.
- Calculators may not be used.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- You must show all your working out.

#### Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

#### Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.



Turn over ▶

**PEARSON** 

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# Answer ALL questions.

# Write your answers in the spaces provided.

You must write down all the stages in your working.

1 (a) Factorise 
$$y^2 + 27y$$

y(y+27+)

(b) Simplify  $(t^3)^2$ 

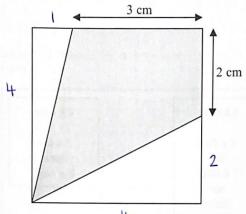
t 6

(c) Simplify  $\frac{w^9}{w^4}$ 

ω<sup>3</sup> (1)

(Total for Question 1 is 3 marks)

2 The diagram shows a square with perimeter 16 cm.



Work out the proportion of the area inside the square that is shaded.

Square side length = 
$$\frac{16}{4}$$
 = 4

Area of nonshaded pare = 
$$\left(\frac{1}{2} \times 1 \times 4\right) + \left(\frac{1}{2} \times 2 \times 4\right)$$
  
= 6

$$\frac{16-6}{16} = \frac{5}{8}$$

5

(Total for Question 2 is 5 marks)

3 David has designed a game.

He uses a fair 6-sided dice and a fair 5-sided spinner.

The dice is numbered 1 to 6

The spinner is numbered 1 to 5

Each player rolls the dice once and spins the spinner once.

A player can win £5 or win £2

Win £5	Win £2
roll a 5	roll a 1
and	or
spin a 5	spin a 1
	or
	both

David expects 30 people will play his game. Each person will pay David £1 to play the game.

(a) Work out how much profit David can expect to make.

$$\frac{1}{6} \times \frac{1}{5} = \frac{1}{30} \quad (win £5)$$

$$\frac{1}{6} + \frac{1}{5} + \frac{1}{30} = \frac{12}{30} \quad \left(\frac{1}{6} \times \frac{4}{5}\right) + \left(\frac{5}{6} \times \frac{1}{5}\right) + \frac{1}{30} \times 30 \times 2$$

$$= \frac{1}{3}$$

$$50 \frac{1}{30} \text{ win £5 and } \frac{1}{3} \text{ win £2}.$$

So 
$$\frac{1}{30}$$
 win  $\pm 5$  and  $\frac{1}{3}$  win  $\pm 2$ .  
Profix =  $30 - (\frac{1}{30} \times 30 \times 5) - (\frac{1}{3} \times 30 \times 2) = 5$ 

(b) Give a reason why David's actual profit may be different to the profit he expects to make.

This is just based on probability, the actual profit may vary -

(1)

(Total for Question 3 is 5 marks)

4 Triangle ABC has perimeter 20 cm.

$$AB = 7$$
 cm.

$$BC = 4$$
 cm.

By calculation, deduce whether triangle ABC is a right-angled triangle.

$$AC = 20 - 7 - 4 = 9$$

$$4^2+7^2=65 \neq 9^2=81$$

## (Total for Question 4 is 4 marks)

5 One sheet of A3 card has area  $\frac{1}{8}$  m<sup>2</sup>.

The card has a mass of 160 g per m<sup>2</sup>.

Work out the total mass of 25 sheets of A3 card.

$$160 \times \frac{1}{8} = 20$$

5009

(Total for Question 5 is 4 marks)

**6** (a) Work out  $2\frac{1}{4} \times 3\frac{1}{3}$ 

Give your answer as a mixed number in its simplest form.

$$2\frac{1}{4} \times 3\frac{1}{3} = \frac{9}{4} \times \frac{10}{3} = \frac{90}{12} = \frac{45}{6} = \frac{15}{2} = 7\frac{1}{2}$$



(b) Write the numbers 3, 4, 5 and 6 in the boxes to give the greatest possible total. You may write each number only once.

$$5\frac{1}{4} + 6\frac{2}{3}$$

(1)

(Total for Question 6 is 4 marks)

7 A shop has a sale.

Microwave ovens

 $\frac{1}{3}$  off normal price

Combination ovens

40% off normal price

A microwave oven has a sale price of £90 A combination oven has a sale price of £84

Which of these ovens has the greater normal price? You must show all your working.

$$90 \div \frac{2}{3} = \frac{90 \times 3}{2} = 135$$

$$84 \div \frac{6}{10} = \frac{840}{6} = 140$$

Combination oven.

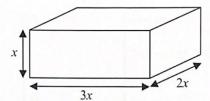
(Total for Question 7 is 4 marks)

8 Work out an estimate for  $\sqrt{4.98 + 2.16 \times 7.35}$ 

$$\approx \sqrt{5+2\times7} = \sqrt{19} \approx 4.3$$

4.3

(Total for Question 8 is 3 marks)



All measurements are in centimetres. *x* is an integer.

The total volume of the cuboid is less than 900 cm<sup>3</sup>

Show that  $x \leq 5$ 

$$\chi \times 3x \times 2x < 900$$
=7  $6x^3 < 900$ 
=7  $\chi^3 < 150$ 
=7  $\chi < \sqrt{3} \sqrt{150}$ 

$$\sqrt{3} \sqrt{125} = 5$$

$$6^3 = 216$$

As x is an integer, x <6, so x ≤5

(Total for Question 9 is 3 marks)

10 *y* is inversely proportional to *x* When x = 1.5, y = 36

Find the value of y when x = 6

$$y = \frac{k}{x}$$

$$y = \frac{54}{6} = 9$$

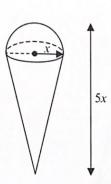
$$36 = \frac{k}{1.5}$$

$$= 7k = 54$$

9

(Total for Question 10 is 3 marks)

11 A solid is made by putting a hemisphere on top of a cone.



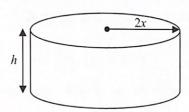
Volume of cone =  $\frac{1}{3}\pi r^2 h$ 



Volume of sphere =  $\frac{4}{3}\pi r^3$ 



The total height of the solid is 5xThe radius of the base of the cone is xThe radius of the hemisphere is x



height of cone = 5x-x=4xVolume of cone =  $\frac{1}{3}\pi x^2 4x$ =  $\frac{4}{3}\pi 4x^3$ 

Volume of hemisphere =  $\frac{1}{2} \times \frac{4}{3} \pi x^3$ =  $\frac{2}{3} \pi x^3$ 

Volume of  $= \frac{2}{3} \pi x^3 + \frac{1}{3} \pi x^3$  $= \left[2\pi x^3\right]$ 

Volume of Cyclinder =  $\pi(2x)^2 xh$ =  $4x^2 \pi h$ 

A cylinder has the same volume as the solid. The cylinder has radius 2x and height h All measurements are in centimetres.

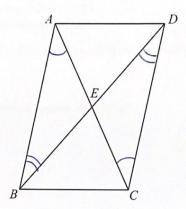
Find a formula for h in terms of x Give your answer in its simplest form.

Vsolid = Vcylinder =7  $\cancel{x}_{\pi} \cancel{x}^{3} = \cancel{x}_{\pi}^{2} \cancel{x}_{h}$ =7 2h = x=7  $h = \frac{x}{2}$ 

 $h = \frac{x}{2}$ 

(Total for Question 11 is 5 marks)

12 ABCD is a parallelogram.



E is the point where the diagonals AC and BD meet.

Prove that triangle ABE is congruent to triangle CDE.

AB = DC, because opposite sides of a parallelogram are equal.

Angle BAE = Angle ACD because the are alternate angles.

Angle ABE = Angle CDE for the same reason. Hence  $\triangle$  ABE is congruent to  $\triangle$ CDE due to ASA

(Total for Question 12 is 3 marks)

13 Mr Brown gives his class a test.

The 10 girls in the class get a mean mark of 70%

The 15 boys in the class get a mean mark of 80%

Nick says that because the mean of 70 and 80 is 75 then the mean mark for the whole class in the test is 75%

Nick is not correct.

Is the correct mean mark less than or greater than 75%?

You must justify your answer.

The mean mark for boys is greater than girls, there are also more guids boys than girls. Thus, the mean mark for the whole class win be greater than 75.

(Total for Question 13 is 2 marks)

14 Show that 
$$\frac{(4-\sqrt{3})(4+\sqrt{3})}{\sqrt{13}}$$
 simplifies to  $\sqrt{13}$ 

$$= \frac{16-3}{\sqrt{13}} = \frac{13}{\sqrt{13}} = \frac{\sqrt{13}\sqrt{13}}{\sqrt{13}} = \sqrt{13}$$

(Total for Question 14 is 2 marks)

15 (a) Find the value of 
$$\sqrt[3]{8 \times 10^6}$$
 =  $\sqrt[3]{8} \times \sqrt[3]{10^6}$   
=  $2 \times 10^2 = 200$ 

(b) Find the value of 
$$144^{\frac{1}{2}} \times 64^{\frac{1}{3}} = 12 \times \frac{1}{3\sqrt{64}} = 12 \times \frac{1}{4} = 3$$

(c) Solve 
$$3^{2x} = \frac{1}{81}$$

$$50 - 4 = 1x$$
$$x = -2$$

$$x = \frac{-2}{(2)}$$

## (Total for Question 15 is 5 marks)

16 The probability that Sanay is late for school tomorrow is 0.05 The probability that Jaden is late for school tomorrow is 0.15

Alfie says that the probability that Sanay and Jaden will both be late for school tomorrow is 0.0075 because  $0.05 \times 0.15 = 0.0075$ 

What assumption has Alfie made?

That the two events are independent.

hier

(Total for Question 16 is 1 mark)

17 Solve  $x^2 - 6x - 8 = 0$ 

Write your answer in the form  $a \pm \sqrt{b}$  where a and b are integers.

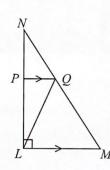
$$= (x-3)^{2} - 9 - 8 = 0$$

$$= (x-3)^{2} = 17$$

$$= x = 3 \pm \sqrt{17}$$

(Total for Question 17 is 3 marks)

18 LMN is a right-angled triangle.



$$16 \div 8 = 2$$
  
So  $PL = 2PN$   
Area of LMN =  $8 \times (2+1)^2$   
=  $72 \text{ cm}^2$ 

Angle  $NLM = 90^{\circ}$ PQ is parallel to LM.

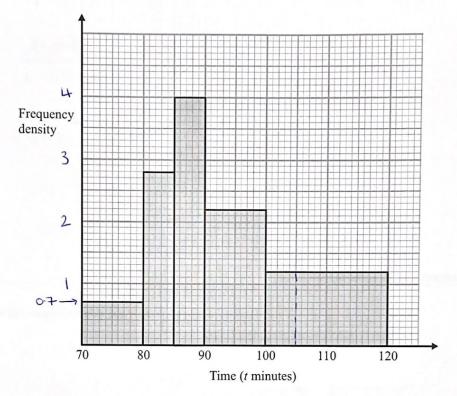
The area of triangle PNQ is 8 cm<sup>2</sup> The area of triangle LPQ is 16 cm<sup>2</sup>

Work out the area of triangle LQM.

48

 $cm^2$ 

(Total for Question 18 is 4 marks)



7 cyclists took 80 minutes or less to finish the race.

(i) Work out an estimate for the number of cyclists who took more than 105 minutes to finish the race.

$$7 \div (80-70) = 0.7$$
  
 $15 \times 1.2 = 18$ 

18

(ii) Explain why your answer to part (i) is only an estimate.

of people over 10105 mins is unknown.

(Total for Question 19 is 4 marks)

DO NOT WRITE BY THIS AREA

20 Show that  $\frac{3x+6}{x^2-3x-10} \div \frac{x+5}{x^3-25x}$  simplifies to ax where a is an integer.

$$= \frac{3(x+2)}{(x-5)(x+2)} \div \frac{(x+5)}{x(x^2-25)}$$

$$= \frac{3}{(x-5)} \times \frac{x(x-5)(x+5)}{(x+5)} = \frac{3x}{x+6}$$

(Total for Question 20 is 4 marks)

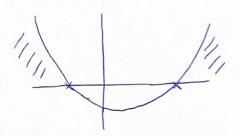
21 Solve the inequality  $x^2 > 3(x+6)$ 

$$= x^{2} > 3x + 18$$

$$= x^{2} - 3x - 18 > 0$$

$$= (x - 6)(x + 3) > 0$$

$$x > 6 \text{ or } x < -3$$



x76, x<-3

(Total for Question 21 is 4 marks)

22 The line *l* is a tangent to the circle  $x^2 + y^2 = 40$  at the point *A*. *A* is the point (2, 6).

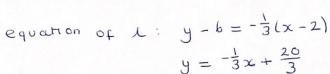
The line l crosses the x-axis at the point P.

Work out the area of triangle OAP.

graduant of normal to

$$A = \frac{6-0}{2-0} = 3$$

gradient of 
$$l = \frac{1}{3} \times -1 = -\frac{1}{3}$$



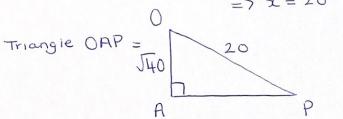
crosses x-axis: 
$$(y=0)$$
  $0 = -\frac{1}{3}x + \frac{20}{3}$   
=>  $x = 20$  (P = (20,0))

-140

0

-540

2



$$20^2 = (J_{40})^2 + AP^2$$
  
=>  $AP = J_{360} = 6J_{10}$ 

Area = 
$$\frac{1}{2} \times 6\sqrt{10} \times \sqrt{40} = 3\sqrt{400} = 3\times20 = 60$$

60

(Total for Question 22 is 5 marks)

### TOTAL FOR PAPER IS 80 MARKS