| Volume of 3D Shapes Mark Scheme |  |  |
| :---: | :---: | :---: |
| 1 | $3 \times 12 \times 16=576 \mathrm{~cm}^{3}$ | [1] |
| 2 | $\text { Volume }=\frac{a^{2} h}{3}=\frac{5^{2} \times 12}{3}$ | [1] Substitution of values |
|  | Volume $=100 \mathrm{~m}^{3}$ | [1] Correct answer |
| 3(a) | $4 \times 4=16$ $2 \times 3=6$ <br> $6 \mathrm{~cm}^{2}$ <br>  2 cm <br> $16 \mathrm{~cm}^{2}$  <br> 4 cm  | [1] Correct method |
|  | Area of Cross section $=16+6=22 \mathrm{~cm}^{2}$ | [1] Correct answer |
| 3(b) | $\begin{aligned} \text { Volume }= & \text { area of cross section } \times \text { length } \\ & =22 \times 3=66 \mathrm{~cm}^{3} \end{aligned}$ | [1] Substitution of values |
| 4 | $\begin{gathered} \text { Volume }=\pi r^{2} h \\ \text { Volume }=\pi \times 4.5^{2} \times 2=127.23 \mathrm{~cm}^{3} \end{gathered}$ | [1] Substitution of values |
|  | $127.23 \mathrm{~cm}^{3}$ | [1] Correct answer |
| 5 | Volume of sphere $=\frac{4}{3} \pi r^{3}$ | [1] Substitution of values |
|  | Volume $=\frac{4}{3} \times \pi \times 4^{3}=\frac{256 \pi}{3}$ | [1] Correct answer |
| 6 | Substituting these values into the formula to find $h$ : $\begin{aligned} & 1500=8^{2} \pi h \\ & 1500=64 \pi h \end{aligned}$ | [1] Substitution of values |
|  | $h=\frac{1500}{64 \pi}=7.46(2 \mathrm{dp})$ | [1] Rearranging to find $h$ |
|  | The water reaches 7.46 cm from the base of the cylinder. | [1] Correct answer |
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| 7 | $\begin{aligned} & \frac{1}{3} \times h \times \pi r^{2} \\ & h=10 r=3 \end{aligned}$ | [1] Correct volume formula |
| :---: | :---: | :---: |
|  | $\frac{1}{3} \times 10 \times \pi \times 3^{2}=\frac{1}{3} \times 90 \pi=30 \pi$ | [1] Substitution of values |
|  | $\text { Volume }=\frac{\frac{4}{3} \times \pi \times 3^{3}}{2}=\frac{108 \pi}{6}=18 \pi$ | [1] Volume of hemi-sphere |
|  | $18 \pi+30 \pi=48 \pi \mathrm{~cm}^{3}$ | [1] Correct answer |
| 8 | $\begin{aligned} & \text { Volume }=x^{2} \frac{3 h}{3} \\ & \text { Volume }=x^{2} h \end{aligned}$ | [1] Volume of larger pyramid |
|  | $\begin{gathered} \text { Volume }=\left(\frac{2 x}{3}\right)^{2} \times \frac{2 h}{3} \\ \text { Volume }=\frac{4 x^{2}}{9} \times \frac{2 h}{3}=\frac{8 x^{2} h}{27} \\ \text { Volume of water } \\ =\text { Larger Pyramid }- \text { Smaller Pyramid } \end{gathered}$ | [1] Volume of smaller pyramid |
|  | $\begin{aligned} & \text { Water volume }=x^{2} h-\frac{8 x^{2} h}{27}=\frac{19 x^{2} h}{27} \\ & \text { Proportion filled } \\ & =\text { Water volume } \div \text { Larger pyramid } \\ & \frac{19 x^{2} h}{27} \div x^{2} h \end{aligned}$ | [1] Smaller volume divided by larger volume |
|  | $\frac{19}{27}$ | [1] Correct answer simplified |
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