GCSE MATHEMATICS
AQA | Edexcel | OCR I WJEC

## Quadratics And Harder Graphs

Please write clearly in block capitals

Forename:

Surname:

## Materials

For this paper you must have:

- mathematical instruments

You can use a calculator.

## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

- The marks for questions are shown in brackets.
- You may ask for graph paper, tracing paper and more answer paper. These must be tagged securely to this answer book.


## Advice

- In all calculations, show clearly how you work out your answer.

1 Complete the table, and plot the graph of $y=x^{2}$ on the axes below.

| $\boldsymbol{x}$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{y}$ |  |  |  |  |  | 4 | 9 |



Turn over for next question

2 Plot the graph of $y=x^{3}-2 x$ for $-2 \leq x \leq 2$ on the axes below.

| $\boldsymbol{x}$ | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ |  |  |  |  |  |



Turn over for next question

3 On the axes below, plot the graphs of the quadratics for $-2 \leq x \leq 3$

$$
\begin{aligned}
& A: \quad y=x^{2}-1 \\
& B: y=x^{2}-x
\end{aligned}
$$

| $\mathbf{x}$ | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{y}$ |  |  |  |  |  |  |


| $\mathbf{x}$ | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ |  |  |  |  |  |  |


$4 \quad A$ is a cubic graph, $B$ is a reciprocal graph, their equations are shown below.

$$
\begin{gathered}
A: \quad y=x^{3}-1 \\
B: y=\frac{1}{x}
\end{gathered}
$$

4(a) Complete the table below showing the values of A for $-2 \leq x \leq 2$
[2 marks]

| $\boldsymbol{x}$ | -2 | -1 | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{y}$ |  |  |  |  |  |

4(b) Complete the table below showing the values of B for $-2 \leq x \leq 2$
[2 marks]

| $\boldsymbol{x}$ | -2 | -1 | -0.5 | -0.25 | 0 | 0.25 | 0.5 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ |  |  |  |  | Undefined |  |  |  |  |

$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Question continues on next page.

4(c) $\quad$ On the axes below, plot graph $A$ and graph $B$. Label your graphs.
[3 marks]


4(d) What are the approximate points of intersection of the two graphs?
$\qquad$
$\qquad$
Answer

Turn over for next question

5 The graph below shows the graph of,

$$
y=5^{x}
$$

5(a) Complete the table below showing the values of $y=2^{x}$ for $-2 \leq x \leq 3$
[2 marks]

| $\boldsymbol{x}$ | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{y}$ |  |  |  |  |  |  |

5(b) Plot $y=2^{x}$ on the axes below for the values of $-2 \leq x \leq 3$


5(c) Describe the differences between the two graphs, making sure to include reference to the shape of each curve and any points of intersection.
[3 marks]
$\qquad$
$\qquad$
Answer $\qquad$

Turn over for next question
6(a) What is the difference between a sketch and a plot of a graph?

7 Match the sketches of the six graphs below to the equations given.
One has been done for you.
A: $y=x^{3}+2 x^{2}$
B: $y=x^{3}$
$C: y=-x^{3}$
D: $y=x^{2}$
E: $y=x^{2}+2 x$
$F: \quad y=-x^{2}$
[5 marks]



D
$\square$





8 The grid below shows the graph of $N=A r^{t}$ which represents the number of bacteria in a sample ( $N$ ) over a period of time $(t)$. $A$ and $r$ are constants.


Use the graph to find the values of the constants $A$ and $r$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer $\qquad$

9 Match the sketches of the six graphs below to the equations given.
One has been done for you.
$A: y=\frac{1}{x}$
B: $y=-\frac{1}{x}$
C: $y=\frac{1}{10 x}$
D: $y=e^{x}$
E: $y=0.5^{x}$
$F: y=-e^{x}$






