

Write your name here	
Surname	Other names
Pearson Edexcel	Centre Number
Level 1/Level 2 GCSE (9-1)	Candidate Number
<h1 style="margin: 0;">Mathematics</h1> <h2 style="margin: 0;">Paper 1 (Non-Calculator)</h2>	
Higher Tier	
Thursday 2 November 2017 – Morning	Paper Reference
Time: 1 hour 30 minutes	1MA1/1H
You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser. Tracing paper may be used.	Total Marks <div style="border: 1px solid black; width: 50px; height: 50px; margin: 0 auto;"></div>

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **show all your working**.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- **Calculators may not be used.**



Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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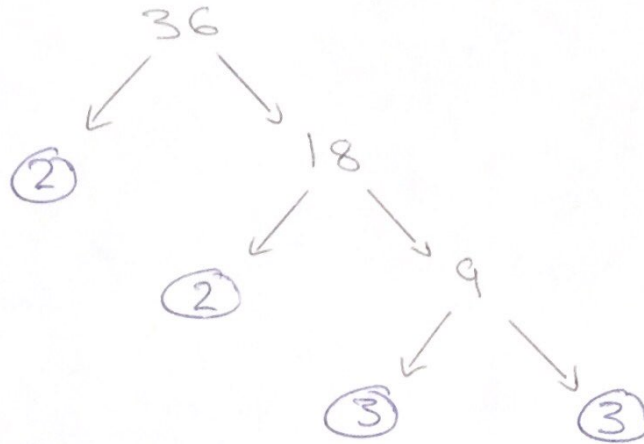

Pearson

Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

- 1 Write 36 as a product of its prime factors.



$$2 \times 2 \times 3 \times 3$$

(Total for Question 1 is 2 marks)

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- 2 Kiaria is 7 years older than Jay.
Martha is twice as old as Kiaria.
The sum of their three ages is 77

Find the ratio of Jay's age to Kiaria's age to Martha's age.

$$K = J + 7$$

$$M = 2K$$

$$J + K + M = 77$$

$$J + (J + 7) + 2(J + 7) = 77$$

$$4J + 21 = 77, \quad 4J = 56$$

$$J = 14$$

$$K = 14 + 7 = 21$$

$$M = 2(21) = 42$$

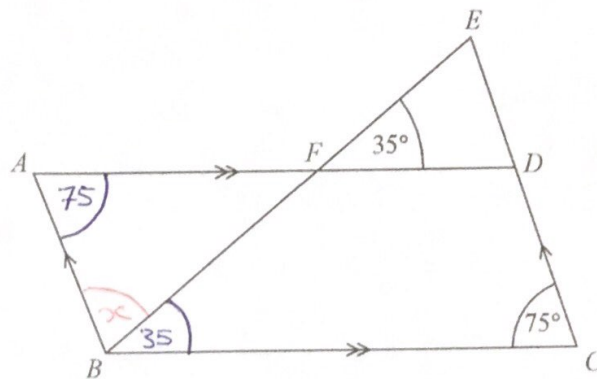
$$14 : 21 : 42$$

(Total for Question 2 is 4 marks)



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3



$ABCD$ is a parallelogram.

EDC is a straight line.

F is the point on AD so that BFE is a straight line.

Angle $EFD = 35^\circ$

Angle $DCB = 75^\circ$

Show that angle $ABF = 70^\circ$

Give a reason for each stage of your working.

$\angle FBC = 35^\circ$ as $EFD = FBC$
by corresponding angles

$\angle BAF = 75^\circ$ as $DCB = BAF$
as opposite angles in a
parallelogram are equal

\Rightarrow

$$\begin{aligned} x &= 180^\circ - 75^\circ - 35^\circ \\ &= 70^\circ \end{aligned}$$

as co-interior angles
sum to 180°

(Total for Question 3 is 4 marks)

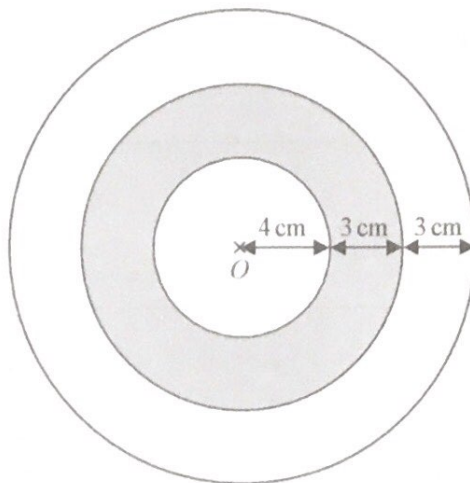
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- 4 The diagram shows a logo made from three circles.



Each circle has centre O .

Daisy says that exactly $\frac{1}{3}$ of the logo is shaded.

Is Daisy correct?

You must show all your working.

$$\text{Area} = \pi r^2$$

$$\text{Total Area} = \pi (10)^2 = 100\pi$$

$$\begin{aligned} \text{Shaded Area} &= \pi (7)^2 - \pi (4)^2 \\ &= 33\pi \end{aligned}$$

\Rightarrow Daisy is incorrect as

$$\begin{aligned} \frac{\text{Area of logo}}{\text{Shaded}} &= \frac{33\pi}{100\pi} = \frac{33}{100} \\ &\neq \frac{1}{3} \end{aligned}$$

(Total for Question 4 is 4 marks)

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P 4 9 3 0 8 A 0 5 2 0

- 5 The table shows information about the weekly earnings of 20 people who work in a shop.

Weekly earnings (£x)	Frequency
$150 < x \leq 250$	1
$250 < x \leq 350$	11
$350 < x \leq 450$	5
$450 < x \leq 550$	0
$550 < x \leq 650$	3

- (a) Work out an estimate for the mean of the weekly earnings.

$$fx = 1 \times 200, 11 \times 300, 5 \times 400 \\ 0 \times 500, 3 \times 600$$

$$\frac{\sum fx}{\sum f} = \frac{7300}{20} = 365$$

£ (3)

Nadiya says,

"The mean may **not** be the best average to use to represent this information."

- (b) Do you agree with Nadiya?

You must justify your answer.

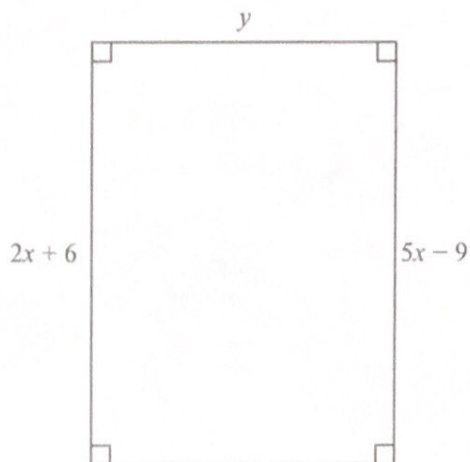
Yes as outliers will affect the mean value

(1)

(Total for Question 5 is 4 marks)



6 Here is a rectangle.



All measurements are in centimetres.

The area of the rectangle is 48 cm^2 .

Show that $y = 3$

$$2x + 6 = 5x - 9$$

$$\Rightarrow 3x = 15$$

$$x = 5$$

$$\therefore (2(5) + 6)y = 48$$

$$16y = 48$$

$$y = 3$$

(Total for Question 6 is 4 marks)

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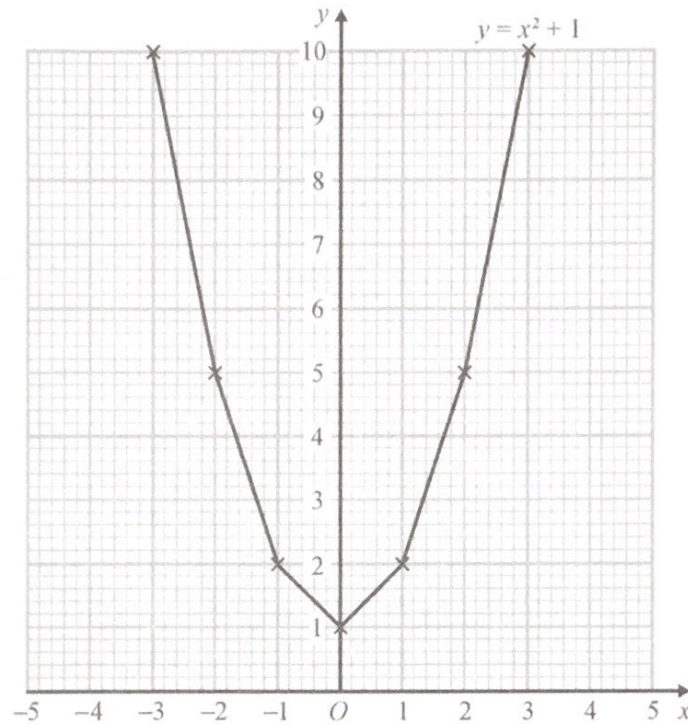
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- 7 Brogan needs to draw the graph of $y = x^2 + 1$
Here is her graph.



Write down one thing that is wrong with Brogan's graph.

$y = x^2 + 1$ should be drawn freehand
as a curve not individual line

(Total for Question 7 is 1 mark)

segments that connects each
of the points

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- 8 Write these numbers in order of size.
Start with the smallest number.

$$0.2\dot{4}\dot{6} = 0.24666... \quad 0.24\dot{6} = 0.246246... \quad 0.\dot{2}4\dot{6} = 0.246246... \quad 0.246$$

$$0.246, 0.\dot{2}4\dot{6}, 0.24\dot{6}, 0.2\dot{4}\dot{6}$$

(Total for Question 8 is 2 marks)

- 9 James and Peter cycled along the same 50 km route.

James took $2\frac{1}{2}$ hours to cycle the 50 km.

$$\text{Speed} = \frac{\text{distance}}{\text{time}}$$

Peter started to cycle 5 minutes after James started to cycle.

Peter caught up with James when they had both cycled 15 km.

James and Peter both cycled at constant speeds.

Work out Peter's speed.

$$J \text{ speed} = \frac{50}{2.5} = 20 \text{ kph}$$

$$J \text{ time @ 15 km} = \frac{15}{20} = 0.75 = 45 \text{ mins}$$

$$\text{Peter time } 45 - 5 = 40 \text{ mins}$$

$$P \text{ speed} = \frac{15}{40/60} = 22.5$$

km/h

(Total for Question 9 is 5 marks)



P 4 9 3 0 8 A 0 9 2 0

- 10 (a) Write down the value of $100^{\frac{1}{2}}$

$$\sqrt{100}$$

$$\pm 10$$

(1)

- (b) Find the value of $125^{\frac{2}{3}}$

$$(\sqrt[3]{125})^2 = 5^2 = 25$$

(2)

(Total for Question 10 is 3 marks)

- 11 3 teas and 2 coffees have a total cost of £7.80
5 teas and 4 coffees have a total cost of £14.20

Work out the cost of one tea and the cost of one coffee.

$$3t + 2c = 7.80 \quad (\times 2)$$

$$5t + 4c = 14.20$$

$$6t + 4c = 15.60$$

$$5t + 4c = 14.20$$

$$\Rightarrow \underline{t = £1.40}$$

$$\Rightarrow 3(1.40) + 2c = 7.80$$

$$\Rightarrow \underline{c = £1.80}$$

tea £

coffee £

(Total for Question 11 is 4 marks)



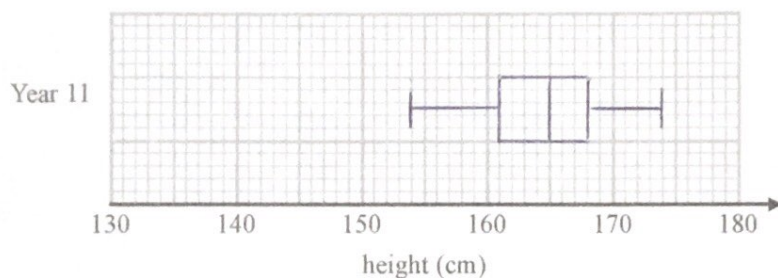
12 The table shows information about the heights, in cm, of a group of Year 11 girls.

	height (cm)
least height	154
median	165
lower quartile	161
interquartile range	7
range	20

$$161 + 7 = \text{UQ}$$

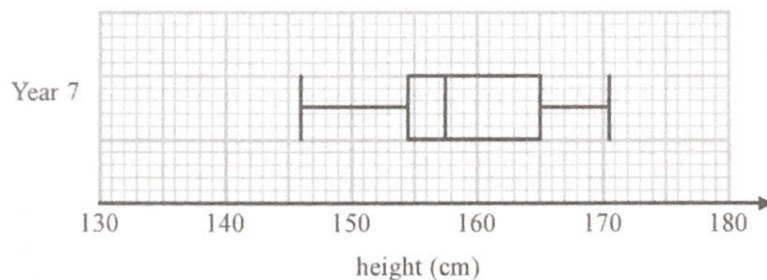
(a) Draw a box plot for this information.

$$\text{max height} = 154 + 20$$



(3)

The box plot below shows information about the heights, in cm, of a group of Year 7 girls.



(b) Compare the distribution of heights of the Year 7 girls with the distribution of heights of the Year 11 girls.

- lower median 157.5 vs 165
- larger range 24.5 vs 20

(2)

(Total for Question 12 is 5 marks)



P 4 9 3 0 8 A 0 1 1 2 0

- 13 A factory makes 450 pies every day.
The pies are chicken pies or steak pies.

Each day Milo takes a sample of 15 pies to check.

The proportion of the pies in his sample that are chicken is the same as the proportion of the pies made that day that are chicken.

On Monday Milo calculated that he needed exactly 4 chicken pies in his sample.

- (a) Work out the total number of chicken pies that were made on Monday.

$$\frac{4}{15} \times 450 = \underline{120}$$

(2)

On Tuesday, the number of steak pies Milo needs in his sample is 6 correct to the nearest whole number.

Milo takes at random a pie from the 450 pies made on Tuesday.

- (b) Work out the lower bound of the probability that the pie is a steak pie.

$$\frac{5}{15} \times 450 = 150 \quad \frac{6}{15} \times 450 = 180$$

mid point

$$\frac{165}{450}$$

(2)

(Total for Question 13 is 4 marks)

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14 The ratio $(y+x):(y-x)$ is equivalent to $k:1$

Show that $y = \frac{x(k+1)}{k-1}$

$$y + x = k(y - x)$$

$$ky - y = x + kx$$

$$y = \frac{x(k+1)}{(k-1)}$$

(Total for Question 14 is 3 marks)

15 $x = 0.4\dot{3}\dot{6}$

Prove algebraically that x can be written as $\frac{24}{55}$

$$1000x = 436.\dot{3}\dot{6}$$

$$10x = 4.\dot{3}\dot{6}$$

$$1000x - 10x = 432$$

$$990x = 432$$

$$x = \frac{432}{990} = \frac{24}{55}$$

(Total for Question 15 is 3 marks)



16 y is directly proportional to $\sqrt[3]{x}$

$$y = 1\frac{1}{6} \text{ when } x = 8$$

Find the value of y when $x = 64$

$$y \propto \sqrt[3]{x}, \quad y = K\sqrt[3]{x}$$

$$@ \ x=8, \ y=1\frac{1}{6}, \quad \frac{7}{6} = 2K \Rightarrow K = \frac{7}{12}$$

when $x=64$

$$y = \frac{7}{12} \times \sqrt[3]{64} = \frac{7}{12} \times 4 = \frac{7}{3}$$

(Total for Question 16 is 3 marks)

17 n is an integer.

Prove algebraically that the sum of $\frac{1}{2}n(n+1)$ and $\frac{1}{2}(n+1)(n+2)$ is always a square number.

expanding and adding

$$\frac{1}{2}(n^2 + n + n^2 + 3n + 2)$$

$$= \frac{1}{2}(2n^2 + 4n + 2)$$

$$= (n^2 + 2n + 1)$$

$$= (n+1)^2$$

which is a square number for all values of n .

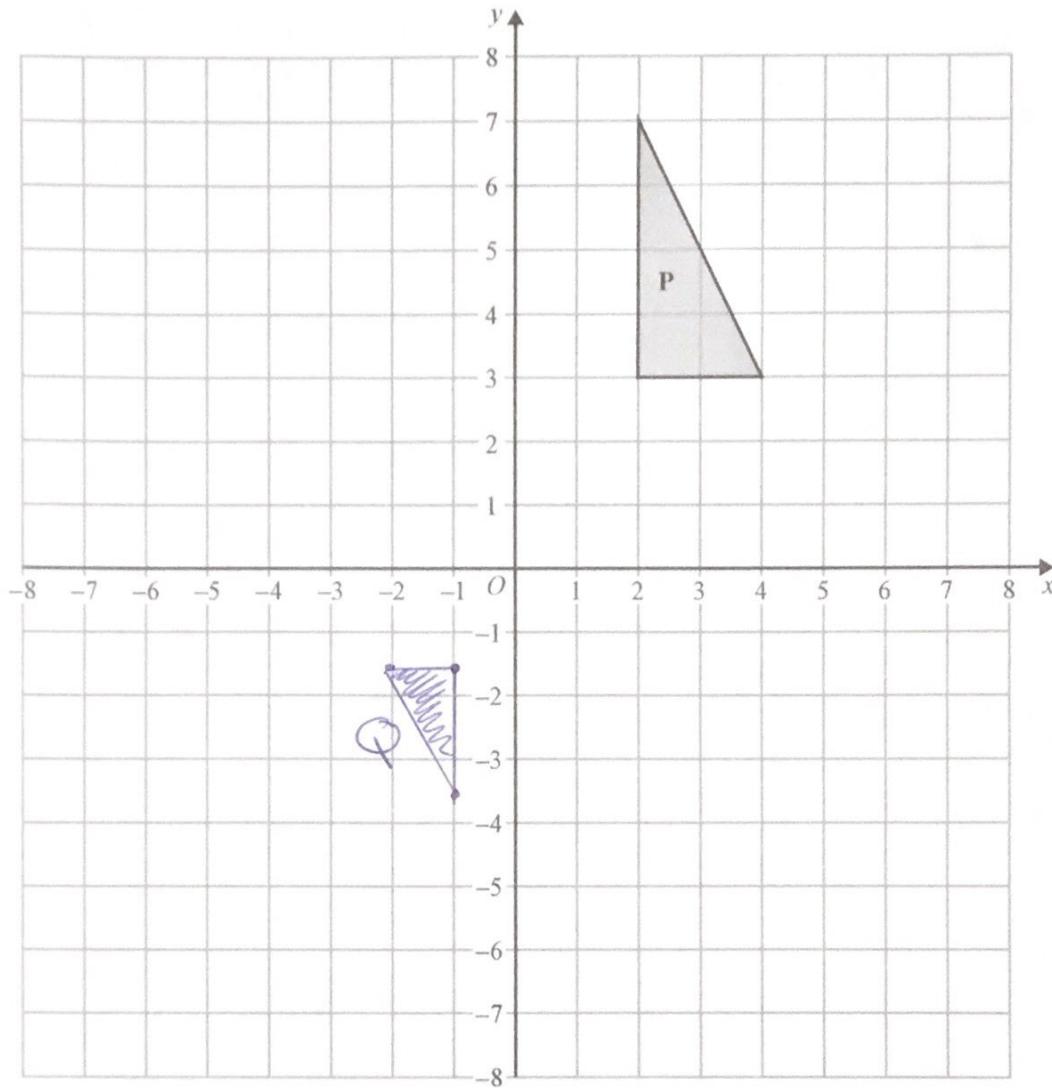
(Total for Question 17 is 2 marks)

18

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Enlarge shape **P** by scale factor $-\frac{1}{2}$ with centre of enlargement $(0, 0)$.

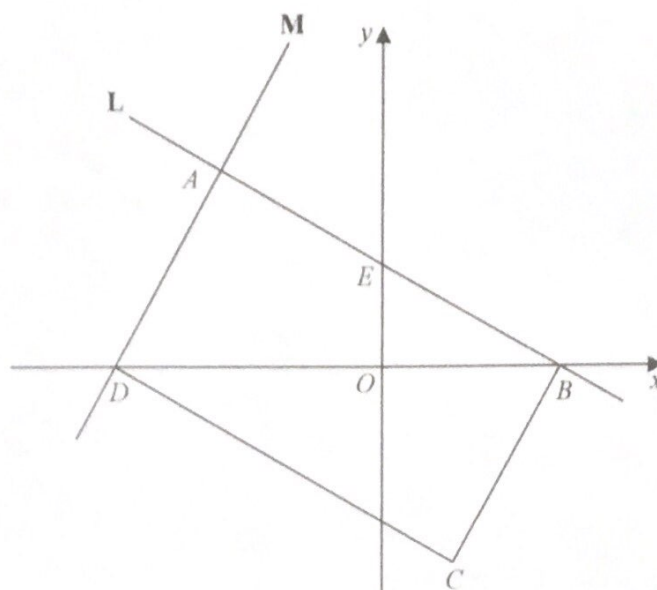
Label your image **Q**.

(Total for Question 18 is 2 marks)



P 4 9 3 0 8 A 0 1 5 2 0

19



$ABCD$ is a rectangle.

A , E and B are points on the straight line L with equation $x + 2y = 12$

A and D are points on the straight line M .

$AE = EB$

Find an equation for M .

for L $y = -\frac{1}{2}x + 6$

so $\frac{\Delta y}{\Delta x}$ of M is $2x$ $\left(\frac{-1}{m}\right)$

$E(0, 6)$ $B(12, 0) \Rightarrow A(-12, 12)$

$y = 2x + c$ @ A

$\Rightarrow 12 = 2(-12) + c$

$\Rightarrow c = 36$

$y = 2x + 36$

(Total for Question 19 is 4 marks)



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20 The table shows some values of x and y that satisfy the equation $y = a \cos x^\circ + b$

x	0	30	60	90	120	150	180
y	3	$1 + \sqrt{3}$	2	1	0	$1 - \sqrt{3}$	-1

Find the value of y when $x = 45$

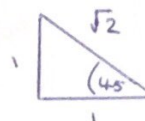
$$\cos(90) = 0 \Rightarrow b = 1$$

$$\cos(0) = 1 \Rightarrow 3 = a(1) + 1$$

$$\Rightarrow a = 2$$

$$y = 2 \times \frac{\sqrt{2}}{2} + 1$$

$$y = 1 + \sqrt{2}$$



$$\cos = \frac{A}{H} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$

(Total for Question 20 is 4 marks)

21 Show that $\frac{6 - \sqrt{8}}{\sqrt{2} - 1}$ can be written in the form $a + b\sqrt{2}$ where a and b are integers.

$$\frac{6 - \sqrt{8}}{\sqrt{2} - 1} \times \frac{\sqrt{2} + 1}{\sqrt{2} + 1} = \frac{6\sqrt{2} + 6 - \sqrt{8}\sqrt{2} - \sqrt{8}}{2 - 1}$$

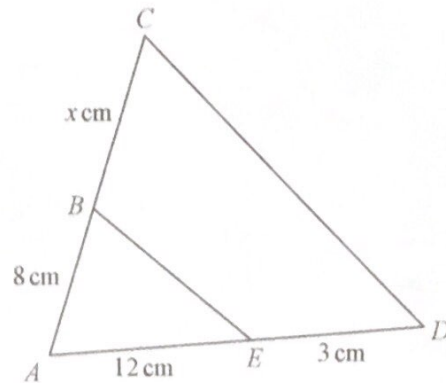
$$\Rightarrow 6\sqrt{2} + 6 - 4 - 2\sqrt{2}$$

$$= 2 + 4\sqrt{2}$$

(Total for Question 21 is 3 marks)



22 The two triangles in the diagram are similar.



There are two possible values of x .

Work out each of these values.

State any assumptions you make in your working.

$$AD \text{ scale factor } \frac{12}{3}$$

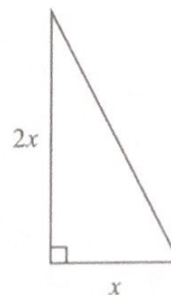
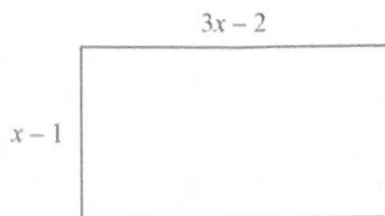
$$\Rightarrow x = 8 \times \frac{3}{12} = 2 \text{ cm}$$

$$\text{or } \frac{15}{8} \times 12 - 8, x = 14.5$$

(Total for Question 22 is 5 marks)



23 Here is a rectangle and a right-angled triangle.



All measurements are in centimetres.

The area of the rectangle is greater than the area of the triangle.

Find the set of possible values of x .

$$\begin{aligned} \text{Areas : } (3x-2)(x-1) & , \quad \frac{1}{2}(2x \times x) \\ & = 3x^2 - 5x + 2 & , \quad x^2 \end{aligned}$$

so condition is

$$3x^2 - 5x + 2 > x^2$$

$$\Rightarrow 2x^2 - 5x + 2 > 0$$

i.e. $ax^2 - bx + c > 0$
to solve

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{5 \pm \sqrt{25 - 16}}{4}$$

$$x = \frac{5 \pm 3}{4} \quad x = \frac{5+3}{4} = 2 \quad \text{so } x > 2$$

other

(Total for Question 23 is 5 marks)
result is non physical so has to be (+)

TOTAL FOR PAPER IS 80 MARKS



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