



A Level Further Mathematics B (MEI) Y435 Extra Pure

Sample Question Paper

Date - Morning/Afternoon

Time allowed: 1 hour 15 minutes

OCR supplied materials:

- Printed Answer Booklet
- · Formulae Further Mathematics B (MEI)

You must have:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)
- · Scientific or graphical calculator



INSTRUCTIONS

- · Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer all the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet.
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION

- The total number of marks for this paper is 60.
- The marks for each question are shown in brackets [].
- You are advised that an answer may receive no marks unless you show sufficient detail of the
 working to indicate that a correct method is used. You should communicate your method with
 correct reasoning.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 4 pages.

Answer all the questions.

- The set $G = \{1, 4, 5, 6, 7, 9, 11, 16, 17\}$ is a group of order 9 under the binary operation of multiplication modulo 19.
 - (i) Show that *G* is a cyclic group generated by the element 4. [3]
 - (ii) Find another generator for G. Justify your answer. [2]
 - (iii) Specify two distinct isomorphisms from the group $J = \{0, 1, 2, 3, 4, 5, 6, 7, 8\}$ under addition modulo 9 to G. [5]
- A binary operation * is defined on the set $S = \{p, q, r, s, t\}$ by the following composition table.

Determine whether (S, *) is a group.

[4]

3 (i) Find the general solution of

$$u_n = 8u_{n-1} - 16u_{n-2}, \ n \ge 2.$$
 (*)

A new sequence v_n is defined by $v_n = \frac{u_n}{u_{n-1}}$ for $n \ge 1$.

(ii) (A) Use (*) to show that
$$v_n = 8 - \frac{16}{v_{n-1}}$$
 for $n \ge 2$. [2]

- (B) Deduce that if v_n tends to a limit then it must be 4. [2]
- (iii) Use your general solution in part (i) to show that $\lim_{n\to\infty} v_n = 4$. [3]
- (iv) Deduce the value of $\lim_{n\to\infty} \left(\frac{u_n}{u_{n-2}}\right)$. [1]

A surface S has equation g(x, y, z) = 0, where $g(x, y, z) = (y - 2x)(y + z)^2 - 18$.

(i) Show that
$$\frac{\partial g}{\partial y} = (y+z)(-4x+3y+z)$$
. [2]

(ii) Show that
$$\frac{\partial g}{\partial x} + 2 \frac{\partial g}{\partial y} - 2 \frac{\partial g}{\partial z} = 0$$
. [4]

- (iii) Hence identify a vector which lies in the tangent plane of every point on S, explaining your reasoning. [3]
- (iv) Find the cartesian equation of the tangent plane to the surface S at the point P(1, 4, -7). [3]

The tangent plane to the surface S at the point Q(0, 2, 1) has equation 6x - 7y - 4z = -18.

- (v) Find a vector equation for the line of intersection of the tangent planes at P and Q. [4]
- 5 In this question you must show detailed reasoning.

You are given that the matrix $\mathbf{M} = \begin{pmatrix} \frac{1}{2} & -\frac{1}{\sqrt{2}} & \frac{1}{2} \\ \frac{1}{\sqrt{2}} & 0 & -\frac{1}{\sqrt{2}} \\ \frac{1}{2} & \frac{1}{\sqrt{2}} & \frac{1}{2} \end{pmatrix}$ represents a rotation in 3-D space.

- (i) Explain why it follows that **M** has 1 as an eigenvalue. [2]
- (ii) Find a vector equation for the axis of the rotation. [4]
- (iii) Show that the characteristic equation of \mathbf{M} can be written as

$$\lambda^3 - \lambda^2 + \lambda - 1 = 0.$$
 [5]

- (iv) Find the smallest positive integer n such that $\mathbf{M}^n = \mathbf{I}$. [6]
- (v) Find the magnitude of the angle of the rotation which M represents. Give your reasoning. [1]

END OF QUESTION PAPER



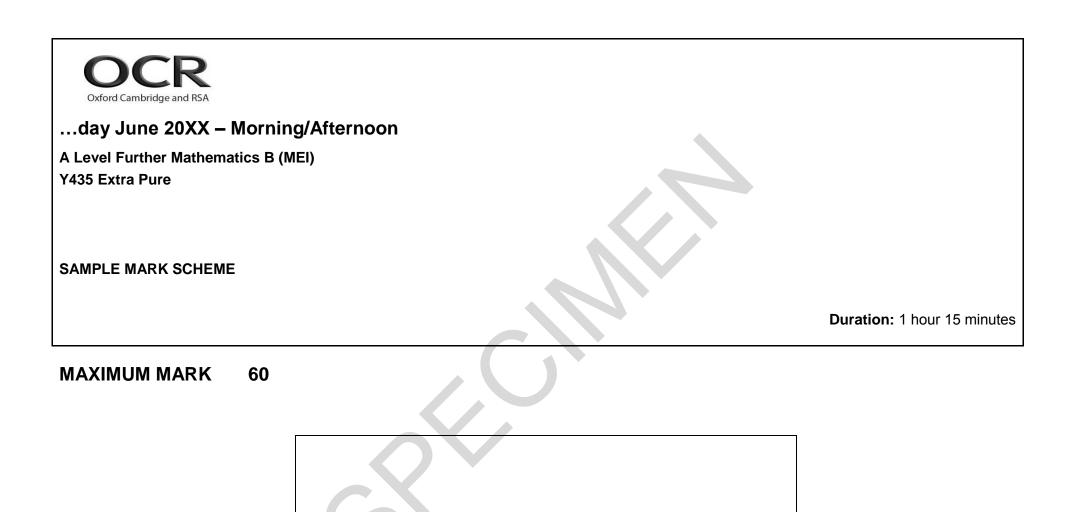
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This document consists of 16 pages

Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
√and x	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
Highlighting	
Other abbreviations in	Meaning
mark scheme	
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By calculator
DR	This indicates that the instruction In this question you must show detailed reasoning appears in the question.

2. Subject-specific Marking Instructions for A Level Further Mathematics B (MEI)

- Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

 If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

М

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

 Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for g. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.
- k Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned on this occasion, but shows what a complete solution might look like

	Quest	tion	Answer	Marks	AOs	Guidance
1	(i)		Order of <i>G</i> is 9, so 4 has order [1,] 3 or 9. $4^1 = 4, 4^3 = 7$ $4^9 = 7^3 = 1$	E1 M1	2.1 1.1	Use of modulo arithmetic
			So 4 has order 9 and G is a cyclic group generated by 4.	A1	1.1	
			Alternative Method n 1 2 3 4 5 6 7 8 9 4^n 4 16 7 9 17 11 6 5 1 4 has order 9 and generates G so G is a cyclic group generated by the element 4	M1 A1 E1 [3]		Attempt Correct
1	(ii)		One of 16, 9, 17, 6, 5 Appropriate reason e.g. $5 = 4^{-1}$, reference to table if given in (i).	B1 E1 [2]	1.1 2.4	
1	(iii)		In <i>J</i> , elements of order 9 are 1, 2, 4, 5, 7 and 8.	M1	3.1a	For naming two
			4 must correspond to an element of order 9. n		2.4 1.1	First isomorphism has five correct correspondences First isomorphism correct
				A1 [5]	2.1	Second isomorphism correct

	Questio	n Answer	Marks	AOs	Guidance
2	If it has an identity, then it is p, since $p * x = x * p = x$ for all $x \in S$.		B1	1.1	
		Leading diagonal shows that $x*x = p$ for all $x \in S$, so all elements have order 2.	E1	3.1a	Only need to note this for one element
					other than p.
		But 2 is not a factor of 5, the order of S, so this breaks Lagrange.	E1	2.4	
		So not a group	E 1	1.2	
		Alternative method			
		Attempt to look at associativity	M1		
		(q*r)*t = s*t = q	E1		
		q*(r*t) = q*s = t	E1		
		Not associative so not a group	E1		
			[4]		If not complete argument can score SC1 for attempting to check 2 axioms, SC2 for attempting to check 4
3	(i)	$u_n - 8u_{n-1} + 16u_{n-2} = 0$			
		Auxiliary equation: $\lambda^2 - 8\lambda + 16 = 0$	M1	1.1a	
		$(\lambda - 4)^2 = 0$ repeated root $\lambda = 4$	A1	1.1	Or BC
		$u_n = (A + Bn)4^n$	M1	1.1	
			A1 [4]	1.1	

	Quest	tion	Answer	Marks	AOs	Guidance
3	(ii)	(A)	$u_n = 8u_{n-1} - 16u_{n-2}, \ n \ge 2$			
			$\frac{u_n}{u_n} - 8 - 16 \frac{u_{n-2}}{u_{n-2}}$	M1	1.1	
			$\frac{u_n}{u_{n-1}} = 8 - 16 \frac{u_{n-2}}{u_{n-1}}$			
			$\frac{u_n}{u_n} = v$ and $\frac{u_{n-2}}{u_{n-2}} = \frac{1}{u_{n-2}}$			
			$\frac{u_n}{u_{n-1}} = v_n$ and $\frac{u_{n-2}}{u_{n-1}} = \frac{1}{v_{n-1}}$			
			$\Rightarrow v_n = 8 - \frac{16}{v_{n-1}} AG$	E 1	3.1a	
			v_{n-1}	[2]		
				[2]		
3	(ii)	(B)	If v_n tends to a limit μ then $\mu = 8 - \frac{16}{\mu}$.	M1	2.2a	
			If v_n tends to a limit μ then $\mu = 8 - \frac{1}{\mu}$.			
			$\Rightarrow \mu^2 - 8\mu + 16 = 0$			
			which has only one root, 4.			
			So if v_n tends to a limit then it must be 4.	E 1	1.1	Uniqueness must be
				[2]		shown
3	(iii)			[2] M1	3.1a	
3	(111)		$v_n = \frac{u_n}{u_{n-1}} = \frac{(A+Bn)4^n}{(A+B(n-1))4^{n-1}}$	IVII	3.1a	
			$=\frac{(\frac{A}{n}+B)4}{(\frac{A}{n}+B-\frac{B}{n})}$	A1	1.1	
			$(\frac{A}{n} + B - \frac{B}{n})$			
			$\rightarrow \frac{4B}{B}$ as $n \rightarrow \infty$	A1	2.2a	Must be convincing
			= 4 AG			
				[3]		
3	(iv)		$4^2 = 16$	B1	2.2a	
				[1]		

	Questi	ion	Answer	Marks	AOs	Guidance
4	(i)		$\frac{\partial g}{\partial y} = (y - 2x)2(y + z) + (y + z)^2$	M1	1.1a	Attempt at differentiation, treating x and z as constants
			= (y+z)(2y-4x+y+z) = (y+z)(-4x+3y+z) AG	A1 [2]	1.1	
4	(ii)		$\frac{\partial g}{\partial x} = -2(y+z)^2$ $\frac{\partial g}{\partial z} = 2(y-2x)(y+z)$ $\frac{\partial g}{\partial x} + 2\frac{\partial g}{\partial y} - 2\frac{\partial g}{\partial z}$ $= -2(y+z)^2 + 2(y+z)(-4x+3y+z) - 4(y-2x)(y+z)$	B1 B1	1.1a 1.1	
			= 2(y+z)(-y-z-4x+3y+z-2y+4x) = 0 AG	M1 A1 [4]	1.1 2.1	Some simplification

	Quest	tion	Answer	Marks	AOs	Guidance
4	(iii)		$ \begin{pmatrix} \frac{\partial \mathbf{g}}{\partial x} \\ \frac{\partial \mathbf{g}}{\partial y} \\ \frac{\partial \mathbf{g}}{\partial z} \end{pmatrix} $ is normal vector for tangent plane	E1	3.1a	
			$\begin{pmatrix} \frac{\partial g}{\partial x} \\ \frac{\partial g}{\partial y} \\ \frac{\partial g}{\partial z} \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 2 \\ -2 \end{pmatrix} = 0 \text{ for every point on S}$ $\begin{pmatrix} 1 \\ 2 \\ \text{lies in tangent plane of every point on S}$	E1	2.4 2.2a	
			(-2)	[3]		
4	(iv)		At P, $\begin{pmatrix} \frac{\partial g}{\partial x} \\ \frac{\partial g}{\partial y} \\ \frac{\partial g}{\partial z} \end{pmatrix} = \begin{pmatrix} -18 \\ -3 \\ -12 \end{pmatrix}$	M1	1.1	At least one correct, or clear attempt to use formulae from (i), (ii) or redone here
			Use of scalar product with correct vector. $6x + y + 4z = -18$	M1 A1 [3]	1.1 1.1	oe

	Quest	tion	Answer	Marks	AOs	Guidance
4	_		$8y + 8z = 0$ $(-3, 0, 0)$ $\begin{pmatrix} 1 \end{pmatrix}$	M1 A1 M1	3.1a 1.1 3.1a	Dealing with planes as simultaneous equations to find equation of a common point Finding a common point
			$\begin{vmatrix} 2 \\ -2 \end{vmatrix}$ in both planes, so is direction vector for line of intersection $\mathbf{r} = \begin{pmatrix} -3 \\ 0 \\ 0 \end{pmatrix} + t \begin{pmatrix} 1 \\ 2 \\ -2 \end{pmatrix}$	A1 [4]	2.2a	
5	(i)		A rotation has an axis and this is a line of invariant points.	E1	1.2	The second of these can be implied
			The direction vector of this line/axis has associated eigenvalue 1.	E1 [2]	2.2a	

	Quest	tion	Answer	Marks	AOs	Guidance
5	(ii)		DR $ \begin{pmatrix} \frac{1}{2} & -\frac{1}{\sqrt{2}} & \frac{1}{2} \\ \frac{1}{\sqrt{2}} & 0 & -\frac{1}{\sqrt{2}} \\ \frac{1}{2} & \frac{1}{\sqrt{2}} & \frac{1}{2} \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} x \\ y \\ z \end{pmatrix} $ $ \frac{1}{2}x - \frac{1}{\sqrt{2}}y + \frac{1}{2}z = x $ $ \frac{1}{\sqrt{2}}x & -\frac{1}{\sqrt{2}}z = y $ $ \frac{1}{2}x + \frac{1}{\sqrt{2}}y + \frac{1}{2}z = z $ Simplifying algebra which eliminates one variable	M1 M1	3.1a 1.1	For any two correct equations May be awarded for starting with $\begin{pmatrix} 1 \\ y \\ z \end{pmatrix}$.
			Eigenvector $\begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$. Axis of rotation $\mathbf{r} = t \begin{pmatrix} 1 \\ 0 \end{pmatrix}$	A1	1.1 3.2a	Or any multiple oe
			Axis of rotation $1-t \begin{pmatrix} 0 \\ 1 \end{pmatrix}$	[4]		

Question	Answer Mar			Guidance
5 (iii)	DR	M1	1.1	
	$\begin{vmatrix} \frac{1}{2} - \lambda & -\frac{1}{\sqrt{2}} & \frac{1}{2} \\ \frac{1}{\sqrt{2}} & -\lambda & -\frac{1}{\sqrt{2}} \end{vmatrix} = 0$			
	$\begin{vmatrix} \frac{1}{\sqrt{5}} & -\lambda & -\frac{1}{\sqrt{5}} \end{vmatrix} = 0$			
	$\begin{vmatrix} \frac{1}{\sqrt{2}} & -\lambda & -\frac{1}{\sqrt{2}} \\ \frac{1}{2} & \frac{1}{\sqrt{2}} & \frac{1}{2} - \lambda \end{vmatrix} = 0$			
		3.54		
	$\frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} \left(\frac{1}{2} - \lambda \right) + \frac{1}{2} \frac{1}{\sqrt{2}} \right)$	M1	1.1	This expands on middle column; any
	$-\lambda \left(\left(\frac{1}{2} - \lambda \right)^2 - \frac{1}{4} \right)$			other column or row
				acceptable.
	$-\frac{1}{\sqrt{2}} \left(-\frac{1}{\sqrt{2}} \left(\frac{1}{2} - \lambda \right) - \frac{1}{2} \frac{1}{\sqrt{2}} \right) = 0$			Condone missing =0.
		M1	1.1a	Correct one line
	$\frac{1}{2} - \frac{1}{2}\lambda$	A1	1.1	All correct
	$+\lambda^2 - \lambda^3$			
	$+\frac{1}{2}-\frac{1}{2}\lambda=0$			
	$-\lambda^3 + \lambda^2 - \lambda + 1 = 0$	A1	2.1	Answer given; must
	So $\lambda^3 - \lambda^2 + \lambda - 1 = 0$			follow from previous working.
		[5]		

	Question Answer		Marks	AOs	Guidar	ice			
5	(iv)		DR	B1	3.1a	Showing $\mathbf{M}^2 \neq \mathbf{I}$	(0	0	1)
			$\left(\begin{array}{cccc} \frac{1}{2} & -\frac{1}{\sqrt{D}} & \frac{1}{2} \end{array}\right) \left(\begin{array}{cccc} \frac{1}{2} & -\frac{1}{\sqrt{D}} & \frac{1}{2} \end{array}\right)$				$\mathbf{M}^2 = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$	-1	0
			$\mathbf{M}^2 = \begin{vmatrix} \frac{1}{5} & 0 & -\frac{1}{5} \end{vmatrix} \begin{vmatrix} \frac{1}{5} & 0 & -\frac{1}{5} \end{vmatrix}$				1	0	0
			$\mathbf{M}^{2} = \begin{pmatrix} \frac{1}{2} & -\frac{1}{\sqrt{2}} & \frac{1}{2} \\ \frac{1}{\sqrt{2}} & 0 & -\frac{1}{\sqrt{2}} \\ \frac{1}{2} & \frac{1}{\sqrt{2}} & \frac{1}{2} \end{pmatrix} \begin{pmatrix} \frac{1}{2} & -\frac{1}{\sqrt{2}} & \frac{1}{2} \\ \frac{1}{\sqrt{2}} & 0 & -\frac{1}{\sqrt{2}} \\ \frac{1}{2} & \frac{1}{\sqrt{2}} & \frac{1}{2} \end{pmatrix}$				`		
			$\begin{pmatrix} 2 & \sqrt{2} & 2 \end{pmatrix} \begin{pmatrix} 2 & \sqrt{2} & 2 \end{pmatrix}$						
			$= \begin{pmatrix} & -1 & \\ & \neq \mathbf{I} \end{pmatrix}$						
				7.51					
			$\mathbf{M}^3 = \mathbf{M}^2 - \mathbf{M} + \mathbf{I}$ (Cayley-Hamilton theorem)	M1	2.4				
			So $\mathbf{M}^3 \neq \mathbf{I}$ because $\mathbf{M}^2 \neq \mathbf{M}$ from above	A1	2.2a				
			Alternative method						
				M1		Or convincing			
			$\mathbf{M}^3 = \begin{bmatrix} -1 & -1 & 0 & +\mathbf{I} = \end{bmatrix} 0 \neq \mathbf{I}$	A1		multiplication			
			$\mathbf{M}^3 = \begin{pmatrix} & & \\ & -1 & \\ & & \end{pmatrix} - \begin{pmatrix} & & \\ & & \\ & & \end{pmatrix} + \mathbf{I} = \begin{pmatrix} & & \\ & & \\ & & \end{pmatrix} \neq \mathbf{I}$			showing $\mathbf{M}^3 \neq \mathbf{I}$.			
			$\mathbf{M}^4 = \mathbf{M}^3 - \mathbf{M}^2 + \mathbf{M}$	M1	1.1				
			$= \mathbf{M}^2 - \mathbf{M} - \mathbf{M}^2 + \mathbf{M} = \mathbf{I}$	A1	2.1	Or convincing			
						multiplication.			
			So $n=4$	A1	3.2a				
				[6]					
5	(v)		$\frac{\pi}{2}$ because 4 applications of the transformation gets back to starting point	E 1	2.2a	90°			
			2		2.24				
				[1]					

Question	AO1	AO2	AO3(PS)	AO3(M)	Totals
1i	2	1	0	0	3
1ii	1	1	0	0	2
1iii	2	2	1	0	5
2	2	1	1	0	4
3i	4	0	0	0	4
3iiA	1	0	1	0	2
3iiB	1	1	0	0	2
3iii	1	1	1	0	3
3iv	0	1	0	0	1
4i	2	0	0	0	2
4ii	3	1	0	0	4
4iii	0	2	1	0	3
4iv	3	0	0	0	3
4v	1	1	2	0	4
5i	1	1	0	0	2
5ii	2	0	2	0	4
5iii	4	1	0	0	5
5iv	1	3	2	0	6
5v	0	1	0	0	1
Totals	31	18	11	0	60

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A Level Further Mathematics B (MEI) Y435 Extra Pure

Printed Answer Booklet

Date - Morning/Afternoon

Time allowed: 1 hour 15 minutes

OCR supplied materials:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)

You must have:

- · Printed Answer Booklet
- Formulae Further Mathematics B (MEI)
- · Scientific or graphical calculator



First name	
Last name	
Centre number	Candidate number

INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- · Answer all the questions.
- · Write your answer to each question in the space provided in the Printed Answer Booklet.
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION

- You are advised that an answer may receive no marks unless you show sufficient detail of the
 working to indicate that a correct method is used. You should communicate your method with
 correct reasoning.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 4 pages.

1 (i)	
1 (ii)	
1 (iii)	

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3 (i)	
3 (ii) (A)	
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3 (ii) (B)	
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3 (iii)	
3 (iv)	
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4 (i)	
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4 (iii)	
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5 (i)	
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5 (iii)	

5 (iv)	
5 (v)	





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