



AS Level Further Mathematics A Y534 Discrete Mathematics

Sample Question Paper

Date - Morning/Afternoon

Time allowed: 1 hour 15 minutes

OCR supplied materials:

- Printed Answer Booklet
- · Formulae AS Level Further Mathematics A

You must have:

- · Printed Answer Booklet
- · Formulae AS Level Further Mathematics A
- Scientific or graphical calculator



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INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer all the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet.
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by $g \, \text{m} \, \text{s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use g = 9.8.

INFORMATION

- The total number of marks for this paper is 60.
- The marks for each question are shown in brackets [].
- You are reminded of the need for clear presentation in your answers.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 8 pages.

Answer all the questions.

- Hussain wants to travel by train from Edinburgh to Southampton, leaving Edinburgh after 9 am and arriving in Southampton by 4 pm. He wants to leave Edinburgh as late as possible.

 Hussain rings the train company to find out about the train times. Write down a question he might ask that leads to
 - (A) an existence problem,
 - (B) an optimisation problem.

[2]

- 2 Some of the activities that may be involved in making a cup of tea are listed below.
 - A: Boil water.
 - B: Put teabag in teapot, pour on boiled water and let tea brew.
 - C: Get cup from cupboard.
 - D: Pour tea into cup.
 - E: Add milk to cup.
 - F: Add sugar to cup.

Activity A must happen before activity B.

Activities B and C must happen before activity D.

Activities E and F cannot happen until after activity C.

Other than that, the activities can happen in any order.

- (i) Lisa does not take milk or sugar in her tea, so she only needs to use activities A, B, C and D. In how many different orders can activities A, B, C and D be arranged, subject to the restrictions above? [1]
- (ii) Mick takes milk but no sugar, so he needs to use activities A, B, C, D and E. Explain carefully why there are exactly nine different orders for these activities, subject to the restrictions above. [3]
- (iii) Find the number of different orders for all six activities, subject to the restrictions above. Explain your reasoning carefully. [3]
- 3 A zero-sum game is being played between two players, *X* and *Y*. The pay-off matrix for *X* is given below.

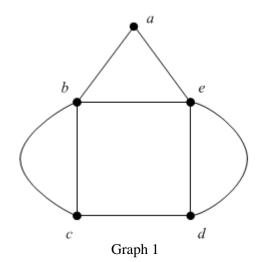
		Player Y		
		Strategy R	Strategy S	
	Strategy P	4	-2	
Player X	Strategy Q	-3	1	

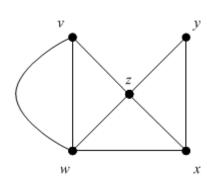
(i) Find an optimal mixed strategy for player *X*.

[5]

(ii) Give one assumption that must be made about the behaviour of *Y* in order to make the mixed strategy of Player *X* valid. [1]

4 Two graphs are shown below. Each has exactly five vertices with vertex orders 2, 3, 3, 4, 4.





Graph 2

(i) Write down a semi-Eulerian route for graph 1.

[1]

(ii) Explain how the vertex orders show that graph 2 is also semi-Eulerian.

- [1]
- (iii) By referring to specific vertices, explain how you know that these graphs are not simple.
- [2]

[2]

- (iv) By referring to specific vertices, explain how you know that these graphs are not isomorphic.
- 5 There are three non-isomorphic trees on five vertices.
 - (i) Draw an example of each of these trees.

[1]

[3]

[2]

- (ii) State three properties that must be satisfied by the vertex orders of a tree on six vertices.
- (iii) List the five different sets of possible vertex orders for trees on six vertices.
- [2]

(iv) Draw an example of each type listed in part (iii).

6	The following	masses, in kg,	are to be	packed into bins.
---	---------------	----------------	-----------	-------------------

8 5 9 7 7 9 1 3 3 8

(i) Chloe says that first-fit decreasing gives a packing that requires 4 bins, but first-fit only requires 3 bins. Find the maximum capacity of the bins. [6]

First-fit requires one pass through the list and the time taken may be regarded as being proportional to the length of the list. Suppose that shuttle sort was used to sort the list into decreasing order.

(ii) What can be deduced, in this case, about the order of the time complexity, T(n), for first-fit decreasing? [2]

A complete graph on five vertices is weighted to form a network, as given in the weighted matrix below.

	A	В	C	D	E
A	-	9	5	4	2
В	9	-	7	5	7
C	5	7	-	6	8
D	4	5	6		5
\mathbf{E}	2	7	8	5	-

(i) Apply Prim's algorithm to the copy of this weighted matrix in the Printed Answer Booklet to construct a minimum spanning tree for the five vertices.

Draw your minimum spanning tree, stating the order in which you built the tree and giving its total weight. [4]

(ii) (a) Using only the arcs in the minimum spanning tree, which vertex should be chosen to find the smallest total of the weights of the paths from that vertex to each of the other vertices? [1]

(b) State the minimum total for this vertex. [1]

(iii) Show that the total number of comparisons needed to find a minimum spanning tree for a 5×5 matrix is 16. [3]

(iv) If a computer takes 4 seconds to find a minimum spanning tree for a network with 100 vertices, how long would it take to find a minimum spanning tree for a network with 500 vertices? [2]

A sweet shop sells three different types of boxes of chocolate truffles. The cost of each type of box and the number of truffles of each variety in each type of box are given in the table below.

Type	Cost (£)	Milk chocolate	Plain chocolate	White chocolate	Nutty chocolate
Assorted	2.00	5	5	5	5
No Nuts	1.00	5	8	7	0
Speciality	2.50	5	4	9	2

Narendra wants to buy some boxes of truffles so that in total he has at least 20 milk chocolate, 10 plain chocolate, 16 white chocolate and 12 nutty chocolate truffles.

(i) Explain why Narendra needs to buy at least four boxes of truffles.
--

- (ii) Narendra decides that he will buy exactly four boxes. Determine the minimum number of Assorted boxes that Narendra must buy. [1]
- (iii) For your answer in part (ii),
 - list all the feasible solutions and
 - find the cheapest solution.

[3]

Narendra finds that the sweet shop has sold out of Assorted boxes, but he then spots that it also sells small boxes of milk chocolate truffles and small boxes of nutty chocolate truffles. Each small box contains 4 truffles (all of one variety) and costs £0.50.

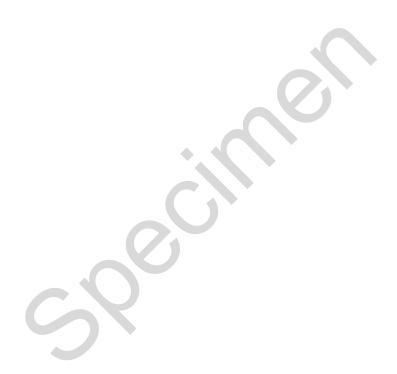
He decides to buy x boxes of No Nuts and y boxes of Speciality, where x + y < 4, so that he has at least 10 plain chocolate and 16 white chocolate truffles. He will then buy as many small boxes as he needs to give a total of at least 20 milk chocolate and 12 nutty chocolate truffles.

(i	v) (a	ı) S	Set up constraints on the values of x and y.	[2]	

- (b) Represent the feasible region graphically. [2]
- (c) Hence determine the cheapest cost for Narendra. [3]

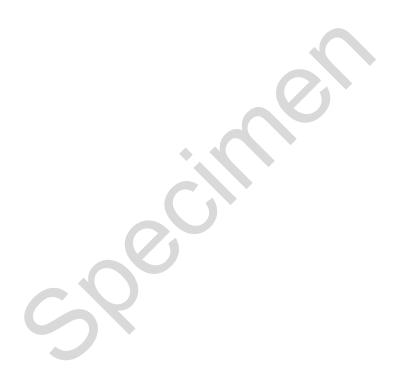
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...day June 20XX - Morning/Afternoon

AS Level Further Mathematics A Y534 Discrete Mathematics

SAMPLE MARK SCHEME

Duration: 1 hour 15 minutes

MAXIMUM MARK 60

This document consists of 16 pages

Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
√and x	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
٨	Omission sign
MR	Misread
Highlighting	
Other abbreviations in	Meaning
mark scheme	
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator

2. Subject-specific Marking Instructions for AS Level Further Mathematics A

- Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

 If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

 Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it
- Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for g. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

easier to mark follow through questions candidate-by-candidate rather than question-by-question.

	Questio	n Answer	Marks	AO	Guidance		
1		(A) e.g. Is this journey possible?	B1	1.1	Any relevant problem that	In the context of this train	
		e.g. Is it possible to travel from Edinburgh to			demonstrates the idea of existence	journey	
		Southampton, leaving Edinburgh after 9 am and					
		arriving in Southampton by 4 pm?					
1		(B) e.g. What is the latest time I can leave	B 1	1.1	Any relevant problem that	In the context of this train	
		Edinburgh to arrive in Southampton by 4 pm?			demonstrates the idea of optimisation	journey	
			[2]				
2	(i)	3 possible orders: ABCD ACBD CABD	B1	1.1	Stating 3 or listing the three orders		
			[1]				
2	(22)	E must some often C but otherwise it can so	B1	11	Con or invalid by heing two for all		
2	(ii)	E must come after C, but otherwise it can go	В1	1.1	Seen, or implied by being true for all		
		anywhere	3.71	2.1	given orders	A D CED A D CDE	
		If A, B, C, D are in the order A B C D then E	M1	2.1	Breaking the problem up into cases	ABCED ABCDE	
		can go immediately after C or D \Rightarrow 2		* *		ACEBD ACBED	
		If they are in the order A C B D then E can go			· ·	ACBDE CEABD	
		immediately after C, B or D \Rightarrow 3				CAEBD CABED	
		If they are in the order C A B D then E can go				CABDE	
		immediately after C, A, B or D \Rightarrow 4					
		In total there are 9 possible orders	E1	2.4	Showing that there are 9 orders and no		
					more		
			[3]				

	Question	n Answer	Marks	AO	Guidance		
2	(iii)	F must come after C	B1	1.1	Seen, or implied by being true for all given orders		
		If C is in the third position (A B C E D, A B C D E) there are 3 possibilities for $F \Rightarrow 6$ If C is in the second position (A C E B D, A C B E D, A C B D E) there are 4 possibilities for $F \Rightarrow 12$ If C is in the first position (C E A B D, C A E B D, C A B E D, C A B D E) there are 5 possibilities for $F \Rightarrow 20$ In total there are 38 possible orders	M1	2.1	Making a substantial start at counting the possibilities, this may involve starting again With appropriate working	A listing of the possibilities, without written reasoning, would score M0	
3	(i)	Let X play strategy P with probability p and strategy Q with probability $1-p$ If Y plays strategy R , X can expect to win $4p-3(1-p)=7p-3$ If Y plays S , X can expect $-2p+(1-p)=1-3p$ $p=0 \Rightarrow \min E(\min)=-3$ $p=1 \Rightarrow \min E(\min)=-2$ $7p-3=1-3p \Rightarrow p=0.4$ and $\min E(\min)=-0.2$ X should choose randomly between strategies P and Q so that P has prob 0.4 and Q has prob 0.6	[3] M1 A1 E1 M1	3.3 1.1 3.4 1.1a 3.4	Calculating expected winnings if Y plays R or S Both correct Explicitly considering extreme points, or using a sketch graph to show that optimum point is at intersection Solving their expressions simultaneously to achieve their p Interpretation of $p = 0.4$ in context	May use p for $P(X \text{ plays } Q)$ May add a constant throughout Need not simplify expressions	
			[5]	J•T	interpretation of $p = 0.7$ in context		

	Question	Answer	Marks	AO	Guidance
3	(ii)	E.g. You must assume that <i>Y</i> is not going to play predictably E.g. You must assume that <i>Y</i> is not going to use a pure strategy	E1	3.5b	For one limitation of the model with reference to <i>Y</i> 's limited behaviour
4	(i)	Route e.g. $c - b - a - e - d - c - b - e - d$	B1 [1]	1.1	A route that starts and ends at c and d and uses every edge once and only once
4	(ii)	It has exactly two odd vertex orders	B1 [1]	1.2	Two and only two odd
4	(iii)	In graph 1 there are two arcs directly joining b to c (or d to e) In graph 2 there are two arcs directly joining v to w	B1 B1 [2]	1.1	Reason why graph 1 is not simple Reason why graph 2 is not simple
4	(iv)	e.g. in graph 1 the vertex of degree 2 (a) is adjacent to each vertex of degree 4 (b and e), whereas in graph 2 the vertex of degree 2 (y) is adjacent to one vertex of degree 4 (z) but not the other (w) e.g. graph 1 has two pairs of vertices directly joined by two arcs (bc and de) whereas graph 2 only has one such pair (vw)	M1 A1	2.3	Partially correct explanation of why the graphs are not isomorphic Fully correct explanation
			[2]	1.1	i uny correct explanation

	Questic	on	Answer	Marks	AO	Guida	nce
5	(i)			B1	1.1	These three graphs and no others	May appear in any equivalent variation
5	(ii)		e.g. Six vertices so need 6 positive integers e.g. 5 arcs so sum of vertex orders =10 e.g. Tree must have at least two 'ends' so at least two vertex orders have value 1	B3 [3]	1.1 1.1 2.5	B1 for each independently correct property	Award B2 for three properties if incorrect or inconsistent terminology used
5	(iii)		{1, 1, 1, 1, 1, 5} {1, 1, 1, 1, 2, 4} {1, 1, 1, 1, 3, 3} {1, 1, 1, 2, 2, 3} {1, 1, 2, 2, 2, 2}	M1 A1 [2]	1.1	At least four correct sets All five correct with no extras	
5	(iv)			M1 A1	1.1	At least four correct graphs Five correct graphs and no extras, unless it is because both versions of {1, 1, 1, 2, 2, 3} are shown	Other possibility for {1, 1, 1, 2, 2, 3}

	Questio	n Answer	Marks	AO	Guidan	ce
6	(i)	Total mass is 60, so each bin must hold at least	B1	1.1	Consider total mass to find a lower	
		20kg			bound for capacity	
		If it is 20kg then using first-fit:			Attempt first-fit with a capacity of at	
		8 5 7	M1	3.1b	least 20kg	First bin correct, in this order
		9 7 1 3				
		9 3 8	A1	1.1	All correct, in this order	
		Using first-fit decreasing:				
		9 9 1				
		8 8 3			Attempt first-fit decreasing with a	Correct placement of the values
		7 7 5	M1	3.1b	capacity of at least 20kg	998877
		3	A1	1.1	All correct, in this order (or a	
		But if the capacity was 21kg then the 3 could go			description in words)	
		into the first bin and the 1 into the second bin, so				
		only three bins are needed	•			
		So the bins cannot be more than 20kg, so they	E 1	3.2a	20 is also the upper bound, so the	
		must be exactly 20kg			capacity is 20	
			[6]			
6	(ii)	Shuttle sort has quadratic order, as a function of	M1	1.1	Knowing and using the fact that shuttle	$T(n) = O(n^2) + O(n)$
		the length of the list, so the time to run first-fit			sort has quadratic order	
		decreasing would be the sum of a quadratic				
		function and a linear function, which is a				
		quadratic function				
		This means that first fit-decreasing has quadratic	A1	2.2a		$=O(n^2)$
		order in this case				
			[2]			

	Questic	n	Answer	Marks	AO	Guidance
7	(i)		e.g. A B C D E A - 9 5 4 2 B 9 - 7 (\$) 7 C (\$) 7 - 6 8 D (4) 5 6 - 5 E (2) 7 8 5 - Using Prim's algorithm starting at A AE = 2 AD = 4 AC = 5 (or DB) DB = 5 (or AC) Total weight = 16	M1 A1 B1	1.1a 1.1 1.1 1.1	Stating which is the starting vertex A valid order of building the tree for their starting vertex, clearly shown (arcs or vertices with arcs indicated on matrix) Correct (labelled) tree Weights need not be shown
7	(ii)	(a)	Vertex A	B1 [1]	3.1a	
	(ii)	(b)	0+(4+5)+5+4+2	B1	1.1	
			\Rightarrow 20			
				[1]		

	Question		Answer	Marks	AO	Guidance		
7	(iii)		$(1\times4-1)+(2\times3-1)+(3\times2-1)+(4\times1-1)$	M1	2.1	1×4 , 2×3 , etc.	Or by referring to their working	
							in part (i)	
				M1	1.1	Subtracting 1 for each pass		
			=3+5+5+3=16	A1	1.1	www		
				[3]				
7	(iv)		Cubic order	M1	1.1	Stating or using the fact that Prim's		
						has cubic order		
			$(500)^3$	A1	2.2b	Must include an indication that this is	8 minutes 20 seconds	
			Approximately $\left(\frac{500}{100}\right)^3 \times 4 = 500$ seconds oe			an approximation		
				[2]				

(Questio	n		Ansv	wer		Marks	AO	Guidan	ice
8	(i)		5 milk choco	olate in each	type, $4 \times 5 =$	20	B1	2.2a	Using numbers of milk chocolate truffles	
							[1]			
8	(ii)		2 so that ther	re are at least	12 nutty cho	ocolate	B1	2.2a	2 (Assorted boxes) and using numbers	
			truffles						of nutty chocolate truffles	
							[1]			
8	(iii)			Type		Cost	M1	1.1	Identifying at least three of these five	Need not show costs, and if
			Assorted	No Nuts	Speciality	£			cases for the number of boxes of the	given do not penalise calculation
			4	0	0	8.00			different types bought	errors
			3	1	0	7.00	A1	1.1	All five eases and no others unless	
			3	0	1	8.50	AI	1.1	All five cases, and no others, unless explicitly rejected as being infeasible	
			2	1	1	7.50			explicitly rejected as being lineasible	
			2	0	2	9.00	4	• 4		
			8	3						
			3× Assorted	l and 1× No	Nuts	0	B1 [3]	1.1	cao	May be marked in list

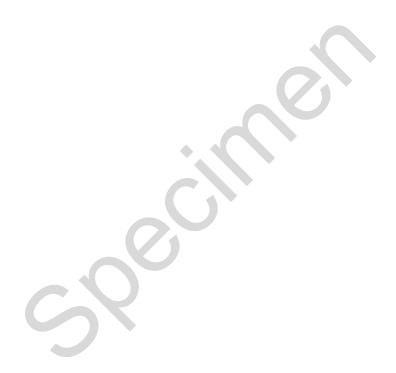
	Questic	n	Answer	Marks	AO	Guidance		
8	(iv)	(a)	P: $8x + 4y \ge 10$ oe	M1	3.1b	One of $8x + 4y \ge 10$ and $7x + 9y \ge 16$,	Allow strict inequalities, but not	
			W: $7x + 9y \ge 16$ oe			in any form	an equality or with inequality reversed	
			$x \ge 0$ and $y \ge 0$ (and integer-valued)	A1	1.2	Both of these correct, in any form		
				[2]				
8	(iv)	(b)	v	M1	3.3	Plotting lines and identifying feasible	For reference:	
						region	(0, 2.5)	
			\`\\				(0.59, 1.32) or better	
				A1	1.1	All lines and feasible region correct on	(2.28 to 2.29, 0)	
						scaled axes		
					• 4			
						*		
			$\lambda \lambda $					
			7					
				[2]				
8	(iv)	(c)	$(0, 3) + 2 \text{ small milk} + 2 \text{ small nutty} \Rightarrow £9.50$	M1	3.4	Calculating costs for any integer-	May go straight to solution	
			$(1, 2) + 2$ small milk + 2 small nutty \Rightarrow £8.00			valued feasible solution	(from logical reasoning or	
			$(2, 1) + 2 \text{ small milk} + 3 \text{ small nutty} \Rightarrow £7.00$	2.51	2.2	X 1 1 CC 1 1 1 1 1 1 1	calculation)	
			$(3, 0) + 2$ small milk + 3 small nutty \Rightarrow £5.50	M1	3.2a	Including sufficient small packs to deal		
			$(1, 1) + 3$ small milk + 3 small nutty \Rightarrow £6.50			with 'milk' and 'nutty' requirements		
						05.50	70.0	
			Cheapest solution costs Narendra £5.50	E 1	3.4	£5.50	E0 if exterior points used as if	
							feasible	
							E0 if correct answer given with	
				[2]			insufficient evidence to justify it	
				[3]				

Assessment Objectives (AO) Grid

Question	AO1	AO2	AO3(PS)	AO3(M)	Total
1	2	0	0	0	2
2(i)	1	0	()	()	1
2(ii)	1	2	()	0	3
2(iii)	1	2	()	Û	3
3(i)	2		0	3	5
3(ii)				1	1
4(i)	1	()	0	Û	1
4(ii)	1	()	0	0	1
4(iii)	2	()	0	0	2
4(iv)	1	1	()	Ü	2
5(i)	1	()	()	0	1
5(ii)	2	1			3
5(iii)	2	()		0	2
5(iv)	2	()	()	0	2
6(i)	3	0	3	0	6
6(ii)	1	1	0	0	2
7(i)	4				4
7(ii)	1		1		2
7(iii)	2	1	()		3
7(iv)	1	1	0		2
8(i)		1	0	1	1
8(ii)	r.J.	1			1
8(iii)	3				3
8(iv)(a)	1	0	l		2
8(iv)(b)	1			1	2
8(iv)(c)			1	2	3
Totals	36	11	6	7	60

PS = Problem Solving M = Modelling

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AS Level Further Mathematics AUnit Y534 Discrete Mathematics

Printed Answer Booklet

Date - Morning/Afternoon

Time allowed: 1 hour 15 minutes

OCR supplied materials:

- Printed Answer Booklet
- · Formulae AS Level Further Mathematics A

You must have:

- · Printed Answer Booklet
- Formulae AS Level Further Mathematics A
- · Scientific or graphical calculator



First name	
Last name	
Centre number	Candidate number

INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer all the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet.
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by g m s⁻². Unless otherwise instructed, when a numerical value is needed, use g = 9.8.

INFORMATION

- You are reminded of the need for clear presentation in your answers.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 8 pages.



1(A)	
1 (B)	
- (2)	
2(i)	
2(**)	
2(ii)	
2(iii)	

3	
4(1)	
4(i)	
4(ii)	
4(II)	
4(iii)	
4(iv)	

5(i)	
5(ii)	
- (111)	
5(iii)	

5(iv)	

6(i)	
•	
•	
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6(ii)(a)	
6(ii)(a)	
6(iii)	

7(i)									
	A B C D E A - 9 5 4 2								
	A - 9 5 4 2 B 9 - 7 5 7								
	A B C D E A - 9 5 4 2 B 9 - 7 5 7 C 5 7 - 6 8 D 4 5 6 - 5								
	D 4 5 6 - 5								
	E 2 7 8 5 -								
7(ii)(a)									
-									
7(*)(1)									
7(ii)(b)									

7(iii)	
7(iv)	

8(i)	
0(**)	
8(ii)	
8(iii)	

8(iv)(a)									1
								•	-
								•	
		<u> </u>	<u>i</u>	<u> </u>	<u>i</u>			<u>i</u>	.1
					7 7				
8(iv)(b)				Ÿ					
0(11)(0)									
1									

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