

A Level Further Mathematics A Y541 Pure Core 2 Sample Question Paper

Date – Morning/Afternoon

Time allowed: 1 hour 30 minutes

OCR supplied materials:

- Printed Answer Booklet
- Formulae A Level Further Mathematics A

You must have:

- Printed Answer Booklet
- Formulae A Level Further Mathematics A
- Scientific or graphical calculator



INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.**
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by $g \text{ m s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $g = 9.8$.

INFORMATION

- The total number of marks for this paper is **75**.
- The marks for each question are shown in brackets [].
- **You are reminded of the need for clear presentation in your answers.**
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **4** pages.

Answer **all** the questions.

1 Find $\sum_{r=1}^n (r+1)(r+5)$. Give your answer in a fully factorised form. [4]

2 **In this question you must show detailed reasoning.**

The finite region R is enclosed by the curve with equation $y = \frac{8}{\sqrt{16+x^2}}$, the x -axis and the lines $x=0$ and $x=4$. Region R is rotated through 360° about the x -axis. Find the exact value of the volume generated. [4]

3 (i) Find $\sum_{r=1}^n \left(\frac{1}{r} - \frac{1}{r+2} \right)$. [3]

(ii) What does the sum in part (i) tend to as $n \rightarrow \infty$? Justify your answer. [1]

4 It is given that $\frac{5x^2+x+12}{x^3+kx} \equiv \frac{A}{x} + \frac{Bx+C}{x^2+k}$ where k , A , B and C are positive integers. Determine the set of possible values of k . [5]

5 **In this question you must show detailed reasoning.**

Evaluate $\int_0^\infty 2xe^{-x} dx$.

[You may use the result $\lim_{x \rightarrow \infty} xe^{-x} = 0$.] [4]

6 The equation of a plane Π is $x - 2y - z = 30$.

(i) Find the acute angle between the line $\mathbf{r} = \begin{pmatrix} 3 \\ 2 \\ -5 \end{pmatrix} + \lambda \begin{pmatrix} -5 \\ 3 \\ 2 \end{pmatrix}$ and Π . [4]

(ii) Determine the geometrical relationship between the line $\mathbf{r} = \begin{pmatrix} 1 \\ 4 \\ 2 \end{pmatrix} + \mu \begin{pmatrix} 3 \\ -1 \\ 5 \end{pmatrix}$ and Π . [4]

7 (i) Use the Maclaurin series for $\sin x$ to work out the series expansion of $\sin x \sin 2x \sin 4x$ up to and including the term in x^3 . [4]

(ii) Hence find, in exact surd form, an approximation to the least positive root of the equation $2\sin x \sin 2x \sin 4x = x$. [3]

8 The equation of a curve is $y = \cosh^2 x - 3\sinh x$. Show that $\left(\ln\left(\frac{3+\sqrt{13}}{2}\right), -\frac{5}{4}\right)$ is the only stationary point on the curve. [8]

9 A curve has equation $x^4 + y^4 = x^2 + y^2$, where x and y are not both zero.

(i) Show that the equation of the curve in polar coordinates is $r^2 = \frac{2}{2 - \sin^2 2\theta}$. [4]

(ii) Deduce that no point on the curve $x^4 + y^4 = x^2 + y^2$ is further than $\sqrt{2}$ from the origin. [2]

10 Let $C = \sum_{r=0}^{20} \binom{20}{r} \cos r\theta$. Show that $C = 2^{20} \cos^{20}\left(\frac{1}{2}\theta\right) \cos 10\theta$. [8]

11 During an industrial process substance X is converted into substance Z . Some of the substance X goes through an intermediate phase, and is converted to substance Y , before being converted to substance Z . The situation is modelled by

$$\frac{dy}{dt} = 0.3x - 0.2y \quad \text{and} \quad \frac{dz}{dt} = 0.2y + 0.1x$$

where x , y and z are the amounts in kg of X , Y and Z at time t hours after the process starts.

Initially there is 10 kg of substance X and nothing of substances Y and Z . The amount of substance X decreases exponentially. The initial rate of decrease is 4 kg per hour.

(i) Show that $x = Ae^{-0.4t}$, stating the value of A . [3]

(ii) (a) Show that $\frac{dx}{dt} + \frac{dy}{dt} + \frac{dz}{dt} = 0$. [2]

(b) Comment on this result in the context of the industrial process. [2]

(iii) Express y in terms of t . [5]

(iv) Determine the maximum amount of substance Y present during the process. [3]

(v) How long does it take to produce 9 kg of substance Z ? [2]

END OF QUESTION PAPER

Specimen

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...day June 20XX – Morning/Afternoon

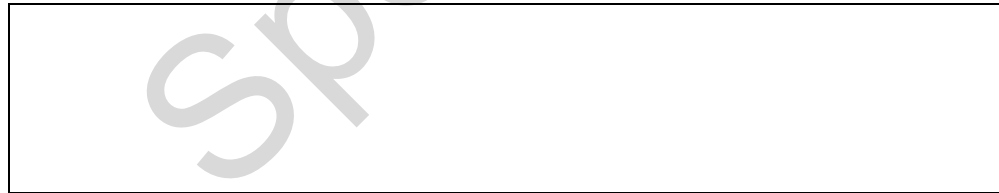
A Level Further Mathematics A

Y541 Pure Core 2

SAMPLE MARK SCHEME

Duration: 1 hour 30 minutes

MAXIMUM MARK 75



This document consists of 16 pages

Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
✓ and ✕	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining a result or establishing a given result
U1	Mark for correct units
G1	Mark for a correct feature on a graph
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.

2. Subject-specific Marking Instructions for A Level Further Mathematics A

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation ‘dep*’ is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate’s data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. ‘Fresh starts’ will not affect an earlier decision about a misread. Note that a miscopy of the candidate’s own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question	Answer	Marks	AO	Guidance
1	$\sum_{r=1}^n r^2 + 6\sum_{r=1}^n r + \sum_{r=1}^n 5$ $= \frac{1}{6}n(n+1)(2n+1) + 6\frac{n(n+1)}{2} + 5n$ $\frac{1}{6}n(n+7)(2n+7) \text{ oe}$	M1 M1 A1 A1 [4]	1.1a 1.2 1.1 1.1	At least two of three elements correct Substitution of at least one correct standard formula Correct unsimplified answer For full marks all algebra must be correct
2	DR $[V =]\pi \int_0^4 \left(\frac{8}{\sqrt{16+x^2}} \right)^2 dx$ $64\pi \times \frac{1}{4} \tan^{-1} \left(\frac{x}{4} \right)$ $16\pi \tan^{-1}(1) - 16\pi \tan^{-1}(0)$ $= 4\pi^2$	B1 M1 M1 A1 [4]	1.1 1.2 1.1 1.1	Must be seen Using formulae booklet Substitution of correct limits must be seen

Question		Answer	Marks	AO	Guidance	
3	(i)	$\left(1 - \frac{1}{3}\right) + \left(\frac{1}{2} - \frac{1}{4}\right) + \left(\frac{1}{3} - \frac{1}{5}\right) + \dots$ $+ \left(\frac{1}{n-1} - \frac{1}{n+1}\right) + \left(\frac{1}{n} - \frac{1}{n+2}\right)$ <p>Cancelling of inner terms</p> $\frac{3}{2} - \frac{1}{n+1} - \frac{1}{n+2}$	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>2.1</p> <p>1.1</p> <p>1.1</p>	At least first and last terms in full	
3	(ii)	$\frac{1}{n+1} \rightarrow 0 \text{ and } \frac{1}{n+2} \rightarrow 0, \text{ hence sum } \rightarrow \frac{3}{2}$	<p>E1</p> <p>[1]</p>	2.4	Justification required E0 for unsupported answer	
4		$5x^2 + x + 12 \equiv A(x^2 + k) + (Bx + C)x$ $A = \frac{12}{k}, B = 5 - \frac{12}{k}$ <p>Since A and B must be integers, k must divide 12.</p> <p>$B > 0$ gives $k = 3, 4, 6$ or 12</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>E1</p> <p>[5]</p>	<p>1.1</p> <p>3.1a</p> <p>1.1</p> <p>3.1a</p> <p>2.2a</p>	<p>Attempt to find A, B and C in terms of k</p> <p>Attempt to express A or B in terms of k</p> <p>For both expressions</p> <p>Interpret the expression for A or B as an integer</p> <p>For this set only, having considered both A and B</p>	Allow without $C = 1$ since it is independent of k
5		<p>DR</p> $-2xe^{-x} + \int 2e^{-x} dx$ <p>Evaluation of their $F[x]$ using both limits</p> $\frac{[0-0] - [0-2]}{2}$	<p>*M1</p> <p>A1</p> <p>dep*M1</p> <p>A1</p> <p>[4]</p>	<p>1.1</p> <p>1.1</p> <p>1.1</p> <p>1.1</p>	<p>Allow sign errors only</p> <p>Must be seen</p> <p>$F[x] = -2xe^{-x} - 2e^{-x}$</p>	<p>e.g. M1 for $\pm 2xe^{-x} \pm \int 2e^{-x} dx$</p> <p>Evaluation must be seen</p>

Question		Answer	Marks	AO	Guidance
6	(i)	$-5-6-2 = \sqrt{1+4+1}\sqrt{25+9+4} \cos \theta$ oe $\theta = \cos^{-1} \frac{-13}{\sqrt{6 \times 38}}$ oe $149.4^\circ - 90^\circ$ 59.4°	*M1 dep*M1 M1 A1 [4]	1.1a 1.1 2.2a 1.1	Allow one slip e.g. sign error Using angle with normal to find angle with plane 1.04 in radians
6	(ii)	$1 \times 3 + (-2) \times (-1) + (-1) \times 5 = 0$ The line is in or parallel to the plane $1 \times 1 - 2 \times 4 - 1 \times (2) \neq 30$ Point on line not in plane, so line is parallel to plane	M1 E1 M1 E1 [4]	3.1a 2.2a 3.1a 2.2a	Alternative method $1 + 3\mu - 2(4 - \mu) - (2 + 5\mu) = -9$ M1A1 -9 is not 30 E1 Conclusion E1 Substitution of e.g. (1, 4, 2) in equation of plane oe
7	(i)	$\sin 2x = 2x - \frac{4}{3}x^3 \dots$ and $\sin 4x = 4x - \frac{32}{3}x^3 \dots$ $(x - \frac{1}{6}x^3)(2x - \frac{4}{3}x^3)(4x - \frac{32}{3}x^3)$ $= 8x^3 - 28x^5$	M1 A1 M1 A1 [4]	2.1 1.1a 1.1 1.1	$x \rightarrow 2x$ and $x \rightarrow 4x$ in $\sin x$ expansion Attempt complete expansion These terms and no others
7	(ii)	$(x)(56x^4 - 16x^2 + 1) = 0$ oe $x^2 = \frac{16 \pm \sqrt{32}}{112}$ $x = \sqrt{\frac{4 - \sqrt{2}}{28}}$ or equivalent exact surd.	M1 M1 A1 [3]	1.1 3.1a 1.1	Substitute and rearrange Solve as quadratic in x^2 Select correct answer

Question	Answer	Marks	AO	Guidance
8	$2\cosh x \sinh x - 3\cosh x$ $2\cosh x \sinh x - 3\cosh x = 0$ $\Rightarrow \cosh x(2\sinh x - 3) = 0$ <p>$\cosh x = 0$ has no roots, because $\cosh x \geq 1$</p> <p>\sinh is a 1-1 function so therefore just one stationary point when $(2\sinh x - 3) = 0$</p> $x = \sinh^{-1} \frac{3}{2} = \ln \left(\frac{3}{2} + \sqrt{1 + \left(\frac{3}{2}\right)^2} \right)$ <p>and completion to $x = \ln \left(\frac{3 + \sqrt{13}}{2} \right)$</p> $\cosh x = \sqrt{1 + \sinh^2 x} = \sqrt{\frac{13}{4}}$ $y = \cosh^2 x - 3\sinh x = \left(\sqrt{\frac{13}{4}} \right)^2 - 3 \times \frac{3}{2}$ <p>completion to $y = -\frac{5}{4}$ oe</p>	<p>*M1</p> <p>dep*M1</p> <p>E1</p> <p>E1</p> <p>E1</p> <p>M1</p> <p>A1</p> <p>E1</p> <p>[8]</p>	<p>1.1</p> <p>2.1</p> <p>2.4</p> <p>2.4</p> <p>2.2a</p> <p>2.1</p> <p>1.1</p> <p>1.1</p>	<p>Allow sign errors only</p> <p>Their $f'(x) = 0$ and factorising their expression</p> <p>AG</p> <p>Attempt to evaluate $\cosh x$ and substitute to find y</p> <p>Correct substitution seen</p> <p>AG</p> <p>e.g. $\pm 2\cosh x \sinh x \pm 3\cosh x$</p> <p>Or other complete method to find y</p>

Question		Answer	Marks	AO	Guidance
9	(i)	e.g. $r^4 \cos^4 \theta + r^4 \sin^4 \theta = r^2$ $r^2 = \frac{1}{\cos^4 \theta + \sin^4 \theta}$ $= \frac{1}{(\cos^2 \theta + \sin^2 \theta)^2 - 2\sin^2 \theta \cos^2 \theta}$ $= \frac{1}{1 - \frac{1}{2} \sin^2 2\theta} = \frac{2}{2 - \sin^2 2\theta}$	B1 B1 M1 A1 [4]	1.1 1.1 2.1 2.2a	Substitute $x = r \cos \theta$, $y = r \sin \theta$ Use $x^2 + y^2 = r^2$ Rearrange and attempt to use relevant trigonometric identity AG
	(ii)	Maximum value of r occurs when $\sin 2\theta = 1$ $r^2 = \frac{2}{2-1} = 2 \Rightarrow r = \sqrt{2}$	M1 A1 [2]	1.1 2.2a	AG

Question	Answer	Marks	AO	Guidance
10	<p>Let $C = \sum_{r=0}^{20} \binom{20}{r} \cos r\theta$ and $S = \sum_{r=1}^{20} \binom{20}{r} \sin r\theta$</p> <p>$C + iS =$</p> <p>$1 + 20(\cos \theta + i \sin \theta) + \binom{20}{2}(\cos 2\theta + i \sin 2\theta) +$</p> <p>$\dots + (\cos 20\theta + i \sin 20\theta)$</p> <p>$= 1 + 20z + \binom{20}{2}z^2 + \dots + z^{20}$</p> <p>where $z = (\cos \theta + i \sin \theta)$</p> <p>$= (1 + z)^{20}$</p> <p>$\left(1 + 2 \cos^2 \frac{\theta}{2} - 1 + i 2 \sin \frac{\theta}{2} \cos \frac{\theta}{2}\right)^{20}$</p> <p>$\left(2 \cos \frac{\theta}{2}\right)^{20} \left(\cos \frac{\theta}{2} + i \sin \frac{\theta}{2}\right)^{20}$</p> <p>$(\cos 10\theta + i \sin 10\theta)$</p> <p>Re: $C = 2^{20} \cos^{20} \left(\frac{1}{2}\theta\right) \cos 10\theta$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>E1</p> <p>[8]</p>	<p>2.1</p> <p>3.1a</p> <p>2.2a</p> <p>1.1</p> <p>3.1a</p> <p>3.1a</p> <p>2.2a</p> <p>3.2a</p>	<p>by de Moivre's theorem</p> <p>by de Moivre's theorem</p> <p>AG, must see the mention of taking the real part only.</p>

Question		Answer	Marks	AO	Guidance	
11	(i)	$A = 10$ $x = Ae^{kt} \Rightarrow \frac{dx}{dt} = Ake^{kt}$ giving $Ak = -4$ $10k = -4$ so $k = -0.4$	B1 M1 E1 [3]	3.3 3.3 1.1	Differentiate and use $\frac{dx}{dt} = \pm 4$ when $t = 0$ AG	
11	(ii)	(a)	$\frac{dx}{dt} + \frac{dy}{dt} + \frac{dz}{dt} = -4e^{-0.4t}$ $+ (0.3x - 0.2y) + (0.2y + 0.1x)$ $= -0.4x + 0.3x + 0.1x = 0$	M1 E1 [2]	3.4 1.1	AG
11	(ii)	(b)	$\frac{d}{dt}(x + y + z) = 0 \Rightarrow x + y + z = \text{constant}$ Throughout the industrial process the total amount of the three substances is constant	B1 E1 [2]	2.2a 3.4	i.e. no loss or gain of amounts Must be in context
11	(iii)	$\frac{dy}{dt} + 0.2y = 3e^{-0.4t}$ $\times e^{0.2t}$ $ye^{0.2t} = 3 \int e^{-0.2t} dt$ $y = -15e^{-0.4t} + ce^{-0.2t}$ $c = 15$	M1 M1 A1 M1 A1 [5]	3.4 3.1a 1.1 1.1 1.1	Substitute x and rearrange Alternative CF and PI Allow arithmetic slips in coefficients of exponential terms and/or sign errors	

Question		Answer	Marks	AO	Guidance	
11	(iv)	$-3e^{-0.2t} + 6e^{-0.4t} = 0$	M1	3.4	FT their $\frac{dy}{dt}$ soi	OR M1 $0.3x = 0.2y$ so $0.3 \times 10e^{-0.4t}$ $= 0.2 \times (-15e^{-0.4t} + 15e^{-0.2t})$
		$t = 3.466$	A1	1.1	BC	A1 $t = 3.466$ BC
		$y_{\max} = 3.75$ kg	A1	3.2a	All three marks may be implied by 3.75 kg BC	A1 $y_{\max} = 3.75$ kg BC
			[3]			
11	(v)	9 kg of substance Z implies $x + y = 1$ $t = 13.4(25)$ hours to 3 s.f. or better	M1 A1 [2]	3.4 1.1	Or by $z = 10 + 5e^{-0.4t} - 15e^{-0.2t} = 9$ BC	

Assessment Objectives (AO) Grid

Question	AO1	AO2	AO3(PS)	AO3(M)	Total
1	4	0	0	0	4
2	4	0	0	0	4
3(i)	2	1	0	0	3
3(ii)	0	1	0	0	1
4	2	1	2	0	5
5	4	0	0	0	4
6(i)	3	1	0	0	4
6(ii)	0	2	2	0	4
7(i)	3	1	0	0	4
7(ii)	2	0	1	0	3
8	3	5	0	0	8
9(i)	2	2	0	0	4
9(ii)	1	1	0	0	2
10	1	3	4	0	8
11(i)	1	0	0	2	3
11(ii)(a)	1	0	0	1	2
11(ii)(b)	0	1	0	1	2
11(iii)	3	0	1	1	5
11(iv)	1	0	1	1	3
11(v)	1	0	0	1	2
Totals	38	19	11	7	75

PS = Problem Solving

M = Modelling

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Specimen

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