## GCE Examinations

## Advanced Subsidiary / Advanced Level

## Statistics

## Module S2

Paper A

## MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.
Accuracy marks (A) can only be awarded when a correct method has been used.
(B) marks are independent of method marks.

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## S2 Paper A - Marking Guide

1. (a) median $=125 \mathrm{~m} \quad \mathrm{~A} 1$
$\mathrm{IQR}=$ middle half $=25 \mathrm{~m}($ or $137.5-112.5)$
(b) e.g. likely to have higher prob. dens. near median and some values more than 25 m away from median

B2
(5)
2.
(a) $=1-\mathrm{F}(5)=1-\frac{1}{64}(80-25)=\frac{9}{64}$

M1 A1
(b) $\mathrm{f}(x)=\mathrm{F}^{\prime}(x)=\frac{1}{64}(16-2 x)$

M1 A1
$\therefore \mathrm{f}(x)= \begin{cases}\frac{1}{32}(8-x), & 0 \leq x \leq 8, \\ 0, & \text { otherwise. }\end{cases}$
A1
(c)


B3
(8)
3. (a) e.g. requests for repairs likely to occur singly, at random and at a constant rate
$\lambda=\frac{180}{40}=4.5$ A1
(b) let $X=$ no. of repairs per day $\therefore X \sim \operatorname{Po}(4.5)$
(i) $\mathrm{P}(X=0)=0.0111$
(ii) $\mathrm{P}(X>6)=1-\mathrm{P}(X \leq 6)=1-0.8311=0.1689$

A1
M1 A1
(c) let $Y=$ no. of days he repairs more than $6 \therefore Y \sim \mathrm{~B}(10,0.1689)$
$\mathrm{P}(Y=3)={ }^{10} \mathrm{C}_{3}(0.1689)^{3}(0.8311){ }^{7}=0.158$ (3sf)
M1
M1 A1
4. (a) e.g. quicker; may not be able to get all pupils to respond B2
(b) school roll B1
(c) let $X=$ no. of students who play tennis $\therefore X \sim \mathrm{~B}\left(120, \frac{1}{20}\right)$
$\mathrm{H}_{0}: p=\frac{1}{20} \quad \mathrm{H}_{1}: p \neq \frac{1}{20}$
B1
Using Po approx. $X \approx \sim \operatorname{Po}(6)$
M1
$\mathrm{P}(X \leq 2)=0.0620 ; ~ \mathrm{P}(X \leq 10)=0.9574$
M1 A1
$\therefore$ C.R. is $X \leq 2$ or $X \geq 11$
A1
(d) $0.0620+0.0426=0.1046$

A1 (10)
5. (a) let $X=$ no. out of 10 shares that have gone up $\therefore X \sim \mathrm{~B}(10,0.35)$
(i) $\mathrm{P}(X=6)=0.9740-0.9051=0.0689$

M1
(ii) $\mathrm{P}(>5$ gone down $)=\mathrm{P}(X \leq 4)=0.7515$
(b) let $Y=$ no. out of 80 shares that have gone down $\therefore Y \sim \mathrm{~B}(80,0.65)$

N approx. $D \sim \mathrm{~N}(52,18.2)$
$\mathrm{P}(Y>55) \approx \mathrm{P}(D>55.5)$

$$
\begin{aligned}
& =\mathrm{P}\left(Z>\frac{55.5-52}{\sqrt{18.2}}\right)=\mathrm{P}(Z>0.82) \\
& =1-0.7939=0.2061
\end{aligned}
$$

6. (a) Poisson with $\lambda=4$

## B1

(b) e.g. more people shopping $\therefore$ probably sell more so $\lambda$ higher
(c) (i) let $X=$ no. of sales per hour $\therefore X \sim \operatorname{Po(4)}$

$$
\mathrm{P}(X>4)=1-\mathrm{P}(X \leq 4)=1-0.6288=0.3712 \quad \mathrm{M} 1 \mathrm{~A} 1
$$

$\begin{array}{lll}\text { (ii) } \begin{array}{ll}\text { let } Y=\text { no. of sales per half-hour } \therefore Y \sim \mathrm{Po}(2) & \text { M1 } \\ & \mathrm{P}(Y=0)=0.1353\end{array} & \mathrm{~A} 1 \\ \text { (iii) }(0.3712)^{3}=0.0511(3 \mathrm{sf}) & \text { M1 A1 }\end{array}$
(d) $\mathrm{H}_{0}: \lambda=4 \quad \mathrm{H}_{1}: \lambda>4$

B1
$\mathrm{P}(X \geq 7)=1-\mathrm{P}(X \leq 6)=1-0.8893=0.1107$
more than $5 \% \therefore$ not significant, insufficient evidence of increase
M1 A1
A1
7. (a) $\int_{0}^{3} k\left(t^{2}+2\right) \mathrm{d} t=1$
$\therefore k\left[\frac{1}{3} t^{3}+2 t\right]_{0}^{3}=1$
$\therefore k[(9+6)-(0)]=1 ; 15 k=1 ; k=\frac{1}{15}$
M1 A1
(b)


B3
(c) 3

A1
(d) $\mathrm{E}(T)=\int_{0}^{3} t \times \frac{1}{15}\left(t^{2}+2\right) \mathrm{d} t=\frac{1}{15} \int_{0}^{3} t^{3}+2 t \mathrm{~d} t$

M1

$$
\begin{aligned}
& =\frac{1}{15}\left[\frac{1}{4} t^{4}+t^{2}\right]_{0}^{3} \\
& =\frac{1}{15}\left[\left(\frac{81}{4}+9\right)-(0)\right]=\frac{39}{20} \text { or } 1.95
\end{aligned}
$$

M1 A1

M1 A1
(e) $\mathrm{E}\left(T^{2}\right)=\int_{0}^{3} t^{2} \times \frac{1}{15}\left(t^{2}+2\right) \mathrm{d} t=\frac{1}{15} \int_{0}^{3} t^{4}+2 t^{2} \mathrm{~d} t$

$$
=\frac{1}{15}\left[\frac{1}{5} t^{5}+\frac{2}{3} t^{3}\right]_{0}^{3}
$$

$$
=\frac{1}{15}\left[\left(\frac{243}{5}+18\right)-(0)\right]=\frac{111}{25}
$$

$\operatorname{Var}(T)=\frac{111}{25}-\left(\frac{39}{20}\right)^{2}=\frac{255}{400}=\frac{51}{80}=0.6375$
$\therefore$ std. dev $=\sqrt{ } 0.6375=0.798(3 \mathrm{sf})$

Performance Record - S2 Paper A

| Question no. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic(s) | rect. dist. | $\begin{array}{\|l\|l} \hline \text { c.c.f.f. } \\ \text { p.d.f. } \end{array}$ | $\begin{array}{\|l\|} \hline \begin{array}{l} \text { Poisson, } \\ \text { binomial } \end{array} \end{array}$ | sampling, <br> Po appr. to <br> binomial, hyp. test | binomial, <br> N approx. | $\begin{array}{\|l\|} \hline \text { Poisson, } \\ \text { hyp. test } \end{array}$ | $\begin{array}{\|l\|l} \hline \text { p.d.f., } \\ \text { mode, } \\ \text { moan, } \\ \text { mean, } \\ \text { variance } \end{array}$ variance |  |
| Marks | 5 | 8 | 10 | 10 | 11 | 12 | 19 | 75 |
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