## GCE Examinations

## Mechanics Module M3

## Advanced Subsidiary / Advanced Level

## Paper F

Time: 1 hour 30 minutes

## Instructions and Information

Candidates may use any calculator except those with a facility for symbolic algebra and/or calculus.

Full marks may be obtained for answers to ALL questions.
Mathematical and statistical formulae and tables are available.
This paper has 6 questions.
When a numerical value of $g$ is required, use $g=9.8 \mathrm{~m} \mathrm{~s}^{-2}$.

## Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working will gain no credit.

Written by Shaun Armstrong \& Chris Huffer
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1. A particle $P$ of mass 1.5 kg moves from rest at the origin such that at time $t$ seconds it is subject to a single force of magnitude $(4 t+3) \mathrm{N}$ in the direction of the positive $x$-axis.
(a) Find the magnitude of the impulse exerted by the force during the interval $1 \leq t \leq 4$.

Given that at time $T$ seconds, $P$ has a speed of $22 \mathrm{~m} \mathrm{~s}^{-1}$,
(b) find the value of $T$ correct to 3 significant figures.
2.


Fig. 1
A particle $P$ of mass 0.5 kg is at rest at the highest point $A$ of a smooth sphere, centre $O$, of radius 1.25 m which is fixed to a horizontal surface.

When $P$ is slightly disturbed it slides along the surface of the sphere. Whilst $P$ is in contact with the sphere it has speed $v \mathrm{~m} \mathrm{~s}^{-1}$ when $\angle A O P=\theta$ as shown in Figure 1.
(a) Show that $v^{2}=24.5(1-\cos \theta)$.
(b) Find the value of $\cos \theta$ when $P$ leaves the surface of the sphere.
3. A car starts from rest at the point $O$ and moves along a straight line. The car accelerates to a maximum velocity, $V \mathrm{~m} \mathrm{~s}^{-1}$, before decelerating and coming to rest again at the point $A$.

The acceleration of the car during this journey, $a \mathrm{~m} \mathrm{~s}^{-2}$, is modelled by the formula

$$
a=\frac{500-k x}{150},
$$

where $x$ is the distance in metres of the car from $O$.
Using this model and given that the car is travelling at $16 \mathrm{~m} \mathrm{~s}^{-1}$ when it is 40 m from $O$,
(a) find $k$,
(b) show that $V=41$, correct to 2 significant figures,
(c) find the distance $O A$.
4.


Fig. 2
A particle $P$ of mass 2 kg is attached to one end of a light elastic string of natural length 1.5 m and modulus of elasticity $\lambda$. The other end of the string is fixed to a point $A$ on a rough plane inclined at an angle of $30^{\circ}$ to the horizontal as shown in Figure 2. The coefficient of friction between $P$ and the plane is $\frac{1}{6} \sqrt{ }$.
$P$ is held at rest at $A$ and then released. It first comes to instantaneous rest at the point $B, 2.2 \mathrm{~m}$ from $A$. For the motion of $P$ from $A$ to $B$,
(a) show that the work done against friction is 10.78 J ,
(b) find the change in the gravitational potential energy of $P$.

By using the work-energy principle, or otherwise,
(c) find $\lambda$.
5.


Fig. 3
A flask is modelled as a uniform solid formed by removing a cylinder of radius $r$ and height $h$ from a cylinder of radius $\frac{4}{3} r$ and height $\frac{3}{2} h$ with the same axis of symmetry and a common plane as shown in Figure 3.
(a) Show that the centre of mass of the flask is a distance of $\frac{9}{10} h$ from the open end of the flask.

The flask is made from a material of density $\rho$ and is filled to the level of the open plane face with a liquid of density $k \rho$. Given that the centre of mass of the flask and liquid together is a distance of $\frac{15}{22} h$ from the open end of the flask,
(b) find the value of $k$.
(c) Explain why it may be advantageous to make the base of the flask from a more dense material.
(2 marks)
6. A particle $P$ of mass 2.5 kg is moving with simple harmonic motion in a straight line between two points $A$ and $B$ on a smooth horizontal table. When $P$ is 3 m from $O$, the centre of the oscillations, its speed is $6 \mathrm{~m} \mathrm{~s}^{-1}$. When $P$ is 2.25 m from $O$, its speed is $8 \mathrm{~m} \mathrm{~s}^{-1}$.
(a) Show that $A B=7.5 \mathrm{~m}$.
(b) Find the period of the motion.
(c) Find the kinetic energy of $P$ when it is 2.7 m from $A$.
(d) Show that the time taken by $P$ to travel directly from $A$ to the midpoint of $O B$ is $\frac{\pi}{4}$ seconds.
(4 marks)

## END

