## GCE Examinations

## Advanced Subsidiary / Advanced Level

## Mechanics <br> Module M2

## Paper F

## MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.
Accuracy marks (A) can only be awarded when a correct method has been used.
(B) marks are independent of method marks.

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1. $\mathbf{I}=\Delta$ mom. $=0.5[(13 \mathbf{i}+7 \mathbf{j})-(5 \mathbf{i}-8 \mathbf{j})] \quad$ M1 A1

$$
\begin{aligned}
& =0.5(8 \mathbf{i}+15 \mathbf{j}) \\
& \text { mag. of } \mathbf{I}=0.5 \sqrt{ }\left(8^{2}+15^{2}\right)=8.5 \mathrm{Ns}
\end{aligned}
$$

A1
M1 A1
2. (a) change in $\mathrm{KE}=\frac{1}{2} 1000\left(10^{2}-20^{2}\right)={ }^{-} 150000 \mathrm{~J}$

M1 A1
change in $\mathrm{PE}=1000(9.8)(200 \sin \theta)=280000 \mathrm{~J}$
M2 A1
change in ME $=280000-150000=$ increase of 130000 J
A1
(b) air resistance

B1
friction
B1
3. (a) $s=t\left(2 t^{2}-13 t+20\right)=t(2 t-5)(t-4)$

M1 A1
particle at $O$ when $s=0 \therefore$ at $t=0, \frac{5}{2}, 4$ seconds
M1 A1
(b) at rest when $v=0, v=\frac{\mathrm{d} s}{\mathrm{~d} t}=6 t^{2}-26 t+20$

M1 A1
$\therefore 3 t^{2}-13 t+10=0,(t-1)(3 t-10)=0$
M1
$t=1, \frac{10}{3}$ seconds
A1
4. (a)

mom. about $B: 6 g \cos 30^{\circ}-R .2 \cos 30^{\circ}=0$
M1 A1
$\therefore R=3 g$
A1
mom. about $A: 6 g \cos 30^{\circ}-S .2=0$
M1 A1
$\therefore S=\frac{3}{2} \sqrt{ } 3 g$
A1
(b) resolve $\rightarrow: \mu S \sin 60^{\circ}-S \sin 30^{\circ}=0$

$$
\mu=\frac{\frac{1}{2}}{\frac{\sqrt{3}}{2}}=\frac{1}{\sqrt{3}}
$$

A1
(9)
5. (a) at max. ht., $v_{y}=0 \therefore 0=(22 \sin \alpha)^{2}-2 g s$

M1 A1
$s_{y}=\frac{\left(22 \cdot \frac{7}{8}\right)^{2}}{2 g}=18.91$
M1
starts 1.6 m above $P$ so max. ht. above ground $=20.5 \mathrm{~m}(3 \mathrm{sf})$
(b) $s_{y}={ }^{-} 1.4 \quad \therefore u t \sin \alpha-\frac{1}{2} g t^{2}={ }^{-} 1.4$
$\frac{77}{4} t-4.9 t^{2}={ }^{-1.4}$ M1 A1
$14 t^{2}-55 t-4=0 \quad \therefore(14 t+1)(t-4)=0$
M1
$t=4$ in this case $\therefore$ ball in flight for 4 seconds
(c) $s_{x}=u t \cos \alpha=22 \times 4 \times \frac{\sqrt{15}}{8}=11 \sqrt{ } 15=42.6$
max. dist. fielder can run is $4 \times 6=24 \mathrm{~m}$
M1 A1
max. initial dist. between fielder and ball $=42.6+24=66.6 \mathrm{~m}(3 \mathrm{sf})$
A1
A1
6. (a) $\frac{1}{2} a$, since masses on $A D$ are equal to mass at $B$
(b)

| portion | mass | $y$ | $m y$ |
| :--- | :--- | :--- | :--- |
| lamina | $8 m$ | $a$ | $8 m a$ |
| particle at $A$ | $2 m$ | 0 | 0 |
| particle at $B$ | $6 m$ | 0 | 0 |
| particle at $D$ | $4 m$ | $2 a$ | $8 m a$ |
| total | $20 m$ | $\bar{y}$ | $16 m a$ |

$$
\begin{array}{ll}
y \text { coords. taken vert. from } A B & \text { M2 A1 } \\
\bar{y}=\frac{16 m a}{20 m}=\frac{4}{5} a & \text { M1 A1 }
\end{array}
$$

(c)

| portion | mass | $x$ | $m x$ |
| :--- | :--- | :--- | :--- |
| lamina | $8 m$ | $\frac{a}{2}$ | $4 m a$ |
| particle at $A$ | $2 m$ | 0 | 0 |
| particles at $B$ | $(6+k) m$ | $a$ | $(6+k) m a$ |
| particle at $D$ | $4 m$ | 0 | 0 |
| total | $(20+k) m$ | $\bar{x}$ | $(10+k) m a$ |

$x$ coords. taken horiz. from $A D$
M1 A1

$$
\bar{x}=\frac{(10+k) m a}{(20+k) m}=\frac{(10+k) a}{(20+k)}
$$


$\tan 45^{\circ}=\frac{16 a}{(10+k) a} \therefore \quad 1=\frac{16}{10+k} \quad$ giving $k=6$
M2 A1
7. (a) cons. of mom: $7 u_{1}+4 u_{2}=7\left(\frac{u_{1}}{2}\right)+4 v_{2}$

M1

$$
8 v_{2}=7 u_{1}+8 u_{2}
$$

A1
$\frac{v_{2}-\frac{1}{2} u_{1}}{u_{1}-u_{2}}=e \quad \therefore v_{2}=e u_{1}-e u_{2}+\frac{1}{2} u_{1}$
M1 A1
eliminate $v_{2}$ giving $7 u_{1}+8 u_{2}=8 e u_{1}-8 e u_{2}+4 u_{1}$
M1 A1
$8 u_{2}+8 e u_{2}=8 e u_{1}-3 u_{1} \therefore 8 u_{2}(e+1)=u_{1}(8 e-3)$
A1
(b) sub. in for $u_{1}$ and $u_{2}: 24(e+1)=14(8 e-3)$

M1
$24 e+24=112 e-42$ giving $e=\frac{3}{4}$
M1 A1
(c) speeds of $A, B$ after impact are $v_{1}$ and $v_{2}$ resp.
$v_{1}=7 \mathrm{~ms}^{-1}, v_{2}=\left(\frac{7}{8}\right) 14+3=15.25 \mathrm{~ms}^{-1}$
A1
original $\mathrm{KE}=\frac{1}{2} \times 7 \times 14^{2}+\frac{1}{2} \times 4 \times 3^{2}=704 \mathrm{~J}$
M1 A1
final $\mathrm{KE}=\frac{1}{2} \times 7 \times 7^{2}+\frac{1}{2} \times 4 \times 15.25^{2}=636.625 \mathrm{~J}$
M1 A1
$\%$ KE lost $=\frac{704-636.625}{704} \times 100=9.6 \%(2 \mathrm{sf})$
M1 A1

Total

## Performance Record - M2 Paper F

| Question no. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic(s) | $\begin{aligned} & \hline \mathbf{i , j} \\ & \text { impulse } \end{aligned}$ | energy | variable <br> accel. | statics | projectiles | centre of <br> mass | collisions, energy |  |
| Marks | 5 | 8 | 8 | 9 | 12 | 16 | 17 | 75 |
| Student |  |  |  |  |  |  |  |  |
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