GCE Examinations Advanced / Advanced Subsidiary

Core Mathematics C4

Paper D Time: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

- Answer **all** the questions.
- Give non-exact numerical answers correct to 3 significant figures, unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are permitted to use a graphic calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 72.
- You are reminded of the need for clear presentation in your answers.



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1. Evaluate

$$\int_{0}^{\pi} \sin x \, (1 + \cos x) \, \mathrm{d}x.$$
 [4]

2. *(i)* Simplify

$$\frac{x^2 + 7x + 12}{2x^2 + 9x + 4}.$$
[2]

(ii) Express

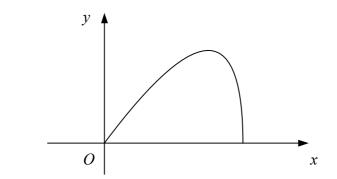
$$\frac{x+4}{2x^2+3x+1} - \frac{2}{2x+1}$$

as a single fraction in its simplest form. [3]

3. Find the exact value of

4.

$$\int_{1}^{3} x^{2} \ln x \, \mathrm{d}x.$$
 [5]



The diagram shows the curve with parametric equations

$$x = t + \sin t$$
, $y = \sin t$, $0 \le t \le \pi$.

(i) Find
$$\frac{dy}{dx}$$
 in terms of t. [3]

(*ii*) Find, in exact form, the coordinates of the point where the tangent to the curve is parallel to the *x*-axis. [3]

5. Given that y = -2 when x = 1, solve the differential equation

$$\frac{\mathrm{d}y}{\mathrm{d}x} = y^2 \sqrt{x} \; ,$$

giving your answer in the form y = f(x).

- 6. (i) Find $\int \tan^2 3x \, dx$. [3]
 - (*ii*) Using the substitution $u = x^2 + 4$, evaluate

$$\int_0^2 \frac{5x}{(x^2+4)^2} \, \mathrm{d}x.$$
 [6]

7. A curve has the equation

$$3x^2 - 2x + xy + y^2 - 11 = 0.$$

The point *P* on the curve has coordinates (-1, 3).

(i)	Show that the normal to the curve at <i>P</i> has the equation $y = 2 - x$.	[6]
(ii)	Find the coordinates of the point where the normal to the curve at P meets the curve again.	[4]

8. The line l_1 passes through the points A and B with position vectors $(-3\mathbf{i} + 3\mathbf{j} + 2\mathbf{k})$ and $(7\mathbf{i} - \mathbf{j} + 12\mathbf{k})$ respectively, relative to a fixed origin.

(*i*) Find a vector equation for
$$l_1$$
. [2]

The line l_2 has the equation

$$\mathbf{r} = (5\mathbf{j} - 7\mathbf{k}) + \mu(\mathbf{i} - 2\mathbf{j} + 7\mathbf{k}).$$

The point C lies on l_2 and is such that AC is perpendicular to BC.

(*ii*) Show that one possible position vector for C is (i + 3j) and find the other. [8]

Assuming that C has position vector (i + 3j),

(*iii*) find the area of triangle *ABC*, giving your answer in the form $k\sqrt{5}$. [3]

Turn over

$$f(x) = \frac{8-x}{(1+x)(2-x)}, |x| < 1.$$

- (*i*) Express f(x) in partial fractions.
- *(ii)* Show that

$$\int_0^{\frac{1}{2}} f(x) dx = \ln k,$$

where k is an integer to be found.

(*iii*) Find the series expansion of f(x) in ascending powers of x up to and including the term in x^3 , simplifying each coefficient. [6]

[3]

[4]

9.