GCE Examinations Advanced / Advanced Subsidiary

Core Mathematics C1

Paper L Time: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

- Answer **all** the questions.
- Give non-exact numerical answers correct to 3 significant figures, unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are not permitted to use a calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 72.
- You are reminded of the need for clear presentation in your answers.



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1. Solve the inequality

$$4(x-2) < 2x+5.$$
[3]

2.
$$f(x) = 2 - x - x^3$$
.

Show that f(x) is decreasing for all values of x. [4]

3. *(i)* Solve the equation

$$y^2 + 8 = 9y.$$
 [2]

(ii) Hence solve the equation

$$x^3 + 8 = 9x^{\frac{3}{2}}.$$
 [3]

4. Given that

(i)

$$y = \frac{x^4 - 3}{2x^2},$$
find $\frac{dy}{dx},$
[4]

(*ii*) show that
$$\frac{d^2 y}{dx^2} = \frac{x^4 - 9}{x^4}$$
. [2]

5. Find the pairs of values (x, y) which satisfy the simultaneous equations

$$3x^2 + y^2 = 21$$

 $5x + y = 7$ [7]

- 6. (i) Evaluate $(5\frac{4}{9})^{-\frac{1}{2}}$. [2]
 - (*ii*) Find the value of x such that

$$\frac{1+x}{x} = \sqrt{3} ,$$

giving your answer in the form $a + b\sqrt{3}$ where a and b are rational. [5]

7. The straight line *l* passes through the point P(-3, 6) and the point Q(1, -4).

(*i*) Find an equation for *l* in the form ax + by + c = 0, where *a*, *b* and *c* are integers. [4] The straight line *m* has the equation 2x + ky + 7 = 0, where *k* is a constant. Given that *l* and *m* are perpendicular,

(*ii*) find the value of
$$k$$
. [4]

8. (i) Describe fully a single transformation that maps the graph of $y = \frac{1}{x}$ onto the graph of $y = \frac{3}{x}$. [2]

(*ii*) Sketch the graph of
$$y = \frac{3}{x}$$
 and write down the equations of any asymptotes. [3]

(*iii*) Find the values of the constant *c* for which the straight line y = c - 3x is a tangent to the curve $y = \frac{3}{x}$. [4]

Turn over

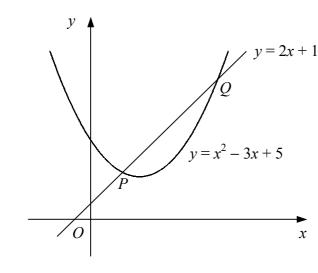
9. The circle *C* has the equation

$$x^2 + y^2 - 12x + 8y + 16 = 0.$$

- (i) Find the coordinates of the centre of C. [2]
- (ii) Find the radius of C. [2]
- (iii) Sketch C. [2]

Given that C crosses the x-axis at the points A and B,

(*iv*) find the length AB, giving your answer in the form $k\sqrt{5}$. [4]



The diagram shows the curve $y = x^2 - 3x + 5$ and the straight line y = 2x + 1. The curve and line intersect at the points *P* and *Q*.

(i)	Using algebra, show that P has coordinates (1, 3) and find the coordinates of Q .	[4]
(ii)	Find an equation for the tangent to the curve at <i>P</i> .	[4]
(iii)	Show that the tangent to the curve at <i>Q</i> has the equation $y = 5x - 11$.	[2]

(iv) Find the coordinates of the point where the tangent to the curve at *P* intersects the tangent to the curve at *Q*.[3]

10.