## GCE Examinations

## Advanced / Advanced Subsidiary

## Core Mathematics C1

## Paper L

## Time: 1 hour 30 minutes

## INSTRUCTIONS TO CANDIDATES

- Answer all the questions.
- Give non-exact numerical answers correct to 3 significant figures, unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are not permitted to use a calculator in this paper.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks for this paper is 72 .
- You are reminded of the need for clear presentation in your answers.

1. Solve the inequality

$$
\begin{equation*}
4(x-2)<2 x+5 \tag{3}
\end{equation*}
$$

2. 

$$
\begin{equation*}
\mathrm{f}(x)=2-x-x^{3} \tag{4}
\end{equation*}
$$

Show that $\mathrm{f}(x)$ is decreasing for all values of $x$.
3. (i) Solve the equation

$$
\begin{equation*}
y^{2}+8=9 y . \tag{2}
\end{equation*}
$$

(ii) Hence solve the equation

$$
\begin{equation*}
x^{3}+8=9 x^{\frac{3}{2}} . \tag{3}
\end{equation*}
$$

4. Given that

$$
y=\frac{x^{4}-3}{2 x^{2}}
$$

(i) find $\frac{\mathrm{d} y}{\mathrm{~d} x}$,
(ii) show that $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}=\frac{x^{4}-9}{x^{4}}$.
5. Find the pairs of values $(x, y)$ which satisfy the simultaneous equations

$$
\begin{align*}
& 3 x^{2}+y^{2}=21 \\
& 5 x+y=7 \tag{7}
\end{align*}
$$

6. (i) Evaluate $\left(5 \frac{4}{9}\right)^{-\frac{1}{2}}$.
(ii) Find the value of $x$ such that

$$
\frac{1+x}{x}=\sqrt{3}
$$

giving your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are rational.
7. $\quad$ The straight line $l$ passes through the point $P(-3,6)$ and the point $Q(1,-4)$.
(i) Find an equation for $l$ in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.

The straight line $m$ has the equation $2 x+k y+7=0$, where $k$ is a constant.
Given that $l$ and $m$ are perpendicular,
(ii) find the value of $k$.
8. (i) Describe fully a single transformation that maps the graph of $y=\frac{1}{x}$ onto the graph of $y=\frac{3}{x}$.
(ii) Sketch the graph of $y=\frac{3}{x}$ and write down the equations of any asymptotes.
(iii) Find the values of the constant $c$ for which the straight line $y=c-3 x$ is a tangent to the curve $y=\frac{3}{x}$.
9. The circle $C$ has the equation

$$
x^{2}+y^{2}-12 x+8 y+16=0 .
$$

(i) Find the coordinates of the centre of $C$.
(ii) Find the radius of $C$.
(iii) Sketch $C$.

Given that $C$ crosses the $x$-axis at the points $A$ and $B$,
(iv) find the length $A B$, giving your answer in the form $k \sqrt{5}$.
10.


The diagram shows the curve $y=x^{2}-3 x+5$ and the straight line $y=2 x+1$.
The curve and line intersect at the points $P$ and $Q$.
(i) Using algebra, show that $P$ has coordinates $(1,3)$ and find the coordinates of $Q$.
(ii) Find an equation for the tangent to the curve at $P$.
(iii) Show that the tangent to the curve at $Q$ has the equation $y=5 x-11$.
(iv) Find the coordinates of the point where the tangent to the curve at $P$ intersects the tangent to the curve at $Q$.

