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## <u>Proof</u>

- 1. The  $n^{th}$  even number is 2n.
  - a. The next even number can be written as 2n + 2Explain why
  - b. Write down an expression, in terms of n, for the next even number after 2n + 2.
  - c. Show algebraically that the sum of any 3 consecutive even numbers is always a divisible by 6

(3 Marks)

- 2. Prove, using algebra, that the sum of two consecutive integers is always odd.
- (2 Marks)
  - 3. Prove algebraically that  $(4n + 2)^2 (2n + 2)^2$  is a multiple of 4 for all positive integers.

(4 Marks)

4. Prove that  $(2n + 3)^2 - (2n - 3)^2$  is a multiple of 8 for all positive integers of *n*.

(3 Marks)

5. Prove algebraically that (3n + 1)(n + 3) - n(3n + 7) = 3(n + 1)

(3 Marks)

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6. Prove Algebraically that  $\frac{1}{8}(4n+1)(n+8) - \frac{1}{8}n(4n+1) = 4n+1$ 

(4 Marks)

7. Prove algebraically that the sum of two consecutive square numbers is twice the product of two consecutive numbers +1.

(4 Marks)

8. Prove algebraically that the sum of 4 consecutive square numbers is divisible by 4 remainder 2.

(5 Marks)

9. Show that the difference between  $14^{20}$  and  $21^{2}$  is a multiple of 7.

(3 Marks)

10. Tom says that 7x - (2x + 3)(x + 2) is always negative. Is he correct? Explain your answer.

(3 Marks)

11. Show that  $3^{60} - 25$  is not a prime.

(3 Marks)