## TIER

## Mathematics test

## Paper 2 <br> Calculator allowed

## 2004

Please read this page, but do not open your booklet until your teacher tells you to start. Write your name and the name of your school in the spaces below.

First name $\qquad$
Last name $\qquad$
School

## Remember

- The test is 1 hour long.
- You may use a calculator for any question in this test.
- You will need: pen, pencil, rubber, ruler, a pair of compasses and a scientific or graphic calculator.
- $\quad$ Some formulae you might need are on page 2.
- This test starts with easier questions.
- Try to answer all the questions.
- Write all your answers and working on the test paper do not use any rough paper. Marks may be awarded for working.
- Check your work carefully.
- Ask your teacher if you are not sure what to do.

|  | For marker's | Total marks |
| :--- | :--- | :--- |
| use only | Borderline check |  |
|  |  |  |

## Instructions

## Answers

This means write down your
《 answer or show your working and write down your answer.

## Calculators

You may use a calculator to answer any question in this test.

## Formulae

You might need to use these formulae
Trapezium


Area $=\frac{1}{2}(a+b) h$

## Prism



Volume $=$ area of cross-section $\times$ length

1. Look at this shape made from six cubes.

Four cubes are white.
Two cubes are grey.


Part of the shape is rotated through $90^{\circ}$ to make the shape below.


After another rotation of $90^{\circ}$, the shape is a cuboid.
Draw this cuboid on the grid below.
2. There are high mountains in Nepal.

At different heights, the temperature is different.

The graph shows information about temperatures in one month.


For example:
At 1000 metres, the maximum temperature is $30^{\circ} \mathrm{C}$.
(a) At $\mathbf{3 0 0 0}$ metres, what is the minimum temperature?
$\qquad$
(b) At $\mathbf{5 0 0 0}$ metres, the minimum temperature is $-\mathbf{3}^{\circ} \mathrm{C}$.

The range in temperature is $15^{\circ} \mathrm{C}$.

On the graph above, draw a bar to show this information.
3. (a) A pupil measured the angles in a triangle.

She said:
The angles are $30^{\circ}, 60^{\circ}$ and $100^{\circ}$

Could she be correct? Tick $(\checkmark)$ Yes or No.
$\geqslant$ $\square$
$\square$ No

Explain your answer.

(b) This diagram is not drawn accurately.

Calculate the size of angle $m$
Show your working.
-
4. The diagram shows part of a number grid. The grid has 6 columns. All the prime numbers in the grid are circled.

| 43 | 44 | 45 | 46 | 47 | 48 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 37 | 38 | 39 | 40 | 41 | 42 |
| 31 | 32 | 33 | 34 | 35 | 36 |
| 25 | 26 | 27 | 28 | 29 | 30 |
| 19 | 20 | 21 | 22 | 23 | 24 |
| 13 | 14 | 15 | 16 | 17 | 18 |
| 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 |

(a) 35 is not circled.

Explain why 35 is not a prime number.
(b) There are no prime numbers circled in column Y .

Explain how you know there will never be a prime number in column Y .
(c) There is one prime number circled in column X .

Explain how you know there will never be another prime number in column $X$.
5. A box contains bags of crisps.

Each bag of crisps weighs $\mathbf{2 5}$ grams.

Altogether, the bags of crisps inside the box weigh 1 kilogram.


How many bags of crisps are inside the box?
6. The square grid below shows a quadrilateral that has four right angles.

(a) Draw a quadrilateral that has exactly two right angles.

(b) Draw a quadrilateral that has exactly one right angle.

7. Shoe sizes in Britain and Germany are different.

The rule below shows how to change a British shoe size to a German shoe size.

Multiply the British shoe size by 1.25 ,
then add 32, then round the answer to the nearest whole number.

Tom's British shoe size is 7, Karl's British shoe size is $\mathbf{7} \frac{\mathbf{1}}{\mathbf{2}}$
They say:
'The rule shows that we have the same German shoe size'.

Are they correct? Tick $(\checkmark)$ Yes or No.

$\square$ Yes $\square$ No

Show working to explain your answer.
8. (a) The square and the rectangle below have the same area.


Work out the value of $y$

(b) The triangle and the rectangle below have the same area.


Not drawn accurately

Work out the value of $w$
Show your working.

9. (a) In 1976 the average yearly wage was $£ \mathbf{3 2 7 5}$

On average, people spent $17 \%$ of $£ 3275$ on their family holiday.

How much is $17 \%$ of $£ 3275$ ?
Show your working.

## £

2 marks
(b) In 2001 the average yearly wage was $£ \mathbf{2 1 8 4 2}$

On average, people spent $£ \mathbf{1} 644$ on their family holiday.

What percentage of the average yearly wage is that?
Show your working.
\%
10. The graph shows a straight line.

(a) Fill in the table for some of the points on the line.


1 mark
(b) Write an equation of the straight line.


1 mark
(c) On the graph, draw the straight line that has the equation $\boldsymbol{x}+\boldsymbol{y}=\mathbf{6}$
11.

There are $\mathbf{2 0}$ questions in a quiz.
A correct answer scores 2 points. An incorrect answer loses 1 point.
A question not answered scores 0 points. A negative total is possible.
(a) What are the maximum and minimum points you could get on the quiz?
maximum
minimum
(b) A pupil answers 10 of the 20 questions. 8 are correct.

How many points does he score?
(c) Complete the table to show 3 different ways to score 24 points.

| Number of <br> answers that are <br> correct | Number of <br> answers that are <br> incorrect | Number of <br> questions that are <br> not answered |
| :---: | :---: | :---: |
| 12 | 0 | 8 |
|  |  |  |
|  |  |  |

12. (a) The cross-section of a cylindrical cotton reel is a circle. The diameter of this circle is $\mathbf{3 c m}$.

What is the circumference of this circle?

$\qquad$
(b) 91 metres of cotton goes round the cotton reel.

About how many times does the cotton go round the reel?

Show your working, and give your answer
 to the nearest ten.
13. Doctors sometimes use this formula to calculate how much medicine to give a child.

$$
c=\frac{a y}{12+y} \quad \begin{array}{ll}
c \text { is the correct amount for a child, in } \mathrm{ml} \\
a \text { is the amount for an adult, in } \mathrm{ml} \\
y \text { is the age of the child, in years }
\end{array}
$$

(a) A child who is 4 years old needs some medicine.

The amount for an adult is $\mathbf{2 0} \mathbf{m l}$.

Use the formula to work out the correct amount for this child.
You must show your working.
(b) Another child needs some medicine.

The amount for an adult is $\mathbf{3 0} \mathbf{m l}$.

The correct amount for this child is $\mathbf{1 5} \mathbf{m l}$.

How old is this child? Show your working.
14. (a) A teacher asked her pupils if they recycled newspapers and glass.

The pie chart shows the results.


5 pupils answered 'Neither'.

How many pupils answered 'Newspapers only'?
Show your working.
pupils
2 marks
(b) The teacher asked a different class if they recycled newspapers and glass.

There were 24 pupils in the class.
9 pupils answered 'Newspapers only'.
On a pie chart, what would the angle be for the sector 'Newspapers only'? Show your working.

。
15. The heights of Russian dolls are in the ratio $4: 6: 7$

(a) In a set of dolls, the height of the middle doll is $9 \mathbf{c m}$.

What are the heights of the other dolls?

(b) In another set of dolls, the height of the tallest doll is $\mathbf{9} \mathbf{c m}$.

What are the heights of the other dolls?
Show your working, and give your answers to 1 decimal place.


16. Altogether, I have 10 bags of sweets.

The mean number of sweets in the bags is 41

The table shows how many sweets there are in 9 of the bags.

| Number of sweets <br> in a bag | Frequency |
| :---: | :---: |
| 39 | 3 |
| 40 | 2 |
| 41 | 1 |
| 42 | 1 |
| 43 | 0 |
| 44 | 2 |

Calculate how many sweets there are in the 10th bag.
You must show your working.
17. The diagram shows the net for a right-pyramid with a regular pentagon as its base.

The net is constructed using five straight lines.

(a) Without measuring, explain why angle $a$ must be $108^{\circ}$
(b) Calculate the size of angle $b$.

You must show your working.
-
(c) On these nets, the point marked P lies on the perpendicular bisector of a side of the pentagon.



On side CD of the regular pentagon below, use compasses and a straight edge to construct the perpendicular bisector.

You must leave in your construction lines.

18. Kali uses a running machine to keep fit.

The simplified distance-time graph shows how she used the machine during one run.


Use the graph to answer these questions.
(a) Between 0930 and 0940, what was her speed in kilometres per hour?

(b) Throughout the run, for how many minutes did she travel at this speed?
minutes
(c) At 0940, she increased her speed.

By how many kilometres per hour did she increase her speed?
19. Some numbers are smaller than their squares.

For example: $7<7^{2}$

Which numbers are equal to their squares?

2 marks
20. Is it possible to have a triangle with the angle and lengths shown below? Show calculations then tick $(\checkmark)$ Yes or No.

21. Look at these expressions.


What value of $y$ makes the two expressions equal?
Show your working.

$$
y=
$$

END OF TEST

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