## AQA, Edexcel, OCR

## A Level

## A Level Mathematics

Newton-Raphson method and other recurrence relations

Name:

# M 

## Total Marks:

1) Write the first four terms of the recurrence relationship defined as

$$
\begin{equation*}
U_{n+1}=3 U_{n}+1 \tag{2}
\end{equation*}
$$

where $U_{0}=3$
2) A relationship is given as

$$
R_{n+1}=\left(A R_{n}+B\right)
$$

we know that
$R_{0}=4, R_{1}=6, R_{2}=8, R_{3}=10$
Determine a general solution and the value for $R_{4}$.
3) i) Use the Newton-Raphson method to find the first four terms of the following:

$$
x^{3}+3 x^{2}-8 x+0.8=0
$$

You may use $x_{0}=0$
ii) Explain why $x_{0}=\sqrt{\frac{11}{3}}-1$ is not a viable option.
4) What is the value of the term $U_{56}$ for the relationship

$$
\begin{equation*}
U_{n+1}=-U n^{n} \tag{2}
\end{equation*}
$$

where $U_{0}=1$
5) i) Draw a flow chart showing how to estimate a solution to $x^{2}+3 x-6=0$ using a recurrence process.
ii) Calculate one of the roots to 2 dp .
6) i) Using an iterative process find one of the non-integer roots of

$$
\begin{equation*}
2 x^{3}+2 x^{2}-10 x=4 \tag{4}
\end{equation*}
$$

ii) Show that one of the roots is 2 .
7) Use the Newton-Raphson method to find one of the solutions to

$$
\begin{equation*}
x^{2}+5 x-11=0 \tag{2}
\end{equation*}
$$

You may use $x_{0}=1.6$
8) Estimate $\sqrt{2}$ using the Newton Raphson method.

