

(a) Define angular velocity.

Solution: Rate of change of angular displacement: $\omega=\theta/t$

(b) Calculate the angular velocity of a car travelling at 30 kmhr^{-1} around a roundabout whose radius is 50 m.

Solution: $\frac{1}{6}$ rad s⁻¹

(c) Give three examples of situations in which centripetal forces arise, detailing precisely which forces [3 contribute to the centripetal force.

Solution: Anything valid e.g. vehicles on banked turns (reaction/friction force), satellites in orbit (gravity), yoyos being whirled (tension).

1.

[3]

[1]

[3]

(d) Outline a simple experiment you could perform to explore circular motion. As well as describing the experimental setup, explain how you would calculate the centripetal force for different radii, speeds and masses.

Solution:

Two masses, M and m are attached to either end of a piece of string. This passes through a tube. Attached to the string on the side of the larger mass, M, is a paperclip. Holding the tube, mass m is swung in circles. The cetripetal force here is the weight of mass M. tube, mass *m* is swing in cherch. The compositive noise is the mass $F = Mg = \frac{mv^2}{r}$ Manipulating this equation allows us to evaluate the required quantities.

2. A cyclist is travelling around a bend with a radius of 15 m on a horizontal road. The frictional force is related to the reaction force from the ground and the coefficient of friction by the equation $F = \mu R$, where μ is the coefficient of friction and R is the reaction force.

Total for Question 2: 10

(a) In dry conditions $\mu = 0.5$. Calculate the maximum speed at which the cyclist can travel if he is not to fall off. [3]

Solution: 8.6 ms^{-1}

(b) The reaction of the surface and the frictional force both act on the cyclist, but at a distance from the centre of mass. They therefore provide a torque. Qualitatively, explain why a cyclist leaning inwards when cycling around bends helps to prevent these torques destabilising the bike.

Solution: 3 forces acting on the bike: weight, friction and reaction of the surface. The first acts through the COM and therefore doesn't provide a torque. The other two act from the same point. Given that their magnitudes can't be changed, the only way to balance them is to change the angle between the direction of the force and the line intersecting the COM and the point through which they act.

(c) Rosie is feeling particularly brave and decides to conduct an experiment to calculate the coefficient of friction when the road surface is wet. She uses five different bends, each with a different radius. For each, she records her speed at the point her wheels begin to slide. Using the data in the table below, plot a graph and calculate the coefficient of friction.

Solution: Should plot v^2 against radius. Best fit line should go through origin. Gradient is μg . $\mu \approx 0.2$

bend radius / m	speed / $\rm ms^{-1}$
9	45
4.5	15
11	60
6.5	20
3	5

[4]

3. A conical pendulum is simply a mass suspended from a point that traces out a horizontal circle, rather than one that swings back and forth.

Total for Question 3: 10

(a) Draw a free-body diagram for the mass.

Solution: Two forces: weight mg acting downwards and tension T acting along the suspending string towards the attachment point, at an angle θ from the vertical.

(b) What provides the centripetal force in this situation?

Solution: Tension in the attaching string.

(c) Express the tension in the string in terms of the mass, the mass's velocity and the radius of the [2] circle in which it moves.

Solution: $\frac{mv^2}{r} = T\sin\theta$

[1]

[1]

(d) By balancing the weight with the tension in the string, show that the speed of the bob is given by $v = \sqrt{rg \tan \theta}$

Solution: Balance: $mg = T \cos \theta$ Divide this equation by answer to previous question: $\frac{\sin \theta}{\cos \theta} = \frac{v^2}{rg}$ Rearrange to get required format.

(e) By considering the circumference of the circle traced out by the bob, determine whether or not the angular velocity depends on the bob's mass. Justify your answer.

Solution: It does not: $\omega = \sqrt{\frac{g \tan \theta}{r}}$

[3]

[3]