



GCSE MARKING SCHEME

AUTUMN 2021

GCSE MATHEMATICS – COMPONENT 2 (HIGHER TIER) C300UB0-1

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INTRODUCTION

This marking scheme was used by WJEC for the 2021 examination. It was finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conference was held shortly after the paper was taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conference was to ensure that the marking scheme was interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conference, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about this marking scheme.

EDUQAS GCSE MATHEMATICS

AUTUMN 2021 MARK SCHEME

GCSE (9-1) Mathematics		
Component 2: Higher Tier	Mark	Comment
1.*(a)		
6x - x = 5 + 1 oe	B1	
$x = \frac{6}{5}$ oe, ISW	B1	FT from $ax = 6$, $a \neq 1$ or $5x = b$ accept $\frac{6}{2}$ or $\frac{b}{2}$ but if on FT either simplifies to an
		a 5 integer the answer must be given as an integer.
		x = can be omitted but must not be wrong if there.
		Correct answer implies first B1.
		Final answer of $x = \frac{-6}{-5}$ is B0.
		Maximum of 1 mark if not fully correct
1.(b) A correct equation e.g. $2x + 10 = 116$ $2(x + 5) = 116$ $x + 5 = 58$ $x = 116 \div 2 - 5$	B2	B1 for 2(<i>x</i> + 5) or 2x + 10
53	B1	
		If no marks award: SC2 for $x = 55.5$ following $2x + 5 = 116$ SC1 for $2x + 5 = 116$
	(5)	
2.* 130 × 1.06 ¹⁰	M2	May be seen in stages. M1 for sight of 130 × 1.06 (= 137.8)
(£)232.81	A1	CAO An answer of (£)208 (simple interest) from use of $130 \times 0.06 \times 10$ +130 is awarded M1 A0
	(3)	
3.*		
(radius =) $\frac{40.841}{2\pi}$ (= 6.50)	B2	B1 for $2\pi r = 40.841$ or $\pi d = 40.841$ or $\frac{40.841}{\pi}$ or 13.0
(Area =) $\pi \times \left(\frac{40.841}{2\pi}\right)^2 (=\pi \times 6.5^2)$	M1	FT 'their derived radius'
132.7() or 133 (cm ²)	A1 (4)	CAO correct answer implies all previous marks

4.*(a)		
$\sin^{-1}\left(\frac{0.5}{6}\right)$	M2	M1 for $\sin() = \frac{0.5}{6}$
4.7(8)	A1	Unsupported 4.7(8) is awarded no marks
4.(b) $\sqrt{1.8^2 - 0.6^2}$ (= 1.69705)	M2	M1 for $1.8^2 - 0.6^2$ or $x^2 + 0.6^2 = 1.8^2$
$\frac{\sqrt{1.8^2 - 0.6^2} \times 0.6}{2}$	M1	Allow FT from use of $\sqrt{1.8^2 + 0.6^2}$ (= 1.897)
2 × 2.5	m1	
1.27() or 1.28 or 1.3 (m ³)	A1	CAO
5.*(a)(i) $\begin{pmatrix} 6 \\ -1 \end{pmatrix}$	B2	B1 for sight of $\begin{pmatrix} 3 \\ -5 \end{pmatrix} + \begin{pmatrix} 3 \\ 4 \end{pmatrix}$ Allow B1 for $\begin{pmatrix} 6 \\ -1 \end{pmatrix}$ written incorrectly e.g. $\begin{pmatrix} 6 \\ -1 \end{pmatrix}$
5.(a)(ii) Correct shape <i>B</i> drawn at (2, 1), (2, 4), (3, 4), (3, 2), (4, 2), (4, 1),	В2	or correct FT; FT 'their $\begin{pmatrix} 6 \\ -1 \end{pmatrix}$, B1 for a translation attempted with at least 4 vertices correct or shape <i>A</i> correctly translated by $\begin{pmatrix} 6 \\ y \end{pmatrix}$ where $y \neq -1$ or $\begin{pmatrix} x \\ -1 \end{pmatrix}$ where $x \neq 6$ If no marks in (a) then award SC1 for a clear attempt to translate by $\begin{pmatrix} 3 \\ -5 \end{pmatrix}$ and $\begin{pmatrix} 3 \\ 4 \end{pmatrix}$.
5.(b) Reflection (in the line) $y = x$	B2	B1 for either stating a reflection or giving the equation $y = x$ Award no marks if more than one transformation indicated If no marks then award SC1 for a correct diagram with the line $y = x$ drawn.
	(6)	

6.7 $a + 4c = 16.30$ and $2a + 3c = 19.10$ B1May use other letters or words throughoutMethod to eliminate an unknown e.g. equal coefficients and subtractionM1FT their equations provided one is correct and the other is linear in the same pair of unknownsAllow one error in one term, but not in the equated coefficientsAllow one error in one term, but not in the equated coefficientsFinds the otherFT inds the other unknown or finds $16.3(0) + 19.1(0) - 6 \times 2.7(0)$ A1CAO $a = 5.5(0)$ or $c = 2.7(0)$ (E) 19.2(0)B1FT 3('their derived a') + ('their derived c') or $35.4 - 6 \times$ their derived c' provided at least one mark previously awarded. Unsupported 19.2(0) is awarded no marks7.(a) $7x^2 + 5x - 42x - 30$ B2B1 for any three terms correct; $nx^2 - 37x + m$ implies two terms correct if not from wrong working7.(b) $(y - 2)(y + 4)$ B2B1 for $(y \dots 2)(y \dots 4)$ 8.(a) Midpoints 30, 60, 90, 125 $30 \times 68 + 60 \times 186 + 90 \times 238 + 125 \times 108$ $(2040 + 11160 + 21420 + 13500 = 48120)$ M1FT 'their midpoints' provided at least 3 of 'their 4 midpoints 30, 60, 90, 125 $30 \times 68 + 60 \times 186 + 90 \times 238 + 125 \times 108$ $(2040 + 11160 + 21420 + 13500 = 48120)$ M1600 (Best estimate) 77.2(minutes) oeA1Note: final answer 79.3 follows from using the midpoints 30, 60, 90, 120 to find $\frac{47580}{.809}$.8.(b) (Best estimate) 77.2(minutes) oeB1FT 'their 80.2' - 3OR for a clear explanation that we cannot tell e.g.FT 'their 80.2' - 3OR for a clear explanation that we cannot tell e.g.FT 'their 80.2' - 3OR for a clear explanation that		1	1
coefficients and subtractionother is linear in the same pair of unknownsAllow one error in one term, but not in the equated coefficientsFinds one unknownA1Finds one unknown or finds 16.3(0) + 19.1(0) - 6 × 2.7(0)A1FT disthe other unknown or finds (£)19.2(0)A1FT 3 (Their derived a') + (Their derived a') or 35.4 - 6 × Their derived a') + (Their derived a') or 35.4 - 6 × Their derived a' provided at least one mark previously awarded. Unsupported 19.2(0) is awarded no marks7(a) $7x^2 + 5x - 42x - 30$ B27(b) $(y^2 - 2)(y + 4)$ B2B1 (0) consider and like terms to collect7(b) $(y^2 - 2)(y + 4)$ B2B1 (2040 + 11160 + 21420 + 13500 = 48120)4 (6)M180.2(minutes) oeA18(a) (Midpoints 30, 60, 90, 1258(b) (Best estimate) 77.2(minutes) oeA1Note: final answer 79.3 follows from using the midpoints 30, 60, 90, 120 to find $\frac{47580}{600}$ 8(a) (b) (Cest estimate) 77.2(minutes) oeB1FT (1) T their 80.2' - 3 Do not award the mark if the explanation is contradicted by the mean will be higher'.	6.* $a + 4c = 16.30$ and $2a + 3c = 19.10$	B1	May use other letters or words throughout
or rearranges one equation and substitutes into the otherequated coefficientsFinds one unknownA1CAO $a = 5.5(0)$ or $c = 2.7(0)$ Finds the other unknown or finds $16.3(0) + 19.1(0) - 6 \times 2.7(0)$ A1FT their a' or 'their c' used in one of their equations(E)19.2(0)B1FT 3('their derived a') + ('their derived c') or $35.4 - 6 \times$ 'their derived a') + ('their derived c') or $35.4 - 6 \times$ 'their derived d') = provided at least one mark previously swarded. Unsupported 19.2(0) is awarded no marks7.(a) $7x^2 + 5x - 42x - 30$ B2B1 for any three terms correct; $nx^2 - 37x + ni$ implies two terms correct if not from wrong working7.(a) $7x^2 - 37x - 30$ B1Implies previous B2. FT for equivalent level of difficulty, providing 4 terms to consider and like terms to collect7.(b) $(y-2)(y+4)$ B2B1 for $(y \dots 2)(y \dots 4)$ 8.(a) Midpoints 30, 60, 90, 125B130 $\times 68 + 60 \times 186 + 90 \times 238 + 125 \times 108$ $(2040 + 11160 + 21420 + 13500 = 48120)$ M1 $\div 600$ m18.2(minutes) oeA1A1Note: final answer 79.3 follows from using the midpoints 30, 60, 90, 120 to find $\frac{47580}{.600}$.8.(b) (Best estimate) 77.2(minutes) oeB1FT 'their 80.2' -3 OR for a clear explanation that we cannot tell e_0 .We do not know how many values will change group' or 'Slighty less as a few will move to the group below'.B1FT 'their 80.2' -3 Do not award the mark if the explanation is contradicted by 'the mean will be higher'.		M1	
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8.(a) Midpoints 30, 60, 90, 125 B1 30 × 68 + 60 × 186 + 90 × 238 + 125 × 108 M1 FT 'their midpoints' provided at least 3 of 'their 4 midpoints' lie within the appropriate group, including lower and upper bounds for the last 3 marks 2040 + 11160 + 21420 + 13500 = 48120) m1 ± 600 m1 80.2(minutes) oe M1 K M1 Note: final answer 79.3 follows from using the midpoints 30, 60, 90, 120 to find $\frac{47580}{600}$. 8.(b) Rest estimate) 77.2(minutes) oe OR for a clear explanation that we cannot tell e.g. B1 'We do not know how many values will change group' or 'Slightly less as a few will move to the group below'. B1		B2	B1 for (y 2)(y4)
Midpoints 30, 60, 90, 125B1 $30 \times 68 + 60 \times 186 + 90 \times 238 + 125 \times 108$ (2040 + 11160 + 21420 + 13500 = 48120)M1FT 'their midpoints' provided at least 3 of 'their 4 midpoints' lie within the appropriate group, including lower and upper bounds for the last 3 marks $\div 600$ m1 $80.2(minutes)$ oeA1Note: final answer 79.3 follows from using the midpoints 30, 60, 90, 120 to find $\frac{47580}{600}$. $8.(b)$ (Best estimate) 77.2(minutes) oeB1FT 'their $80.2' - 3$ OR for a clear explanation that we cannot tell e.g.FT 'their $80.2' - 3$ OR for a clear explanation that we cannot tell e.g.Do not award the mark if the explanation is contradicted by 'the mean will be higher'.		(5)	
$(2040 + 11160 + 21420 + 13500 = 48120)$ midpoints' lie within the appropriate group, including lower and upper bounds for the last 3 marks $\div 600$ m1 $80.2(minutes)$ oeA1 $80.2(minutes)$ oeA1Note: final answer 79.3 follows from using the midpoints 30, 60, 90, 120 to find $\frac{47580}{600}$. $8.(b)$ (Best estimate) 77.2(minutes) oeB1OR for a clear explanation that we cannot tell e.g.FT 'their $80.2' - 3$ OR for a clear explanation that we cannot tell e.g.Do not award the mark if the explanation is contradicted by 'the mean will be higher'.		B1	
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 8.(b) (Best estimate) 77.2(minutes) oe OR for a clear explanation that we cannot tell e.g. 'We do not know how many values will change group' or 'Slightly less as a few will move to the group below'. B1 FT 'their 80.2' – 3 Do not award the mark if the explanation is contradicted by 'the mean will be higher'. 		<u> </u>	
tell e.g. 'We do not know how many values will change group' or 'Slightly less as a few will move to the group below'.		B1	
(5)	tell e.g. 'We do not know how many values will change group' or 'Slightly less as a few will		
		(5)	

9.(a)		
-4	B1	
9.(b) All 7 correct points plotted correctly and joined with a smooth curve	B2	Tolerance \pm a small square; FT 'their points' and 'their curve' for 2 marks provided the curve is reasonably parabolic
		B1 for a smooth curve at least through 4 pairs of coordinates or for all of 'their 7 pairs of coordinates' plotted correctly
9.(c) –1, 3	B1	Must be exact as values given in the table. Do not award for (-1, 0) and (3, 0)
9.(d) The line $y = 1$ drawn	B1	Allow for appropriate marks on the curve at $y = 1$ for at least one intersection
		FT 'their curve' provided there are at least 2 intersections; if their curve has more than 2 intersections with $y = 1$, they must give all their solutions for B2.
x = -1.2 to $-1.3x = 3.2$ to 3.3	B1 B1	Allow these marks for calculated solutions e.g. $x = -1.2360$ and $x = 3.2360$
		Award B1 only if both solutions are given as coordinates e.g.(-1,2, 1) and (3.2, 1)
	(7)	
10.(a)(i) 82	B1	
10.(a)(ii) 8√2	B1	
10.(b) n ² + n oe	B2	Accept unsimplified e.g. $n \times n + n$
		B1 for $n^2 + kn + c$ where k and c are not both 0
10.(c) 2n + 2 and 2n + 4	B1	oe
(2n + 2n + 2 + 2n + 4 =) 6n + 6	B1	FT $2n$ + 'their $2n$ + 2' + 'their $2n$ + 4'
Convincing statement of divisibility by 6 e.g. = $6(n + 1)$ or 'both terms divide by 6'	E1	oe
f	(7)	[

11. Sight of $(1 - 0.38 =) 0.62$ and $(1 - 0.38)(1 - 0.16) =) 0.5208$ oeB1(6510 ÷ 0.84) oeM1 ÷ 0.62 oeFT 'their 1 - 0.16' or 'th implied by sight of 775 Division may be done(£)12 500A1CAO If no marks award SC1 (£)14 152(.17) from a r12.(4)Correct evaluation with $3 \le x \le 4$ 12.Correct evaluation with $3 \le x \le 4$ B1Two correct evaluations with $3.25 \le x \le 3.45$ and one > 40, one < 40 soiB13.3A1 $\frac{x + x^3 + x^2 + 4}{x^3 + x^2}$) or 1050 n either o).5208; 0.16)' for an ar eduction o ugh to im then may all';	o0 order of 54% ply > 40 or < 40; y be implied by
OR $((1-0.38)(1-0.16)=) 0.5208$ oeM1FT 'their 1-0.16' or 'their miniple dy sight of 775 Division may be done in the implied by sight of 755 Division may be done in the implied by sight of 775 Division may be done in the implied by sight of 775 Division may be done in the implied by sight of 775 Division may be done in the implied by sight of 775 Division may be done in the implied by sight of 700 may be done in the implied by sight of 700 may be done in the implied by sight of 700 may be done in the implied by sight of 700 ma) or 1050 n either o).5208; 0.16)' for an ar eduction o ugh to im then may all';	o0 order of 54% ply > 40 or < 40; y be implied by
$\begin{array}{c c} \div 0.62 \text{ oe} \\ \div 0.62 \text{ oe} \\ (\pounds) 12500 \\ (\pounds) 12500 \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 13. \\ 13. \\ 3.3 \\ 3.3 \\ 13. \\ 10. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 13. \\ 12. \\ 13. \\ 12. \\ 13. \\ 12. \\ 13. \\ 12. \\ 13. \\ 12. \\ 13. \\ 12. \\ 13. \\ 12. \\ 13. \\ 13. \\ 13. \\ 13. \\ 13. \\ 10. \\ 1$) or 1050 n either o).5208; 0.16)' for an ar eduction o ugh to im then may all';	o0 order of 54% ply > 40 or < 40; y be implied by
$\div 0.62$ oeM1Division may be done in M2 for sight of $6510 \div$ FT 'their $(1 - 0.38)$	n either o 0.5208; 0.16)' for an ar eduction o ugh to im then may all';	nswer of of 54% ply > 40 or < 40; y be implied by
(£)12500A1FT 'their $(1 - 0.38)$	0.16)' for an ar eduction o ugh to im then may all';	of 54% ply > 40 or < 40; / be implied by
If no marks award SC1 (£)14 152(.17) from a r12.(4)12.Correct evaluation end If evaluations not seen e,g, 'too big' or 'too sm Solving $x^3 + x - 40 =$ equivalentlyOne correct evaluation with $3 \le x \le 4$ B1Two correct evaluations with $3.25 \le x \le 3.45$ and one > 40, one < 40 soi	ugh to im then may all';	of 54% ply > 40 or < 40; / be implied by
(4)(f) $14152(.17)$ from a r12.(4)12.Correct evaluation end If evaluations not seen e,g, 'too big' or 'too sm Solving $x^3 + x - 40 =$ equivalentlyOne correct evaluation with $3 \le x \le 4$ B1Two correct evaluations with $3.25 \le x \le 3.45$ and one > 40, one < 40 soi	ugh to im then may all';	of 54% ply > 40 or < 40; / be implied by
12.Correct evaluation end If evaluations not seen e,g, 'too big' or 'too sm Solving $x^3 + x - 40 =$ equivalentlyOne correct evaluation with $3 \le x \le 4$ B1Two correct evaluations with $3.25 \le x \le 3.45$ and one > 40, one < 40 soi	then may all';	be implied by
One correct evaluation with $3 \le x \le 4$ B1If evaluations not seem e,g, 'too big' or 'too sm Solving $x^3 + x - 40 =$ equivalentlyTwo correct evaluations with $3.25 \le x \le 3.45$ and one > 40, one < 40 soi	then may all';	be implied by
One correct evaluation with $3 \le x \le 4$ B1Two correct evaluations with $3.25 \le x \le 3.45$ B1and one > 40, one < 40 soi		
Two correct evaluations with $3.25 \le x \le 3.45$ and one > 40, one < 40 soiB1Two correct evaluations with $3.25 \le x \le 3.35$ and one > 40, one < 40 soi		
and one > 40, one < 40 soiM1Providing at least B1 a clear statement of the and one > 40, one < 40 soi3.3A1 $\frac{x}{x}$ x^3 +		
and one > 40, one < 40 soiclear statement of the and 3.4.3.3A1 x		
	r or	$x^3 + x - 40$
		$\frac{x + x - 40}{-10}$
3.1 32.89		-7.109
3.2 35.96		-4.032
3.25 37.57		-2.421
3.3 39.23		-0.763
3.35 40.94		0.945
3.4 42.704		2.704
3.45 44.51		4.513
3.5 46.37		6.375
3.6 50.250		10.256
3.7 54.35		14.353
3.8 58.672		18.672
3.9 63.21		23.219
4 68		28
(4)		

13.(a)		
Correct tree diagram e.g.	В3	B1 for left hand branches correct
		FT 'their $\frac{5}{12}$ or $\frac{7}{12}$ '
$\frac{4}{11}$ W		12 12 B1 FT for top right branches correct
		B1 FT for bottom right branches correct
$\frac{5}{12}$ W $\frac{7}{11}$ B		Allow equivalent fractions in all cases.
		If rounded decimals used here
$\frac{7}{12} \qquad \mathbf{B} \qquad \frac{5}{11} \qquad \mathbf{W}$		e.g. 0.42, 0.58, 0.36, 0.64, 0.45 and 0.55 award B1 here and FT in (b) and (c) for M marks only.
6 11 B		
13.(b)		Check tree diagram
$1 - \frac{7}{12} \times \frac{6}{11}$ or $\frac{5}{12} \times \frac{4}{11} + \frac{5}{12} \times \frac{7}{11} + \frac{7}{12} \times \frac{5}{11}$ oe	M1	FT 'their probabilities' providing at least B1 awarded in (a)
$\frac{90}{132}$ or $\frac{15}{22}$ oe	A1	FT 'their tree diagram'
132 22		If no marks award SC1 for the correct sum of two of the required products e.g for:
		$\frac{5}{12} \times \frac{7}{11} + \frac{7}{12} \times \frac{5}{11} = \frac{70}{108} \text{ Oe}$
13.(c)		Check tree diagram
$\frac{5}{12} \times \frac{7}{11} \times \frac{6}{10} + \frac{7}{12} \times \frac{6}{11} \times \frac{5}{10} \text{ oe}$	M2	M1 for either product
$\frac{420}{1320}$ or $\frac{7}{22}$ oe	A1	CAO
1320 22	(8)	
14.(a)	(0)	
28 000	B1	
14.(b)		Allow values to be consistently rounded or
		truncated
(end of 2024). 1.12 ³ ×28 000 (= 39 337.984)	M1	FT '1.12 ³ ×(their 28000)'; may be seen in stages (end of 2021) 1.12 × 28000 (= 31360) (end of 2022) 1.12 × 31360 (= 35123.2) (end of 2023) 1.12 × 35123(.2) (= 39337.984)
(end of 2025)		
1.12 × 39 337(.984) = 44 058(.54) or 44059 or 44 057(.44)	M1	FT 'their 39337' Interpretation of the formula as e.g. $25000(1.12)^5 - 25000(1.12)^4$ implies M1 M1
(44 058.54 – 39 337.984 =) 4720 or 4721	A1	
14.(c)		FT 'their 44058() if a step-by-step method used
Finds (end of 2026 =) 49 345(.56) or (end of 2027 =) 55 267(.03)	S1	Accept 49 343 to 49 346 Accept 55 264 to 55 268
		Allow for appropriate use of 25000 × 1.12 ⁿ where
Yes indicated and sufficient work to show	B1	n is a decimal between 6 and 7 FT 'their 44058() and the correct FT conclusion
the population is both below and above		
50 000 during 2017		If no marke oward SC1 for the correct conclusion
		If no marks award SC1 for the correct conclusion following incorrect work in (b)
	(6)	

15.(a)		Mark using one method only, to the
(Height of pyramid removed =) 4 (cm)	B1	candidate's advantage
$\frac{1}{3} \times 24 \times 12^2 - \frac{1}{3} \times 4 \times 2^2 \ (= 1152 - 5.33)$	M2	FT 'their 4' provided < 24
		M1 for $\frac{1}{3} \times 24 \times 12^2$ or $\frac{1}{3} \times 4 \times 2^2$
$\frac{3440}{3}$ or 1146.6(66) or 1146.7	A1	FT 'their 4' Allow 1147 from correct working
(Mass =) $0.9 \times \frac{3440}{3}$	M1	FT 'their $\frac{3440}{3}$,
3 1032 (grams)	A1	CAO
Valid assumption e.g.	E1	Award for 1031.9(4) to 1032.3
'No wax is lost when the wax is cut.' or 'The mass of the wick is negligible.' or 'The wick		
can be ignored.' or 'The volume of the wick		
is negligible.' or 'The wick has the same density as the wax.'		
Alternative Method 1 for first 6 marks		
(difference of masses): (Height of pyramid removed =) 4 cm	B1	
1 1 1 2 2	M1	(1152 or 5.33)
$\frac{1}{3} \times 24 \times 12^2$ or $\frac{1}{3} \times 4 \times 2^2$		'FT their 4'
$0.9 \times \frac{1}{3} \times 24 \times 12^2$ and $0.9 \times \frac{1}{3} \times 4 \times 2^2$	М2	FT 'their 4' for M2 or M1
		M1 for $0.9 \times \frac{1}{3} \times 24 \times 12^2$ or $0.9 \times \frac{1}{3} \times 4 \times 2^2$;
		(1036.8 or 1037) (4.77 or 4.8)
$\left(0.9 \times \frac{1}{3} \times 24 \times 12^2\right) - \left(0.9 \times \frac{1}{3} \times 4 \times 2^2\right)$	M1	
1032 (grams)	A1	CAO
Alternative Method 2 for first 6 marks		Award for 1031.9(4) to 1032.3
(scaling the volume):		
$\frac{1}{3} \times 24 \times 12^2$	M1	(=1152)
$0.9 \times \frac{1}{3} \times 24 \times 12^2$ or $\frac{1}{6^3} \left(\frac{1}{3} \times 24 \times 12^2 \right)$	M1	(1036.8 or 1037) or (4.77 or 4.8)
$0.9\left(\frac{1}{3} \times 24 \times 12^2 - \frac{1}{6^3}\left(\frac{1}{3} \times 24 \times 12^2\right)\right)$ oe	МЗ	or M2 for sight of
$(3 6^{\circ} (3))$		$\frac{1}{3} \times 24 \times 12^2 - \frac{1}{6^3} \left(\frac{1}{3} \times 24 \times 12^2 \right) 000$
		or M1 for sight of $\frac{1}{6^3} \left(0.9 \times \frac{1}{3} \times 24 \times 12^2 \right) 00$
1032 (grams)	A1	CAO
l	L	Award for 1031.9(4) to 1032.3

15.(b) Valid impact following their assumption e.g. 'The volume of the wax may be a little less so the mass will be less.' or 'The density of the wick is likely to be less than the density of the wax, so in fact the mass of the candle is likely to be a bit less.'	E1	Must have stated an assumption in part (a).
	(8)	
16. smallest miles greatest litres	S1	Allow $187 \le d < 187.5$ and $4.8 < l \le 5.2$
187.25 ÷ 5 (= 37.45)	M2	M1 for one value correct in a division
Correct unit conversion	B1	At some stage; e.g. 299.6 ÷ 5 implies S1 M2 B1
59.92 (km/l)	A1	CAO; allow an answer of 60 from correct working only.
		If many attempts are offered without a method or answer being identified, then mark final attempt
	(5)	
17.(a) 40320	B2	B1 for sight of 8! or equivalent product
17.(b) 10 080	B2	B1 for sight of $4 \times 7 \times 6 \times 5 \times 4 \times 3$ or equivalent
	(4)	
18.(a) 0 (cm per year)	B1	
18.(b) Gradient of the chord joining (10, 145) to (15, 168)		
$\frac{168-145}{15-10}$	M2	M1 for the gradient of a chord with one point correct
4.6 (cm per year)	A1	CAO
	(4)	

19.		
7(x+2) + 4(3x+1) = (3x+1)(x+2)	M2	soi
		M1 for $\frac{7(x+2)+4(3x+1)}{(3x+1)(x+2)}$ (=1) soi
Expands the brackets and collects all terms on one side:	M2	FT for possible M2 or M1 here, only if of equivalent difficulty;
7x + 14 + 12x + 4 = 3x2 + 6x + x + 2 3x2 - 12x - 16 = 0		For M2 and M1 allow one error in expansion or collection;
5x -12x -10 - 0		M1 for expansion not equated to zero e.g. $7x + 14 + 12x + 4 = 3x^2 + 6x + x + 2$ leading to 'their $19x + 18$ ' = 'their $3x^2 + 7x + 2$ '
Applies the quadratic formula: $\frac{-(-12) \pm \sqrt{(-12)^2 - 4(3)(-16)}}{2 \times 3}$ or better	M1	FT 'their derived 3-term quadratic' (even if it does not result in real roots); allow one slip in substitution; formula must not be clearly incorrect; allow attempt to complete the square with at most one slip
Simplifies:	A1	FT 'their derived 3-term quadratic'; may be implied by correct decimal values
$\frac{12 \pm \sqrt{336}}{6}$ or $\frac{6 \pm 2\sqrt{21}}{3}$ or equivalent		-1.05505, 5.05505
-1.06, 5.06	A1	CAO
	(7)	

Correct justification e.g.		
$360 - 150 - 161 (= 49^{\circ})$ or	B1	or equivalent; check diagram; NB method must be seen as answer is given
180 – 161 + 30 (= 49°)		Allow 30 + 19 (= 49)
20.(b)		
$\frac{1}{2}$ × 50 × 72 × sin49	M1	
1358(.4772km ²)	A1	
20.(c) $PR^2 = 2960(.37)$	M2	M1 for $PR^2 = 50^2 + 72^2 - 2$ (50)(72)cos49
<i>PR</i> = 54.4(km)	A1	soi; accept 54 km
$\cos PRQ = \frac{54.4^2 + 72^2 - 50^2}{2 \times 54.4 \dots \times 72} \text{or}$	M2	FT 'their 54.4' for M2 or M1
$\sin PRQ = 50 \times \frac{\sin 49}{54.4}$ or		M1 for $50^2 = 54.4^2 + 72^2 - 2(54.4)(72)\cos PRQ$
$\cos QPR = \frac{54.4^2 + 50^2 - 72^2}{2 \times 54.4 \times 72}$ or		or for $\frac{\sin PRQ}{50} = \frac{\sin 49}{54.4}$ soi; may be inverted
$\sin QPR = 72 \times \frac{\sin 49}{54.4} \text{ or }$		or for $72^2 = 54.4^2 + 50^2 - 2(54.4)(72)\cos QPR$
54.4		or for $\frac{\sin QPR}{72} = \frac{\sin 49}{54.4}$ soi; may be inverted
<i>PRQ</i> = 44° or <i>QPR</i> = 87°	A1	CAO; Accept 43.9() or 87.0()
Bearing is (360 – 44 – 19 =) 297° or (180 + 30 + 87 =) 297°	A1	FT 'their derived 44' or 'their derived 87'
Alternative method using area		
$PR^2 = 2960(.37)$	М2	M1 for $PR^2 = 50^2 + 72^2 - 2$ (50)(72)cos49
PR = 54.4(km)	A1	soi; accept 54 km
$sinQRP = \frac{1358 \times 2}{54.4 \times 72} \text{ or}$	М2	FT 'their 1358' and 'their 54.4' for M2 or M1
<i>J4.4×12</i>		M1 for $\frac{1}{2} \times 54.4 \times 72 \times sinQRP = 1358$ or for
$sinQPR = \frac{1358 \times 2}{54.4 \times 50}$		$\frac{1}{2} \times 54.4 \times 50 \times sinQPR = 1358$
PRQ = 44° or QPR = 87°	A1	2 CAO; Accept 43.9() or 87.0()
Bearing is (360 – 44 – 19 =) 297° or (180 + 30 + 87 =) 297°	A1	FT 'their derived 44' or 'their derived 87'
	(10)	

21.(a) Correctly completed Venn diagram e.g. (a) (A) (0.12) (0.18) (0.42) (0.28) or $0.12 + 0.42$ or $0.3 + 0.6 - 2(0.18)$ or equivalent	B2	B1 for sight of a correct method to find the intersection e.g. $0.3 + 0.6 - 0.72$ or $0.3 - x + x + 0.6 - x = 0.72$ or sight of 0.18
0.54	B1	FT 'their 0.12 + 0.42' or 0.3 + 0.6 – 2('their 0.18'); correct answer implies B2 B1
21.(b) $1 - P(A \cup B)$ or equivalent or correct region on Venn diagram indicated	S1	
0.28	B1 (5)	implies S1 FT 'their Venn diagram'