Please check the examination details below before entering your candidate information


You must have: Ruler graduated in centimetres and millimetres,
Total Marks protractor, pair of compasses, pen, HB pencil, eraser, calculator, Formulae Sheet (enclosed). Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided - there may be more space than you need.
- You must show all your working.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- Calculators may be used.

- If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142 unless the question instructs otherwise.


## Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- Good luck with your examination.



## MME.

 GCSE Revision - GCSE Maths

GCSE Maths Predicted Papers 2024


GCSE Maths
Revision Cards


GCSE Maths
Revision Guide


Course in a Box - GCSE Maths (Guaranteed Pass)

Answer ALL questions.
Write your answers in the spaces provided.
You must write down all the stages in your working.
1 (a) Simplify $\left(x^{3}\right)^{5}$

$$
=x^{3 \times 5}=x^{15}
$$

2


Describe fully the single transformation that maps shape $\mathbf{S}$ onto shape $\mathbf{T}$.
Translation by vector $(6)$

3 The length of a football pitch is 90 metres, correct to the nearest metre.
Complete the error interval for the length of the football pitch.

$$
89.5 \mathrm{~m} \leqslant \text { length }<90.5
$$

(Total for Question 3 is $\mathbf{2}$ marks)

2


Describe fully the single transformation that maps shape $\mathbf{S}$ onto shape $\mathbf{T}$.
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$$
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$$ m

(Total for Question 3 is 2 marks)
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4 Festival A will be in a rectangular field with an area of $80000 \mathrm{~m}^{2}$
The greatest number of people allowed to attend Festival A is 425
Festival B will be in a rectangular field 700 m by 2000 m .
The greatest number of people allowed to attend Festival B is 6750
The area per person allowed for Festival $B$ is greater than the area per person allowed for Festival A.
(a) How much greater?

Give your answer correct to the nearest whole number.
Are of festival $B=700 \times 2000=1,400,000 \mathrm{~m}^{2}$.
$\rightarrow$ Area per person: $1,400,000 \div 6750=207.40 \ldots$
Area per person at $A: 80000 \div 425=188.23 \ldots$
$207 \cdot 4=188 \cdot 2=19$ to the nearest whole number.

5 The points $L, M$ and $N$ are such that $L M N$ is a straight line.
The coordinates of $L$ are $(-3,1)$
The coordinates of $M$ are $(4,9)$
Given that $L M: M N=2: 3$,
find the coordinates of $N$.
LM: $x$ distance: $4-(-3)=7$,

$$
x \text { distance: } 4-0.51=8 \text {. }
$$

MN: $x$ distance: $7 \times \frac{3}{2}=10.5$

$$
y \text { distance: } 8 \times \frac{3}{2}=12
$$

$$
N=(4+10 \cdot 5,9+12)
$$

$$
N=(14.5,21)
$$

(i4.5, 21)
(Total for Question 5 is $\mathbf{4}$ marks)

6 A new phone cost $£ 679$
The value of the phone decreases at a rate of $4 \%$ per year.
Work out the value of the phone at the end of 3 years.

$$
\begin{aligned}
& =£ 679 \times(1-0.04)^{3} \\
& =£ 600.74 \text { (nearest penny). }
\end{aligned}
$$

$$
600.74
$$

7 In Spain, Sam pays 27 euros for 18 litres of petrol.
In Wales, Leo pays $£ 40.80$ for 8 gallons of the same type of petrol.

$$
\begin{aligned}
1 \text { euro } & =£ 0.85 \\
4.5 \text { litres } & =1 \text { gallon }
\end{aligned}
$$

Sam thinks that petrol is cheaper in Spain than in Wales.
Is Sam correct?
You must show how you get your answer.

$$
\begin{aligned}
& 8 \text { gallons }=8 \times 4.5=36 \text { Litres. } \\
& \mathcal{f} 40.80=€ 40.8 \div 0.85=€ 48 . \\
& \text { In Spain: } 27 \div 18=€ 1.50 / \text { Litre. } \\
& \text { In Wales: } 48 \div 36=€ 1.33 / \text { Litre. }
\end{aligned}
$$

No, sames wrong. Petrol is cheaper in Wales.

8 Use your calculator to work out

$$
\frac{\sqrt[3]{1.57^{4}+\tan 60^{\circ}}}{7.2^{\frac{1}{2}}}
$$

Give your answer correct to 3 significant figures.

$$
\begin{aligned}
& =0.7393379403 \ldots \\
& =0.739(3 s . f)
\end{aligned}
$$

(Total for Question 8 is $\mathbf{2}$ marks)

9 A box in the shape of a cuboid is placed on a horizontal floor.
The box exerts a force of 180 newtons on the floor.

$$
\text { pressure }=\frac{\text { force }}{\text { area }}
$$

The box exerts a pressure of 187.5 newtons $/ \mathrm{m}^{2}$ on the floor.
The face in contact with the floor is a rectangle of length 1.2 metres and width $x$ metres.
Work out the value of $x$.

$$
\begin{aligned}
& 187.5=\frac{180}{A} \\
& \Rightarrow A=\frac{180}{187.5}=0.96 \mathrm{~m}^{2} . \\
& A=1.2 x=0.96 \\
& x=0.96 \div 1.2 \\
& x=0.8 \mathrm{~m}
\end{aligned}
$$

$$
x=0.8 \mathrm{~m}
$$

(Total for Question 9 is $\mathbf{3}$ marks)

10 The box plot shows information about the sales, in thousands of pounds ( $£ 000 \mathrm{~s}$ ), of an online store each month.


Andrew says,
"Three quarters of the given data lies between 160000 and 350000 because these are the values of the lower quartile and the upper quartile."

Andrew is wrong.
(a) Explain why.

Half the data lies between the upper and lower quartiles, not three quarters. This is the IQR.

The table shows information about the sales, in $£ 000$ s, in a shop each month.

|  | Sales (f000s) |
| :--- | :---: |
| least value | 30 |
| lower quartile | 80 |
| median | 170 |
| upper quartile | 260 |
| greatest value | 350 |

(b) On the grid below, draw a box plot for this information.

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(c) Compare the distribution of the sales of the online store with the distribution of the sales in the shop.

The online store has a greater median than the shop, but the IQR for the online store is greater than that of the shop.
(Total for Question 10 is 5 marks)

11 Kieron has 13 workers he can use for a job.
He knows that 6 workers would take $14 \frac{1}{2}$ days to complete this job.
Show that Kieron has enough workers to finish this job in less than 7 days.
If 6 worker take 14.5 days, it would take one worker $6 \times 14.5$ days $=87$ days.
If he has $x$ workers and it takes 7 days then $7 x=87 \Rightarrow x=87 / 7=12.42 \ldots$ There for 13 workers can do it in 7 days.

12 The equation of the line $\mathbf{L}_{1}$ is $y=2 x+3$
The equation of the line $\mathbf{L}_{2}$ is $5 y-10 x+4=0$
Show that these two lines are parallel.

$$
\text { Grad tent of } L_{1}=2 \text { (as it's in form } y=m x+c \text { ) }
$$

$$
\begin{aligned}
& L_{2}: 5 y-10 x+4=0 \\
& \Rightarrow 5 y=10 x-4 \Rightarrow y=2 x-4 / 5 .
\end{aligned}
$$

Gradient of $L_{2}=2$.
The have the save gradient and are therefore parallel.

13


Enlarge the shaded shape by scale factor -2 with centre of enlargement $(0,0)$
(Total for Question 13 is 2 marks)
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14 Saffron wants to work out an estimate for the total number of fish in a lake.
On Friday, Saffron catches 180 fish from the lake.
She puts a tag on each of these fish and puts them back into the lake.
On Saturday, Saffron catches 305 fish from the same lake.
She finds that 45 of the 305 fish are tagged.
Work out an estimate for the total number of fish in the lake.
Proport on of fish initally captured to the total population, $n$, is the same as fish tagged to numbercaptured the second time.

$$
\frac{180}{n}=\frac{45}{305}=>n=\frac{305 \times 180}{45}
$$

$$
1220
$$

(Total for Question 14 is 3 marks)

15 The ratio of Marta's hourly pay to Khalid's hourly pay is $6: 5$
Both Marta and Khalid get an increase of $£ 1.50$ in their hourly pay.
The ratio of Marta's hourly pay to Khalid's hourly pay after this increase is $13: 11$
Work out the hourly pay before the increase for Marta and for Khalid.
Inital pay: Marta $=6 x$, Khalid: $5 x$.
After raise: $\frac{6 x+1.5}{5 x+1.5}=\frac{13}{11}$

$$
\begin{aligned}
& \Rightarrow 11(6 x+1.5)=13(5 x+1.5) \\
& \Rightarrow 66 x+16 \cdot 5=65 x+19.5 \\
& \Rightarrow x=19.5-16 \cdot 5=3 . \\
& \text { Inital pay Marta }=6 \times 3=f 18 \\
& \text { Khalid }=5 \times 3=f=f 15
\end{aligned}
$$

Marta $£ 18$
Khalid $£ 15$
(Total for Question 15 is $\mathbf{4}$ marks)

16 A shop manager wants to advertise special offers on social media platforms.
The manager asks 100 customers which of type $A$, type $B$ or type $C$ they use.
Of these customers,
4 use all three types
16 do not use any of type $A$, type $B$ or type $C$
8 use both type $A$ and type $B$, but not type $C$
14 use both type $B$ and type $C$
62 in total use type $A$
all 20 who use type $C$ also use at least one of type $A$ and type $B$.
(a) Complete the Venn diagram for this information.


One of the customers is chosen at random.
Given that this customer uses type $A$,
(b) find the probability that this customer also uses type $B$.

$$
\frac{8+4}{62}=\frac{12}{62}
$$

17 A solid cone is joined to a solid hemisphere to make the solid $\mathbf{T}$ shown below.


The diameter of the base of the cone is 7 cm .
The diameter of the hemisphere is 7 cm .
The total volume of $\mathbf{T}$ is $120 \pi \mathrm{~cm}^{3}$
The total height of $\mathbf{T}$ is $y \mathrm{~cm}$.
(a) Calculate the value of $y$.

Give your answer correct to 3 significant figures.
Hem sphere volume $=\frac{1}{2} \times \frac{4}{3} \times \pi \times 3 \cdot 5^{3}$
Cone volume $=\frac{1}{3} \times \pi \times 3 \cdot 5^{2} \times h($ where $y=h+3 \cdot 5)$.

$$
\begin{aligned}
& \frac{1}{3} \times \pi \times 3 \cdot 5^{2} \times h+\frac{2}{3} \pi \times 3 \cdot 5^{3}=120 \pi \\
& \Rightarrow \quad 3.5^{2} h+2 \times 3.5^{3}=360 \\
& \Rightarrow \quad h=\frac{360-2 \times 3.5^{3}}{3.5^{2}}=\frac{1097}{4} \\
& y=\frac{1097}{4}+3.5=25.9(3 s f) \quad y=25.9
\end{aligned}
$$

The diameter of the base of the cone and the diameter of the hemisphere are both increased by the same amount.
Assuming the total volume of $\mathbf{T}$ does not change,
(b) explain the effect this would have on your answer to part (a).

The height would have to decrease for the volume to stay the same.


Calculate the length of $Q S$.
Give your answer correct to 3 significant figures.
You must show all your working.
Cosine Rule: $Q R^{2}=11^{2}+9.4^{2}-2 \times 11 \times 94 \cos (27)$

$$
Q R=\sqrt{11^{2}+9.4^{2}-2 \times 11 \times 9.4 \cos (27)}
$$

$$
=5.009975 \ldots
$$

Sine Rule: $\frac{Q R}{\sin 41}=\frac{Q S}{\sin 88}$

$$
Q S=\frac{5.0099 \ldots \sin 88}{\sin 41}
$$

$$
Q s=7.63(3 \mathrm{sf}) .
$$

19 The functions g and h are such that

$$
\mathrm{g}(x)=\sqrt[3]{2 x-5} \quad \mathrm{~h}(x)=\frac{1}{x}
$$

(a) Find $g(16)$

$$
g(16)=\sqrt[3]{2 \times 16-5}=\sqrt[3]{27}=3
$$

$$
g(16)=3
$$

(b) Find $\mathrm{hg}^{-1}(x)$

Give your answer in terms of $x$ in its simplest form.

$$
\begin{aligned}
& \text { Let } y=\sqrt[3]{2 x-5} \\
& y^{3}=2 x-5, \quad x=\frac{y^{3}+5}{2} \\
& \Rightarrow g^{-1}(x)=\frac{x^{3}+5}{2} \\
& h\left(g^{-1}(x)\right)=\frac{1}{g^{-1}(x)}=\left(\frac{x^{3}+5}{2}\right)^{-1}=\frac{2}{x^{3}+5} .
\end{aligned}
$$

$$
\mathrm{hg}^{-1}(x)=\frac{2}{x^{3}+5}
$$

$20 A, B, C$ and $D$ are points on the circumference of a circle, centre $O$. $A D E$ and $B C E$ are straight lines.


Work out the size of angle $C D E$.
Give a reason for each stage of your working.
$\angle B A D=132 \div 2=66^{\circ}$ as angles at the centre are twice the angle at the circumference. $\angle B C D=180-66=114^{\circ}$ as opposite angles in ce cyclic quadrilateral add upto $180^{\circ}$. $\angle D C E=66^{\circ}$ as angles on a shaight line add to $180^{\circ}$. $\angle C D E=180-66-16=98^{\circ}$ cos angles in a triangle add to $180^{\circ}$.

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21 The peaph of 1 - $1(1)$ in aloown on the pitel below

(a) On the perid nbove, Nkets the graph of 1'-1( 1 )

Itere is a sketul of the graph of $\mathrm{l}^{\prime}$ - limn"


 Point R has coordinutor (90, S)
(b) I'ind inn expreantan lin $8(1)$ In lomen ol'

$$
\begin{aligned}
& \text { Translation (gar), } 360-10,210 \\
& \tan (0,710)+5 \\
& \tan \left(x, 210^{\circ}\right), 5
\end{aligned}
$$

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22 Find algebraically the set of values of $x$ for which

$$
\begin{gathered}
x^{2}-49>0 \Rightarrow(x+7)(x-7)>0, \\
\quad x<-7 \text { and } x>7 . \\
5 x^{2}-31 x-72>0 \\
\Rightarrow(5 x+9)(x-8)>0 \\
x<-9 / 5 \text { or } x>8 .
\end{gathered}
$$

For both satisfied

$$
x<-7 \text { or } x>8 \text {. }
$$

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