| Please check the examination details belo  | ow before ente  | ring your candidate information |  |  |
|--|-----------------|---------------------------------|--|--|
| Candidate surname  | Other names     |                                 |  |  |
| Centre Number Candidate | al GCSE         |                                 |  |  |
| <b>Time</b> 2 hours 30 minutes   | Paper reference | 4MB1/02                         |  |  |
| Mathematics B PAPER 2  |                 |                                 |  |  |
| <b>You must have:</b> Ruler graduated in ce<br>protractor, pair of compasses, pen, HE<br>Tracing paper may be used.  |                 |                                 |  |  |

### **Instructions**

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
  - there may be more space than you need.
- Calculators may be used.

### **Information**

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

## **Advice**

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.
- Without sufficient working, correct answers may be awarded no marks.

Turn over ▶



### Answer all ELEVEN questions.

## Write your answers in the spaces provided.

## You must write down all the stages in your working.

1 The GDP per capita for a region is defined as follows

GDP per capita = 
$$\frac{\text{total GDP}}{\text{population}}$$

Complete the table below, giving each value to 2 significant figures.

| Region  | Total GDP             | Population | GDP per capita |
|---------|-----------------------|------------|----------------|
| Grenada | 1.23×10°              | 112 000    |                |
| Hungary | 1.61×10 <sup>11</sup> |            | 16500          |
| World   |                       | 7.67×10°   | 11 400         |

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| 2 | $\mathscr{E}$ is the | universal | set and | A, B | and | C are | three sets. |
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$$\mathcal{E} = \{ p, q, r, s, t \} \qquad A = \{ q, r, s \} \qquad B = \{ p, q, t \}$$

- (a) List the members of
  - (i)  $A \cap B$
  - (ii)  $A \cup B$
  - (iii)  $A' \cap B$

(3)

Given that  $A \cap C = \{r\}$ 

(b) write down all the possibilities for set C

(2)

One of the possibilities for set C is selected at random.

(c) Find the probability that this set C is such that  $B \cap C = \emptyset$ 

(2)

- **3** Given that  $2^x \times 4^y = 128$ 
  - (a) show that x + 2y = 7

(3)

Given that  $\frac{8^x}{4^y} = 32$ 

(b) show that 3x - 2y = 5

(2)

(c) Hence, or otherwise, solve the simultaneous equations

$$2^x \times 4^y = 128$$

$$\frac{8^x}{4^y} = 32$$

(3)

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| Time (t minutes)        | Frequency |
|-------------------------|-----------|
| 0 ≤ <i>t</i> < 10       | 5         |
| 10 ≤ <i>t</i> < 30      | 7         |
| $30 \leqslant t < 60$   | 15        |
| 60 ≤ <i>t</i> < 120     | 36        |
| $120 \leqslant t < 240$ | 19        |
| $240 \leqslant t < 360$ | 8         |

(a) Write down the class interval that contains the median time spent on the internet per day.

(1)

(b) Calculate an estimate for the mean time spent on the internet per day.

(4)

Sophie drew a histogram for the information in the table.

In her histogram, the bar for the class interval  $30 \le t < 60$  is a square with sides of length 3 cm.

Given that the bar for the class interval  $10 \le t < 30$  is a rectangle of width w cm and of height h cm,

(c) find the value of w and the value of h

(3)





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| 5 | A closed box is in the shape of a hollow cuboid.   |     |
|---|--|-----|
|   | The dimensions of the cuboid are 12 cm by 4.0 cm by 3.0 cm. Each length is given to 2 significant figures.   |     |
|   | A tin of paint contains enough paint to cover exactly 200 cm <sup>2</sup>  |     |
|   | (a) Determine if this tin of paint is definitely enough to cover the 6 outside faces of the closed box.  | (4) |
|   | (b) Calculate the length of the longest straight rod that can definitely fit inside the box. Give your answer to 3 significant figures. Show your working clearly. |     |
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| 6 | A, P and B are three points on horizontal ground.  |  |
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|   | A is 1 km due south of P   |  |
|   | PQ is a vertical tower.<br>The angle of elevation of $Q$ from $A$ is $16.9^{\circ}$                                  |  |
|   | (a) Show that the height of the tower, in metres to 3 significant figures, is 304 m. (2)                             |  |
|   | B is 2 km due east of $P$  |  |
|   | BC is a vertical radio mast.<br>The angle of elevation of $Q$ from $C$ , the top of the radio mast, is $8.2^{\circ}$ |  |
|   | (b) Calculate the size, in degrees to one decimal place, of the angle of elevation of $C$ from $A$ (5)               |  |
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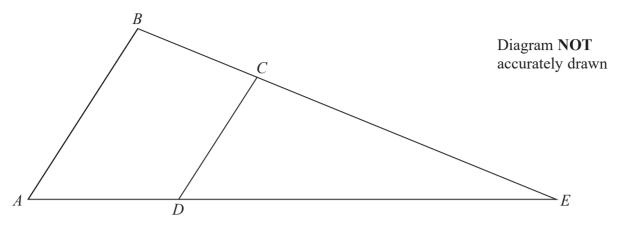


Figure 1

Figure 1 shows quadrilateral  $\overrightarrow{ABCD}$  such that  $\overrightarrow{AB} = \mathbf{a}$  and  $\overrightarrow{AD} = \mathbf{b}$ 

E is the point such that ADE and BCE are straight lines.

Given that  $\overrightarrow{BC} = \mathbf{b} - \frac{1}{3}\mathbf{a}$ 

(a) show that AB is parallel to DC

(2)

Given also that  $\lambda$  is a scalar such that  $\overrightarrow{BE} = \lambda \mathbf{b} - \mathbf{a}$ 

(b) find the value of  $\lambda$ 

(2)

The area of triangle ABE is x square units.

Given that the area of quadrilateral ABCD is P square units,

(c) find an expression for P in terms of x

(3)





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| Question 7 continued |  |
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(Total for Question 7 is 7 marks)

0.9 m

Diagram **NOT** accurately drawn

Figure 2

Figure 2 shows the design for a garden feature.

In the middle of the feature is a circular pond.

The pond is surrounded by 6 identical flower beds.

Each flower bed is in the shape of an isosceles trapezium.

(a) Calculate the area, in m<sup>2</sup> to 3 significant figures, of one of the flower beds.

(3)

Each flower bed needs to be filled with compost to a depth of 10 cm. The compost is sold in bags containing 50 litres of compost.

(b) Show that 16 bags of compost will be needed to fill all six flower beds to a depth of 10 cm. Show your working clearly.

(4)

(c) Find the area of the circular pond. Give your answer in m<sup>2</sup> to 3 significant figures.

(4)

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| Area of trapezium = $\frac{1}{2}(a+b)h$ (Total for Question 8 is 11 marks | ` |



9 [In this question the coordinates of the points are given in centimetres]

The points with coordinates (1, 1), (2, 4), (4, 6) and (3, 3) are the vertices of quadrilateral A

(a) On the grid opposite, draw and label quadrilateral A

(1)

Quadrilateral A is transformed to quadrilateral B by a rotation of 90° anticlockwise about the origin, O

(b) On the grid opposite, draw and label quadrilateral B

**(2)** 

Quadrilateral B is transformed to quadrilateral C under the transformation with matrix M where

$$\mathbf{M} = \begin{pmatrix} 1 & 3 \\ 1 & 1 \end{pmatrix}$$

(c) On the grid opposite, draw and label quadrilateral C

(3)

(d) Calculate the determinant of **M** 

(1)

(e) Calculate the area of quadrilateral A

(2)

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Determinant of matrix 
$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} = ad - bc$$



Turn over for a spare grid if you need to redraw your shapes.

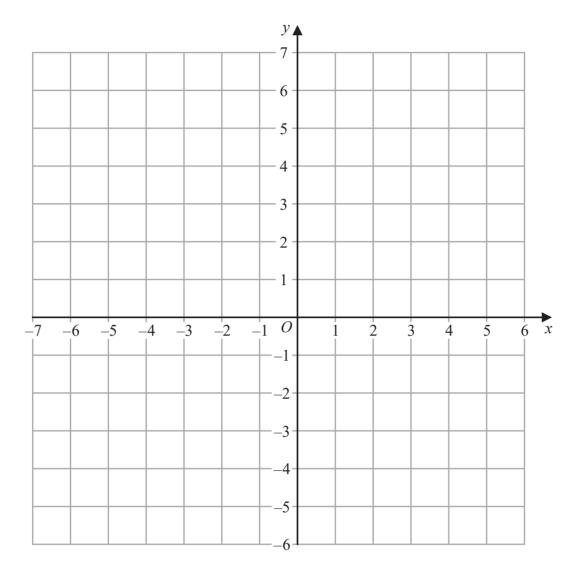
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# **Question 9 continued**

Only use this grid if you need to redraw your shapes.



(Total for Question 9 is 9 marks)

The shape in Figure 3 is then folded along the dotted lines to form a box, without a lid, in the shape of a cuboid, shown in Figure 4

The volume of the box is  $V \text{cm}^3$ 

(a) Show that  $V = 4x^3 - 60x^2 + 200x$ 

(2)

(b) Find, to 3 significant figures, the value of x such that  $\frac{dV}{dx} = 0$ 

(4)

Solutions of 
$$ax^2 + bx + c = 0$$
 are  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

Question 10 parts (c), (d), (e) and (f) continue on page 26

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### **Question 10 continued**

(c) Complete the following table of values for  $V = 4x^3 - 60x^2 + 200x$ 

| x | 0 | 1   | 1.5   | 2.5   | 3 | 3.5   | 4 | 5 |
|---|---|-----|-------|-------|---|-------|---|---|
| V | 0 | 144 | 178.5 | 187.5 |   | 136.5 |   | 0 |

(2)

(d) On the grid opposite, plot the points from your completed table and, using your answer to part (b), join them to form a smooth curve.

**(2)** 

(e) By drawing on the grid a tangent to the curve, find an estimate of the gradient of the curve at the point where x = 1.5

(2)

Starting with a square of side  $15 \, \text{cm}$  and removing a square with sides of length  $x \, \text{cm}$  from each corner, a second box without a lid is formed by folding as in part (a).

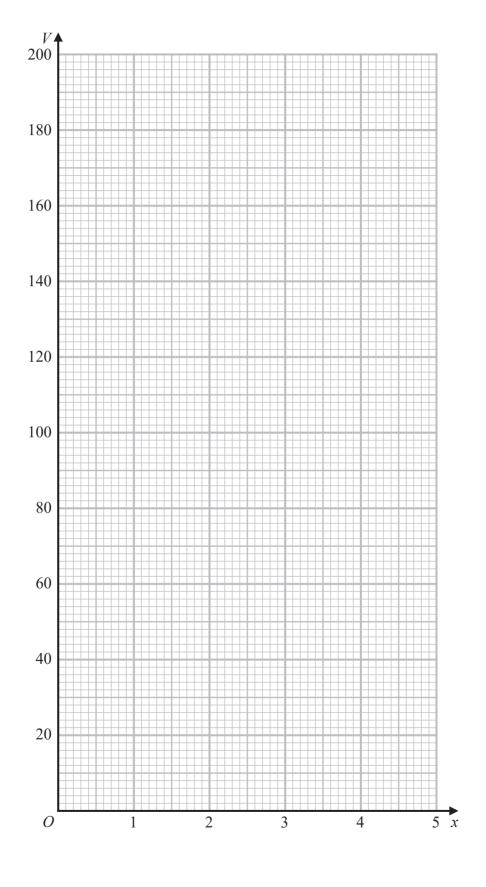
The volume of this box is  $B \text{ cm}^3$  where  $B = 4x^3 - 60x^2 + 225x$ 

Given that B = 200

(f) find, by drawing a suitable straight line on the grid, estimates, to one decimal place, of the possible values of x

(3)

# **Question 10 continued**



Turn over for a spare grid if you need to redraw your curve.



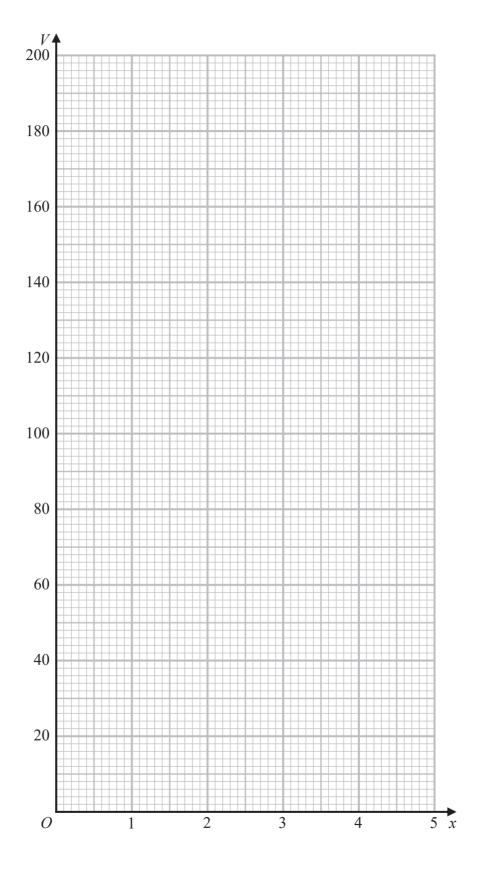
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# **Question 10 continued**

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$$f: x \mapsto \frac{3x+1}{x-1}$$

- (a) Find f(3) (2)
- (b) State the value of x that must be excluded from any domain of the function f (1)
- (c) Find the inverse of the function f
  Give your answer in its simplest form.

  (4)

The function g is such that

$$fg(x) = \frac{x-1}{3x+1}$$

(d) Find the value of a such that gf(a) = fg(a)

| Question 11 continued |                                     |
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