## GCE

# Further Mathematics B MEI 

Y411/01: Mechanics A

AS Level

Mark Scheme for June 2022

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

## MARKING INSTRUCTIONS

## PREPARATION FOR MARKING

## RM ASSESSOR

1. Make sure that you have accessed and completed the relevant training packages for on-screen marking: RM Assessor Online Training; OCR Essential Guide to Marking.
2. Make sure that you have read and understood the mark scheme and the question paper for this unit. These are posted on the RM Cambridge Assessment Support Portal http://www.rm.com/support/ca
3. Log-in to RM Assessor and mark the required number of practice responses ("scripts") and the number of required standardisation responses.

YOU MUST MARK 10 PRACTICE AND 10 STANDARDISATION RESPONSES BEFORE YOU CAN BE APPROVED TO MARK LIVE SCRIPTS.

## MARKING

1. Mark strictly to the mark scheme.
2. Marks awarded must relate directly to the marking criteria.
3. The schedule of dates is very important. It is essential that you meet the RM Assessor $50 \%$ and $100 \%$ (traditional $40 \%$ Batch 1 and 100\% Batch 2) deadlines. If you experience problems, you must contact your Team Leader (Supervisor) without delay.
4. If you are in any doubt about applying the mark scheme, consult your Team Leader by telephone or the RM Assessor messaging system, or by email.

## 5. Crossed Out Responses

Where a candidate has crossed out a response and provided a clear alternative then the crossed out response is not marked. Where no alternative response has been provided, examiners may give candidates the benefit of the doubt and mark the crossed out response where legible.

## Rubric Error Responses - Optional Questions

Where candidates have a choice of question across a whole paper or a whole section and have provided more answers than required, then all responses are marked and the highest mark allowable within the rubric is given. Enter a mark for each question answered into RM assessor, which will select the highest mark from those awarded. (The underlying assumption is that the candidate has penalised themselves by attempting more questions than necessary in the time allowed.)

## Multiple Choice Question Responses

When a multiple choice question has only a single, correct response and a candidate provides two responses (even if one of these responses is correct), then no mark should be awarded (as it is not possible to determine which was the first response selected by the candidate).

## Contradictory Responses

When a candidate provides contradictory responses, then no mark should be awarded, even if one of the answers is correct.
Short Answer Questions (requiring only a list by way of a response, usually worth only one mark per response)
Where candidates are required to provide a set number of short answer responses then only the set number of responses should be marked. The response space should be marked from left to right on each line and then line by line until the required number of responses have been considered. The remaining responses should not then be marked. Examiners will have to apply judgement as to whether a 'second response' on a line is a development of the 'first response', rather than a separate, discrete response. (The underlying assumption is that the candidate is attempting to hedge their bets and therefore getting undue benefit rather than engaging with the question and giving the most relevant/correct responses.)

Short Answer Questions (requiring a more developed response, worth two or more marks)
If the candidates are required to provide a description of, say, three items or factors and four items or factors are provided, then mark on a similar basis - that is downwards (as it is unlikely in this situation that a candidate will provide more than one response in each section of the response space.)

Longer Answer Questions (requiring a developed response)
Where candidates have provided two (or more) responses to a medium or high tariff question which only required a single (developed) response and not crossed out the first response, then only the first response should be marked. Examiners will need to apply professional judgement as to whether the second (or a subsequent) response is a 'new start' or simply a poorly expressed continuation of the first response.
6. Always check the pages (and additional objects if present) at the end of the response in case any answers have been continued there. If the candidate has continued an answer there then add a tick to confirm that the work has been seen.
7. Award No Response (NR) if:

- anything is written in the answer space and is not worthy of credit (this includes text and symbols).

Team Leaders must confirm the correct use of the NR button with their markers before live marking commences and should check this when reviewing scripts.
8. The RM Assessor comments box is used by your team leader to explain the marking of the practice responses. Please refer to these comments when checking your practice responses. Do not use the comments box for any other reason.
If you have any questions or comments for your team leader, use the phone, the RM Assessor messaging system, or e-mail.
9. Assistant Examiners will send a brief report on the performance of candidates to their Team Leader (Supervisor) via email by the end of the marking period. The report should contain notes on particular strengths displayed as well as common errors or weaknesses. Constructive criticism of the question paper/mark scheme is also appreciated.
10. For answers marked by levels of response:
a. To determine the level - start at the highest level and work down until you reach the level that matches the answer
b. To determine the mark within the level, consider the following:

| Descriptor | Award mark |
| :--- | :--- |
| On the borderline of this level and the one <br> below | At bottom of level |
| Just enough achievement on balance for this <br> level | Above bottom and either below middle or at middle of level (depending on number of marks <br> available) |
| Meets the criteria but with some slight <br> inconsistency | Above middle and either below top of level or at middle of level (depending on number of <br> marks available) |
| Consistently meets the criteria for this level | At top of level |

## Text Instructions

## 1. Annotations and abbreviations

| Annotation in scoris | Meaning |
| :--- | :--- |
| $\checkmark$ and $\boldsymbol{x}$ |  |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| E | Explanation mark 1 |
| SC | Special case |
| ^ | Omission sign |
| MR | Misread |
| BP | Blank page |
| Highlighting |  |
|  | Meaning |
| Other abbreviations <br> mark scheme |  |
| E1 | Mark for explaining a result or establishing a given result |
| dep* | Mark dependent on a previous mark, indicated by *. The * may be omitted if only previous M mark. |
| cao | Correct answer only |
| oe | Orequivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |
| AG | Answer given |
| awrt | Anything which rounds to |
| BC | By Calculator |
| DR | This indicates that the instruction In this question you must show detailed reasoning appears in the question. |

## 2. Subject-specific Marking Instructions for AS Level Mathematics B (MEI)

a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ${ }^{\wedge}$ ) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

## Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).
If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.
b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader.

C The following types of marks are available.
M
A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an $M$ mark may be specified.
A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.

E
A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.
d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case, please escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km , when this would be assumed to be the unspecified unit.)
We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

- When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
- When a value is not given in the paper accept any answer that agrees with the correct value to $\mathbf{2}$ s.f. unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.
NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads " 3 s.f"
Follow through should be used so that only one mark in any question is lost for each distinct accuracy error. Candidates using a value of $9.80,9.81$ or 10 for $g$ should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

Rules for replaced work and multiple attempts:

- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
- If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
- if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold "In this question you must show detailed reasoning", or the command words "Show" and "Determine. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

If in any case the scheme operates with considerable unfairness consult your Team Leader.


| Question |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | (a) |  | B1 <br> B1 | 1.1 $1.1$ | Closed triangle with all lengths present, and sides parallel to the relevant forces. Arrowheads and units not needed. Allow magnitudes written at arrowheads <br> $\theta$ correctly indicated on diagram (not necessarily as internal angle of the triangle) |  |
|  |  |  | [2] |  |  |  |
|  | (b) | $\cos \theta=\frac{45^{2}+38^{2}-33^{2}}{2 \cdot 45 \cdot 38}$ | M1 | 1.1a | Correct application of cos rule e.g $33^{2}=45^{2}+38^{2}-2(45)(38) \cos \theta$ |  |
|  |  | $\theta \approx 45.9005 \ldots$ | A1 | 1.1 | Condone $0.80111 \ldots$ radians |  |
|  |  |  | [2] |  |  |  |
|  | (c) | Let the angle between the 33 and $P$ sides be $A$. |  |  |  |  |
|  |  | $\sin A=\frac{\sin 40^{\circ}}{33} \times 45$ | M1 | 1.1 | Correct application of sine rule |  |
|  |  | $A=61.2263 \ldots{ }^{\circ} \text { or } A=118.7736 \ldots{ }^{\circ}$ <br> So the third angle is either $21.2263 \ldots{ }^{\circ}$ or $78.7736 \ldots{ }^{\circ}$ | M1 | 1.1 | Two possibilities for $A$, the complement of each other in $180^{\circ}$ and two values for third angle: $140^{\circ}$ - their possibilities for $A$ |  |
|  |  | So either $P=\frac{33}{\sin 40^{\circ}} \times \sin \left(21.2263 \ldots{ }^{\circ}\right)=18.5874 \ldots$ or $P=\frac{33}{\sin 40^{\circ}} \times \sin \left(78.7736 \ldots{ }^{\circ}\right)=50.3565 \ldots$ | A1 | 1.1 | Both |  |
|  |  | Alternative to (c): |  |  |  |  |
|  |  | $33^{2}=P^{2}+45^{2}-2 \cdot P \cdot 45 \cos 40^{\circ}$ | M1 |  | Correct application of cos rule |  |
|  |  | $\Rightarrow P^{2}-90 \cos 40^{\circ} \cdot P+936=0$ | M1 |  | Rearranging to standard quadratic form, e.g. $P^{2}-68.94 P=-936$ |  |
|  |  | $P=18.5874 \ldots$ or $50.3565 \ldots$ | A1 |  | Both |  |
|  |  |  | [3] |  |  |  |


| Question |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | (a) | Let A be the origin of a coordinate system with $x$ and $y$ axes pointing in directions $\overrightarrow{\mathrm{AB}}$ and $\overrightarrow{\mathrm{AD}}$ respectively. Let the lamina have mass $m \mathrm{~kg}$. |  |  |  |  |
|  |  | Centre of mass of lamina lies 10 cm above AB | M1 | 1.2 | soi |  |
|  |  | $(m+1.7) \times 11.7=1.7 \times 15+m \times 10$ | M1 | 1.1 | M0 if 16.5 used instead of 11.7 | Using their 10 |
|  |  | $\Rightarrow m=3.3$ | A1 | 2.2a | AG |  |
|  |  |  | [3] |  |  |  |
|  | (b) | $3.3 \times \frac{1}{3} x+1.7 \times \frac{1}{2} x=5 \times 16.5$ | M1 | 1.1 | Allow equation involving $m$ Allow 11.7 if 16.5 used in (a) M0 for $2 / 3 x$ | Can award both marks for work in (a) |
|  |  | $\Rightarrow x \approx 42.3 \quad(3 \mathrm{sf})$ | A1 | 1.1 | Accept a value rounding to 42.3 |  |
|  |  | Alternatively, M lies on AC, so $x / 30=11.7 / 16.5$ | M1 |  |  |  |
|  |  | $\Rightarrow x \approx 42.3 \quad(3 \mathrm{sf})$ | A1 |  | Accept a value rounding to 42.3 |  |
|  |  |  | [2] |  |  |  |
|  | (c) | $Q \sin 30^{\circ} \times 32=5 g \times 16.5$ | M1 | 1.1 | Allow omission of $g$ |  |
|  |  | $\Rightarrow Q=50.53125 \approx 50.5$ | A1 | 1.1 | AG |  |
|  |  |  | [2] |  |  |  |
|  | (d) | Let the tension in the string be $T \mathrm{~N}$. |  |  |  |  |
|  |  | $\begin{aligned} & (T \cos \phi=) 5 g-Q \sin 30^{\circ} \quad(=23.73) \\ & (T \sin \phi=) Q \cos 30^{\circ} \quad(=43.76) \end{aligned}$ | M1 | 3.3 | Resolving into horizontal and vertical components. Condone sin / cos switched. | May take moments |
|  |  | $\tan \phi=1.8437 \ldots$ | M1 | 3.1a | Using tan. Allow tan $^{-1}$ (23.7/43.8) |  |
|  |  | $\Rightarrow \phi=61.5263 \ldots{ }^{\circ}$ | A1 | 1.1 | Allow 1.073838... rad | Accept 61-62 |
|  |  | Alternatively: all three lines of action must concur, so ... |  |  |  |  |
|  |  | $\mathrm{XN}=15.5 \tan 30^{\circ}$ | M1 |  | Attempt to find XN |  |
|  |  | $\tan \phi=16.5 / \mathrm{XN}$ | M1 |  | Using tan in triangle including $\phi$ |  |
|  |  | $\Rightarrow \phi=61.5263 \ldots{ }^{\circ}$ | A1 |  |  |  |


| Question |  | Answer | Marks | AOs |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Guidance |  |
|  |  | Alternatively, using triangle of forces |  |  |  |  |  |
|  |  | $T^{2}=(5 g)^{2}+50.53^{2}-2(5 g)(50.53) \cos 60 \quad(T=49.78)$ | M1 |  | Equation involving $T$ |  |  |
|  |  | $\sin \phi / 50.53=\sin 60 / T$ | M1 |  |  |  |  |
|  |  | $\phi=61.5$ | A1 |  |  |  |  |
|  |  |  | $[3]$ |  |  |  |  |


| Question |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | (a) | Let the distance travelled be $x \mathrm{~m}$. |  |  |  |  |
|  |  | $\frac{1}{2} \cdot 240 \cdot 3^{2}+240 g \cdot 25-120 x=\frac{1}{2} \cdot 240 \cdot 18^{2}$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \end{aligned}$ | $\begin{aligned} & 1.1 \\ & 3.4 \end{aligned}$ | One correct term. <br> Attempt at WEP with correct number of terms (condone sign errors). |  |
|  |  | $x=175$ | A1 | 1.1 |  |  |
|  |  |  | [3] |  |  |  |
|  | (b) | Let the engine do $E \mathrm{~J}$ of work from B to A . |  |  |  |  |
|  |  | $E-120 \cdot 175=\frac{1}{2} \cdot 240 \cdot 7^{2}+240 g \cdot 25(\Rightarrow E=85680)$ | M1 | 3.3 | Must have equation which gives correct amount of work done. | Using their $x$ |
|  |  | Average power $=85680 \div 30=2856 \mathrm{~W}$ | A1 | 2.2a | AG, so must see reference to work done $\div 30$ <br> (e.g. $30 P=85680$ ) |  |
|  |  |  | [2] |  |  |  |
|  | (c) | Let the snowmobile have driving force $D \mathrm{~N}$. When travelling at maximum speed $v \mathrm{~ms}^{-1}$, acceleration up the slope is zero. |  |  |  |  |
|  |  | ( $D=$ ) $240 \mathrm{~g} \sin 12^{\circ}+120 \quad(=609)$ | M1 | 3.3 | M0 if $g$ omitted |  |
|  |  | $6000=D v$ | M1 | 3.4 | Applying $P=F v$ with $P=6000$ and Fis driving force (or force down the slope) stated or implied |  |
|  |  | $v=9.85208 \ldots$ | A1 | 1.1 |  |  |
|  |  |  | [3] |  |  |  |
|  | (d) | Work done in lifting the mass |  |  |  |  |
|  |  | $=(550 \div 2.2) \times 9.8 \times(1 \div 3.28)$ | M1 | 1.1 | Using $m g h$ with attempts to convert 550 lb and 1 ft . Condone conversion factors misapplied. <br> M0 if $g$ omitted M1A0 if KE is considered as well |  |
|  |  | $\approx 747 \mathrm{~W}$ | A1 | 2.2b |  |  |
|  |  |  | [2] |  |  |  |


| Question |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | (a) | If it were inelastic, the sphere would stick to the wall (but it doesn't). | B1 | 2.4 |  |  |
|  |  |  | [1] |  |  |  |
|  | (b) | Let the coefficient of restitution be $e$. |  |  |  |  |
|  |  | $5 e^{2}=3.2$ | M1 | 1.1 | Or $v / 5=3.2 / v(=e) \quad(v=4)$ |  |
|  |  | $e=0.8$ | A1 | 1.1 |  |  |
|  |  |  | [2] |  |  |  |
|  | (c) | A and B take $\frac{5}{2}$ and $\frac{5}{3}$ seconds respectively to reach their walls. | M1 | 3.1b |  |  |
|  |  | So B travels an additional $\left(\frac{5}{2}-\frac{5}{3}\right) \times 0.3 \times 0.8=0.2 \mathrm{~m}$ | M1 | 1.1 | Using their e, but M0 for 0.3/e |  |
|  |  | The remaining 0.8 m is covered in the ratio $2: 3$ so spheres meet $\frac{2}{5} \times 0.8=0.32 \mathrm{~m}$ from left-hand wall. | A1 ft | 1.1 | FT is $0.4-0.1 e$ |  |
|  |  | Alternatively, let $d \mathrm{~m}$ be the distance from the left-hand wall at which A and B meet again. |  |  |  |  |
|  |  | $\frac{0.5}{0.2}+\frac{d}{0.2 e}=\frac{0.5}{0.3}+\frac{1-d}{0.3 e}$ | M1 M1 |  | For 0.5/0.2 and 0.5/0.3; OR attempt at expression representing time to impact for either A or B. For correct equation involving $d$ and their $e$. | Or other complete method for $d$ |
|  |  | $\Rightarrow d=0.32$ | A1 ft |  | FT is $0.4-0.1 e$ |  |
|  |  |  | [3] |  |  |  |


| Question |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | (a) | Let the frictional force up the slope have magnitude $F \mathrm{~N}$ and the normal contact force have magnitude $R \mathrm{~N}$. |  |  |  |  |
|  |  | $R=m g \cos \alpha$ and $m g \sin \alpha=F$ | M1 | 3.3 | Both soi Condone $\theta$ used instead of $\alpha$ |  |
|  |  | Limiting equilibrium $\Rightarrow F=F_{\max }=\mu R$ | M1 | 3.4 | soi <br> $m g \sin \alpha=\mu m g \cos \alpha$ implies M1M1 <br> Not inequality (unless recovered) |  |
|  |  | $\frac{m g \sin \alpha}{m g \cos \alpha}=\frac{\frac{5}{9} R}{R} \Rightarrow \tan \alpha=\frac{5}{9}$ | A1 | 1.1 | AG, requires proper explanation throughout <br> (e.g. $F=\mu R$ preceding eqn above) |  |
|  |  |  | [3] |  |  |  |
|  | (b) | Let the block have acceleration $a \mathrm{~ms}^{-2}$ down the slope. |  |  |  |  |
|  |  | Block slides so $F=F_{\max }=\frac{5}{9} m g \cos 40^{\circ}$ | M1 | 3.5a | Accept $F=\mu m g \cos \alpha$ |  |
|  |  | $m g \sin 40^{\circ}-\frac{5}{9} m g \cos 40^{\circ}=m a \Rightarrow a=2.12863 \ldots$ | A1 | 1.1 |  |  |
|  |  |  | [2] |  |  |  |
|  | (c) | $R=m g \cos \alpha+P \sin \alpha$ | B1 | 3.3 | soi |  |
|  |  | So for equilibrium to be broken, we require $P \cos \alpha>m g \sin \alpha+\frac{5}{9}(m g \cos \alpha+P \sin \alpha)$ | M1 | 2.1 | $\begin{aligned} & \text { Any correct form } P \cos \alpha>\ldots \text { e.g. } \\ & P \cos \alpha>m g \sin \alpha+F_{\max } \text { or } \\ & P \cos \alpha>m g \sin \alpha+\mu R \\ & \text { M0 for 'Limiting when } P \cos \alpha=\ldots \text {, } \\ & \text { unless inequality is correctly } \\ & \text { argued later } \end{aligned}$ | M0 for sliding down the slope ( $F$ acting upwards) |
|  |  | $\Rightarrow P\left(\cos \alpha-\frac{5}{9} \sin \alpha\right)>m g\left(\frac{5}{9} \cos \alpha+\sin \alpha\right)$ | A1 | 2.2a | AG |  |
|  |  |  | [3] |  |  |  |
|  | (d) | $\cos \alpha_{\text {min }}-\frac{5}{9} \sin \alpha_{\text {min }}=0$ | M1 | 3.1a | Accept arguments made in terms of inequalities. |  |
|  |  | $\alpha_{\text {min }}=60.94539 \ldots{ }^{\circ}$ | A1 | 1.1 | Allow 1.0636978... radians. |  |
|  |  |  | [2] |  |  |  |


| Question |  |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | (a) | (i) | $480 \times 4=1920$ (Ns) | B1 | 1.1 | Condone missing / incorrect units. |  |
|  |  |  |  | [1] |  |  |  |
|  |  | (ii) | Let the final speed of the trolley be $u \mathrm{~m} \mathrm{~s}^{-1}$. |  |  |  |  |
|  |  |  | $320 u=1920 \Rightarrow u=6$ | B1 | 3.3 |  |  |
|  |  |  |  | [1] |  |  |  |
|  | (b) |  | Let the speed of the trolley after the first firing be $v \mathrm{~ms}^{-1}$ in the forwards direction. |  |  |  |  |
|  |  |  | $5(v-90)+315 v=1920$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \end{aligned}$ | $\begin{aligned} & \hline 3.3 \\ & 3.4 \end{aligned}$ | Attempt at COLM Correct equation, using expressions in a single variable which differ by 90 , or two variables with an equation to indicate their difference is 90 . <br> MIMOAO for $320 v-5 \times 90=320 \times 6$ unless correctly justified | Using their u |
|  |  |  | $\Rightarrow v=7.40625 \approx 7.41$ | A1 | 2.2a | AG |  |
|  |  |  |  | [3] |  |  |  |
|  | (c) |  | Let the speed of the trolley after the second firing be $w \mathrm{~ms}^{-1}$ in the forwards direction. |  |  |  |  |
|  |  |  | $310 w+5(w+90)=315 \times 7.40625$ | M1 | 3.1b | Correct equation(s) <br> Allow $315 w+5 \times 90=315 \times 7.41$ <br> without explanation | M0 if signs wrong |
|  |  |  | $\Rightarrow w=5.97767 \ldots$ | A1 | 1.1 | Value rounding to 5.98 |  |
|  |  |  | $\frac{\text { Final KE }}{\text { Initial KE }}=\frac{5.97767 \ldots{ }^{2}}{6^{2}}(=0.9925733 \ldots)$ | M1 | 3.4 | For final KE (or change) divided by initial KE (using their $u=6$ ). Allow wrong/different masses |  |
|  |  |  | which is a loss of $0.74 \%$. | A1 cao | 1.1 | 0.6-1.0 and loss (by valid method) |  |
|  |  |  |  | [4] |  |  |  |
|  | (d) |  | We require everything other than the cannon ball being fired to be modelled as a single particle, but, e.g. driver is likely to shift about. <br> OR There is likely to be some friction / air resistance | B1 | 3.5b | Mention of particle model or friction or air resistance, etc | Or other suitable answer. |
|  |  |  |  | [1] |  |  |  |

## Need to get in touch?

If you ever have any questions about OCR qualifications or services (including administration, logistics and teaching) please feel free to get in touch with our customer support centre.

Call us on
01223553998
Alternatively, you can email us on
support@ocr.org.uk
For more information visit

ocr.org.uk/qualifications/resource-finder
ocr.org.uk
f Twitter/ocrexams
3) locrexams
in /company/ocr

- locrexams


## 바웅 CAMBRIDGE <br> unvurrtit press a smsssment

OCR is part of Cambridge University Press \& Assessment, a department of the University of Cambridge.
For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored. © OCR 2022 Oxford Cambridge and RSA Examinations is a Company Limited by Guarantee. Registered in England. Registered office The Triangle Building, Shaftesbury Road, Cambridge, CB2 8EA.

Registered company number 3484466 . OCR is an exempt charity.
OCR operates academic and vocational qualifications regulated by Ofqual, Qualifications Wales and CCEA as listed in their qualifications registers including A Levels, GCSEs, Cambridge Technicals and Cambridge Nationals.

OCR provides resources to help you deliver our qualifications. These resources do not represent any particular teaching method we expect you to use. We update our resources regularly and aim to make sure content is accurate but please check the OCR website so that you have the most up-to-date version. OCR cannot be held responsible for any errors or omissions in these resources.

Though we make every effort to check our resources, there may be contradictions between published support and the specification, so it is important that you always use information in the latest specification. We indicate any specification changes within the document itself, change the version number and provide a summary of the changes. If you do notice a discrepancy between the specification and a resource, please contact us.

Whether you already offer OCR qualifications, are new to OCR or are thinking about switching, you can request more information using our Expression of Interest form.

Please get in touch if you want to discuss the accessibility of resources we offer to support you in delivering our qualifications.

